



**THERMAL EVOLUTION OF ACCRETING NEUTRON STARS  
AT HIGH ACCRETION RATES:  
ENERGY LEAKAGE TOWARDS THE  
INTERIOR OF THE STAR?**

**MARTIN JAVIER NAVA CALLEJAS**

**IRENA-INT JOINT WORKSHOP ON THERMAL AND MAGNETIC EVOLUTION OF  
NEUTRON STARS**

**DECEMBER 9TH, 2024**

# OVERVIEW

PREFACE

CHAPTER 1. ENVELOPES WITH ACCRETION: STATIONARY STATES

CHAPTER 2. THERMAL EVOLUTION: A FIRST LOOK

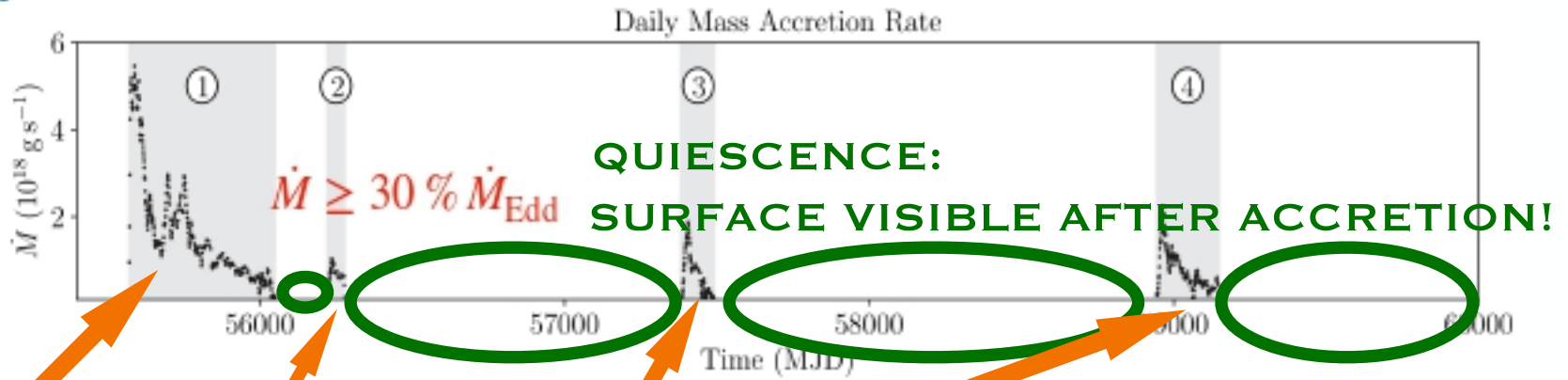
EPILOGUE

# PREFACE

(A SORT OF HOMECOMING)

# LMXBs: BURN AND RELAX

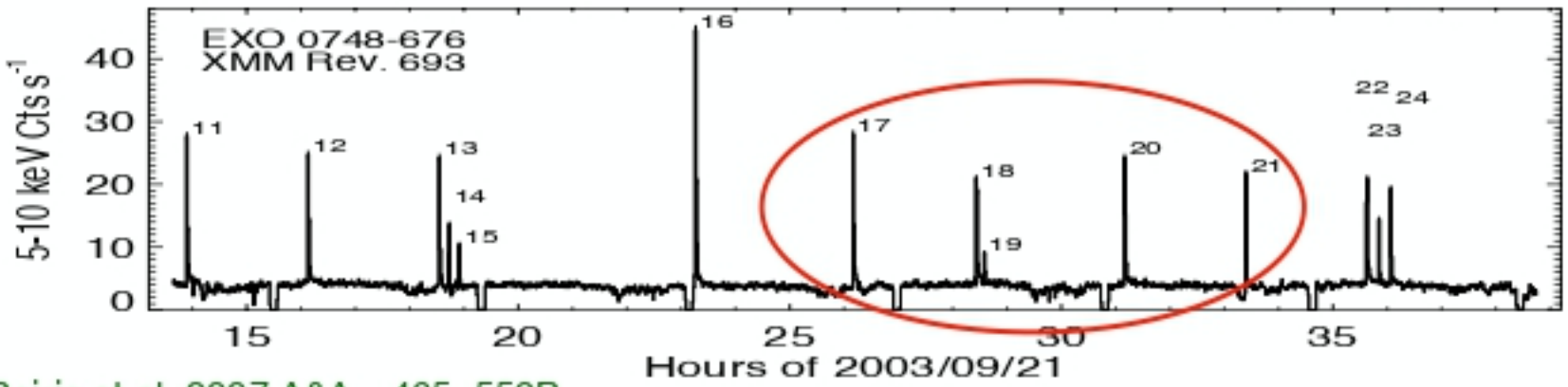
## MAXI J0556-332: Transient accretion of months



Page et al 2022, ApJ 933, 216

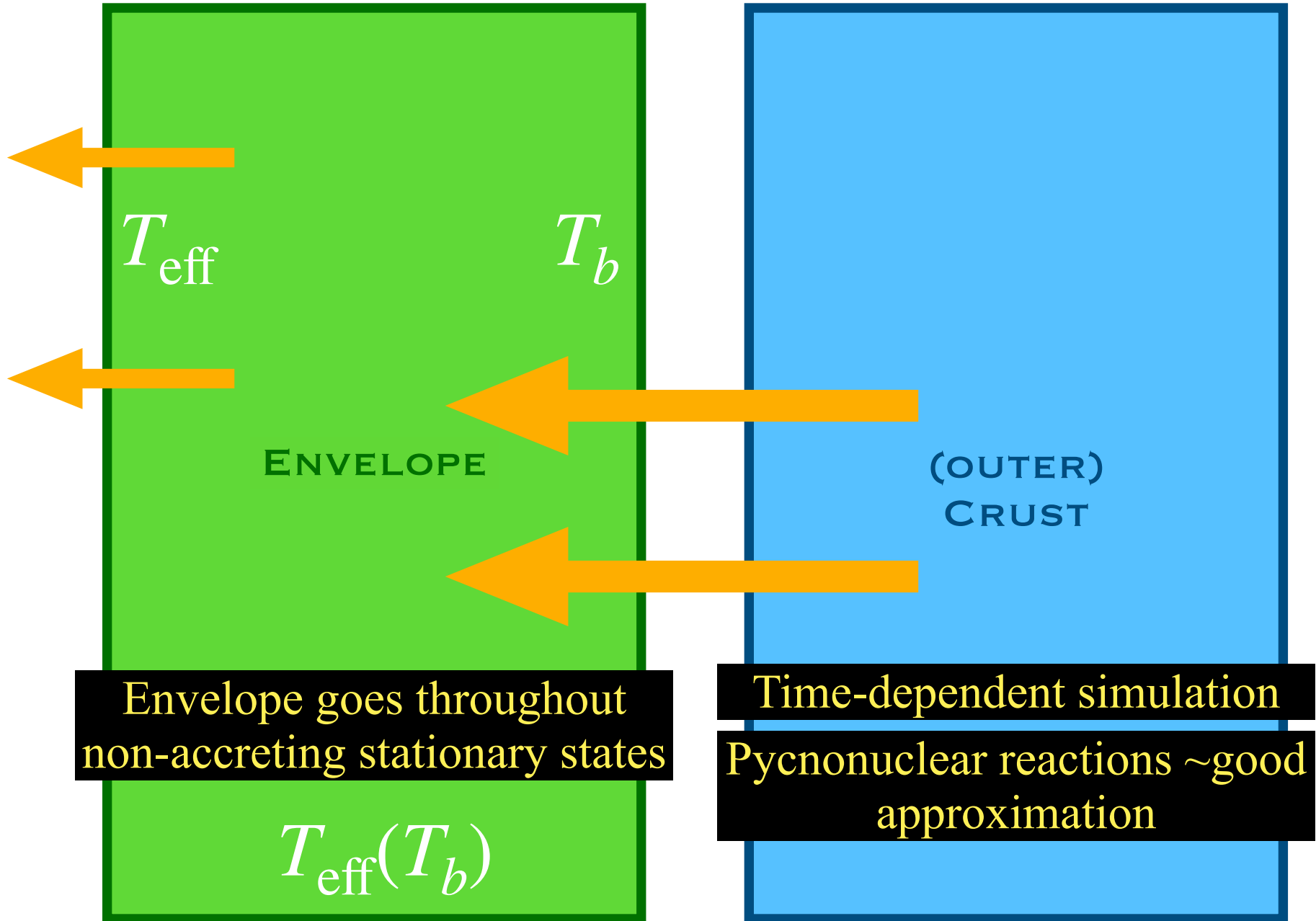
STABLE/UNSTABLE NUCLEAR BURNING

## EXO 0748-676: Accretion and X-ray bursts



Boirin et al, 2007 A&A...465..559B

# CURRENT PARADIGM

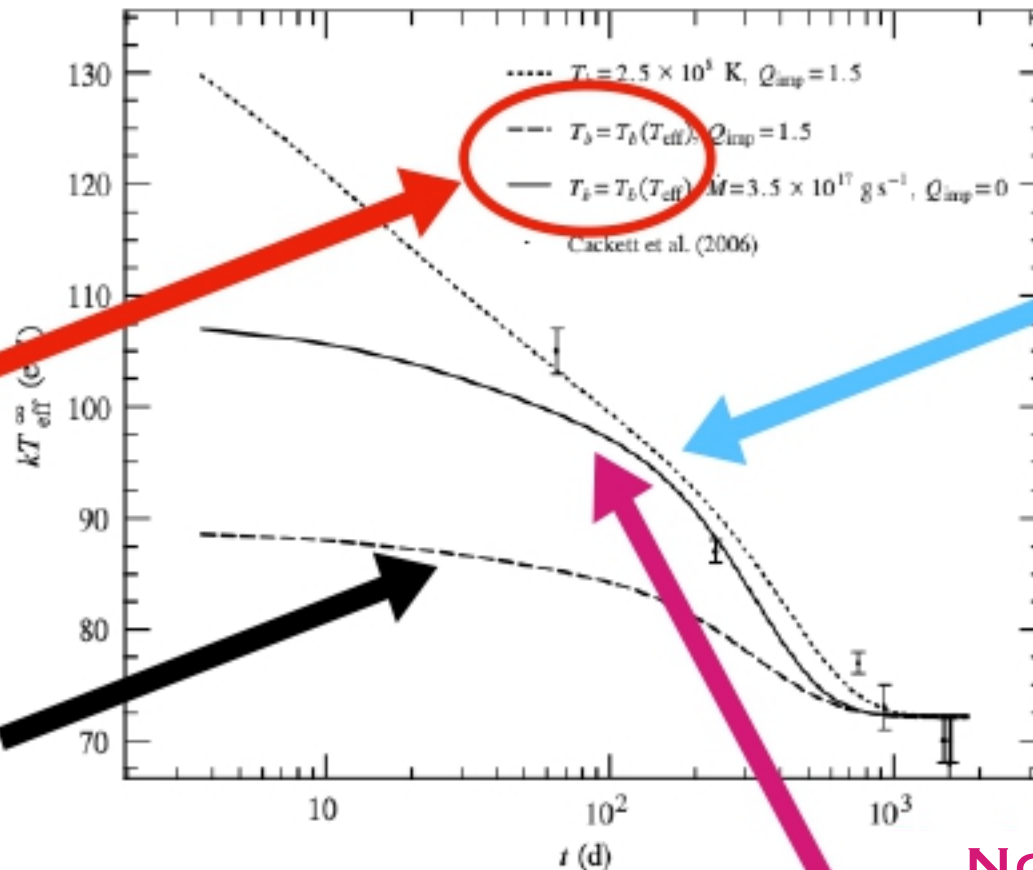


# The *shallow heating* open question

STATIONARY  
APPROXIMATION  
FOR THE  
ENVELOPE:

$$T_b(T_{\text{eff}})$$

WITHOUT  
SHALLOW  
HEATING



WITH  
SHALLOW  
HEATING

NO SHALLOW  
HEATING BUT  
DIFFERENT  
ACCRETION RATE

# DO WE NEED TO CHECK THE ENVELOPE?

## A “Hyperburst” in the MAXI J0556–332 Neutron Star: Evidence for a New Type of Thermonuclear Explosion

Dany Page<sup>1</sup>, Jeroen Homan<sup>2</sup>, Martín Nava-Callejas<sup>1</sup>, Yuri Cavecchi<sup>1</sup>, Mikhail V. Beznogov<sup>1,3</sup>, Nathalie Degenaar<sup>4</sup>, Rudy Wijnands<sup>4</sup>, and Aastha S. Parikh<sup>4</sup>

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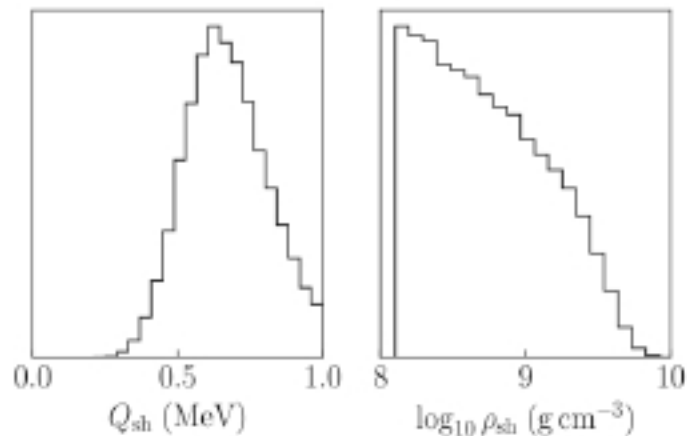


Figure 9. Histograms of the distribution of the shallow heating strength,  $Q_{sh}$ , and lower density,  $\rho_{sh}$ , in scenario “C.”

**MONTE-CARLO MARKOV CHAIN SIMULATIONS (MCMC): FIND THE “BEST” PARAMETERS TO ADJUST OBSERVATIONS**

**APPARENTLY, SHALLOW HEATING MIGHT COME FROM THE ENVELOPE**

# THEORY VS OBSERVATION OF X-RAY BURSTS

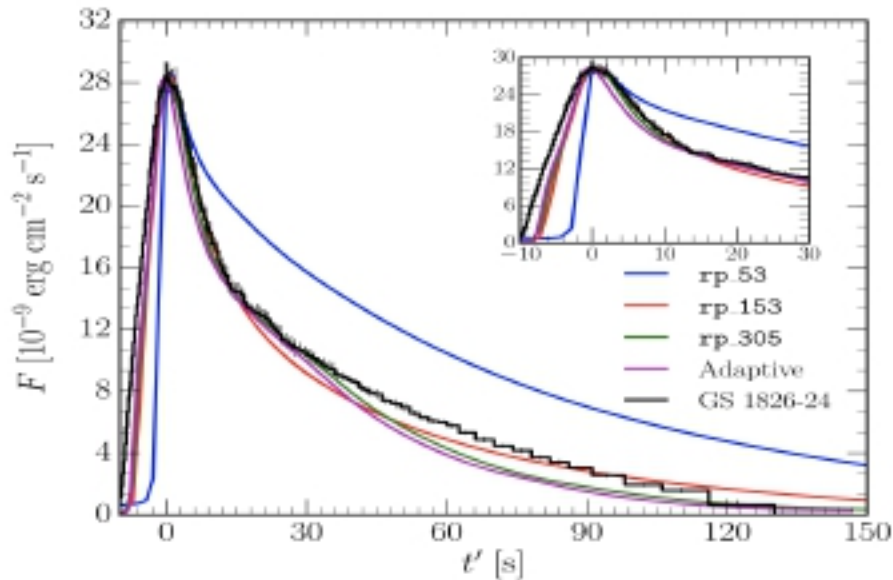


Figure: A typical X-ray burst over GS 1826–24 (black) against theoretical models employing **MESA**

- Observationally they occur at  $\dot{M} < 0.3\dot{M}_{\text{Edd}} (\approx 10^{-9} M_{\odot} \text{ yr}^{-1})$
- Explosions start at  $\sim 10^{5.75} \text{ g cm}^{-3} \equiv$  **ENVELOPE**
- From H into Fe and beyond:  
*rp-process*

**Time-dependent codes such as MESA\* are required!**



# THEORY VS OBSERVATION OF X-RAY BURSTS

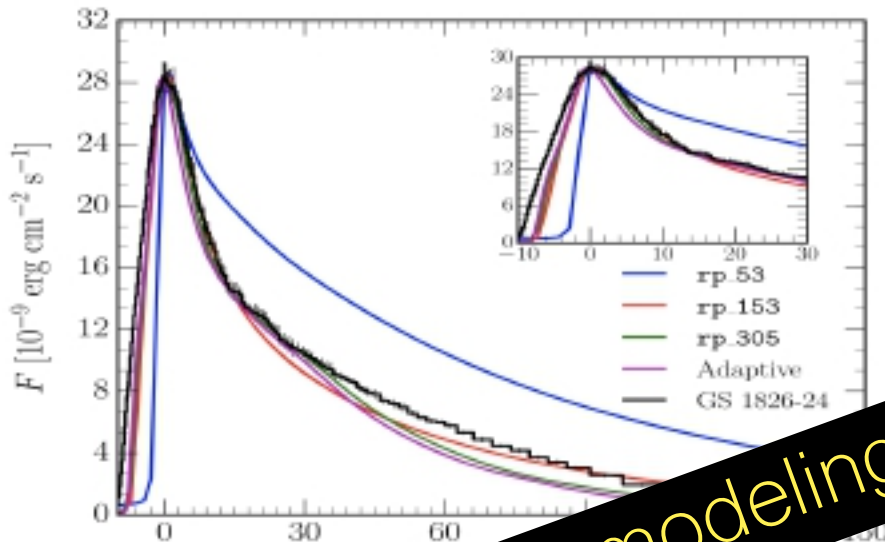


Figure: A typical X-ray burst over the GS 1826-24 (black) against the theoretical models employing **MESA**

- Observationally the accretion rate is  $\dot{M} < 0.3 \dot{M}_{\text{Edd}}$  (at  $\dot{M}_{\text{Edd}} \approx 10^{-8} M_{\odot} \text{ yr}^{-1}$ )

Accretion starts at  $\sim 10^{5.75} \text{ g cm}^{-3} \equiv$  **ENVELOPE**

- From H into Fe and beyond:  
*rp-process*

**Time-dependent codes such as MESA\* are required!**

\*Modules for Experiments in Stellar Astrophysics

# TRANSIENT SYSTEMS: BURN AND RELAX

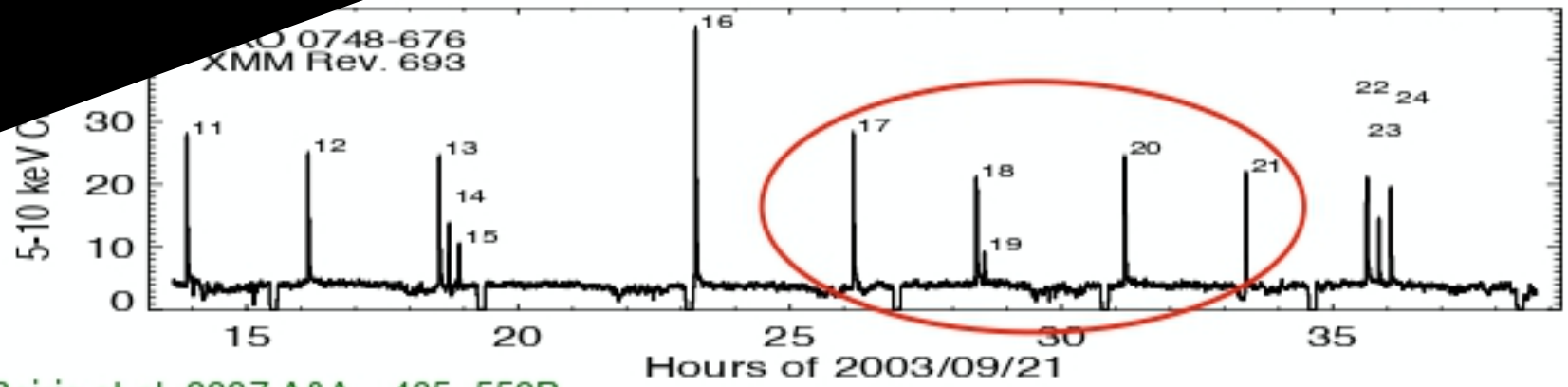
MAXI J0556-332: Acreción transitoria



Page et al 2022, ApJ 933, 216

How does continuous rp-process influence the neutron star's temperature profile?

EXO 0748-676: Acreción y X-ray bursts

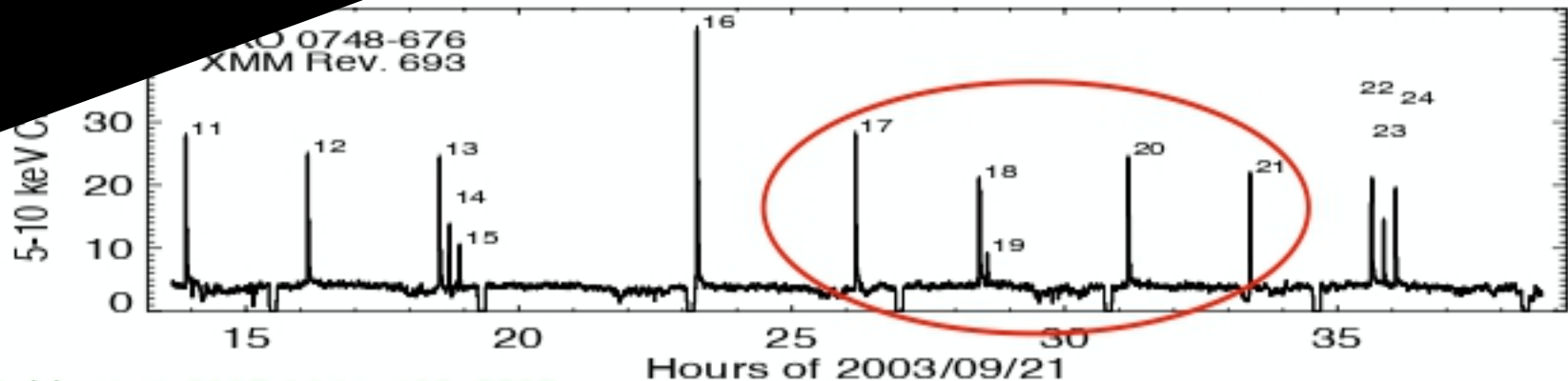


Boirin et al, 2007 A&A...465..559B

# TRANSIENT SYSTEMS: BURN AND RELAX

**MAIN GOAL:** To develop an approximating scheme to model transient (& possibly continuous) accreting sources

How

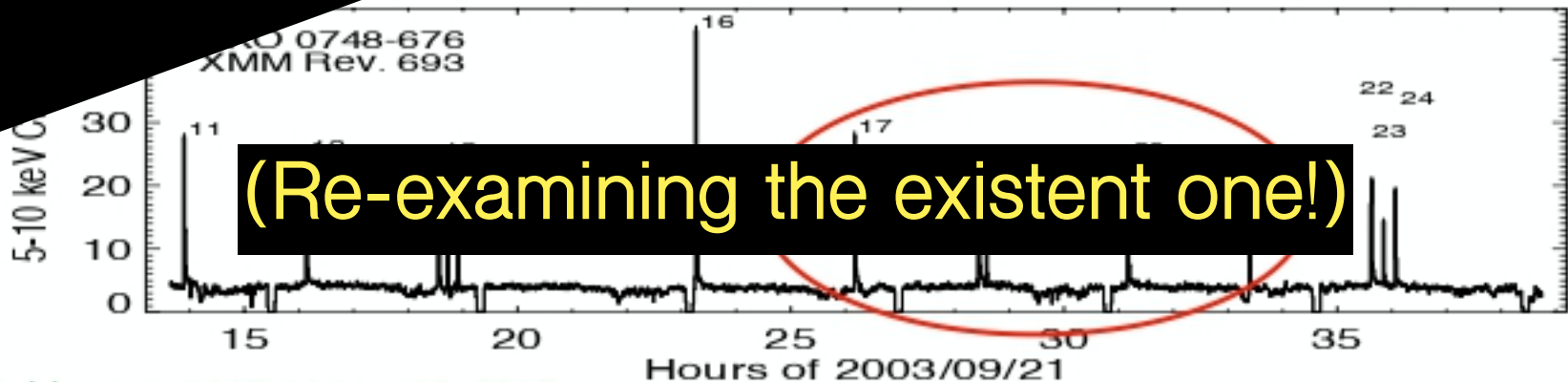


Boirin et al, 2007 A&A...465..559B

# TRANSIENT SYSTEMS: BURN AND RELAX

**MAIN GOAL:** To develop an approximating scheme to model transient (& possibly continuous) accreting sources

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Boirin et al, 2007 A&A...465..559B

CHAPTER 1

# ENVELOPES WITH ACCRETION: STATIONARY STATES

(MOVING PICTURES)

# Current: The $T_b(T_{\text{eff}})$ scheme



$T_{\text{eff}}$

## ENVELOPE:

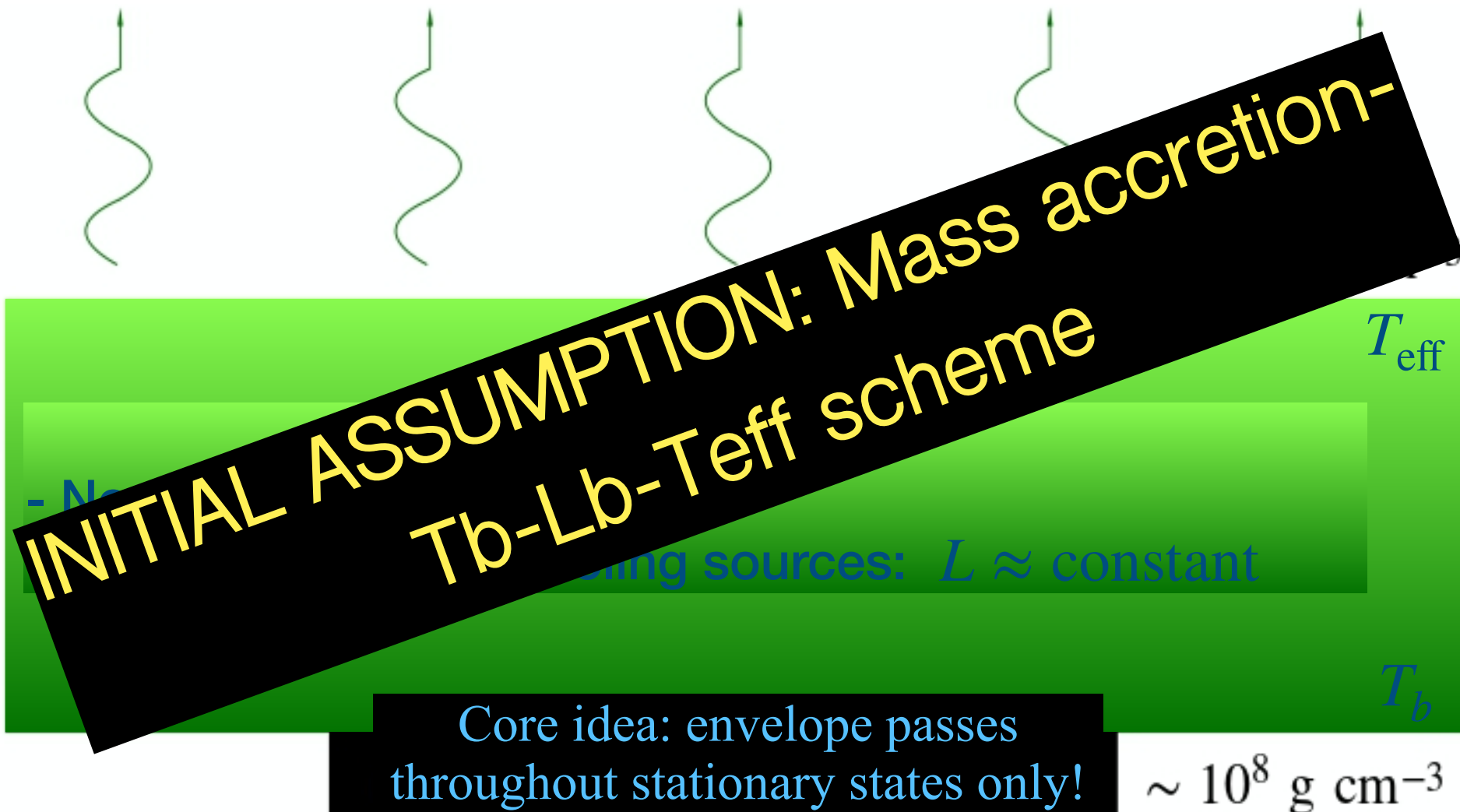
- No accretion
- No further heating/cooling sources:  $L \approx \text{constant}$

$T_b$

Core idea: envelope passes  
throughout stationary states only!

~  $10^8 \text{ g cm}^{-3}$

# Current: The $T_b(T_{\text{eff}})$ scheme



**INITIAL ASSUMPTION: Mass accretion-  
 $T_b$ - $L_b$ - $T_{\text{eff}}$  scheme**

Emitting sources:  $L \approx \text{constant}$

Core idea: envelope passes throughout stationary states only!

$\sim 10^8 \text{ g cm}^{-3}$

$T_{\text{eff}}$

$T_b$

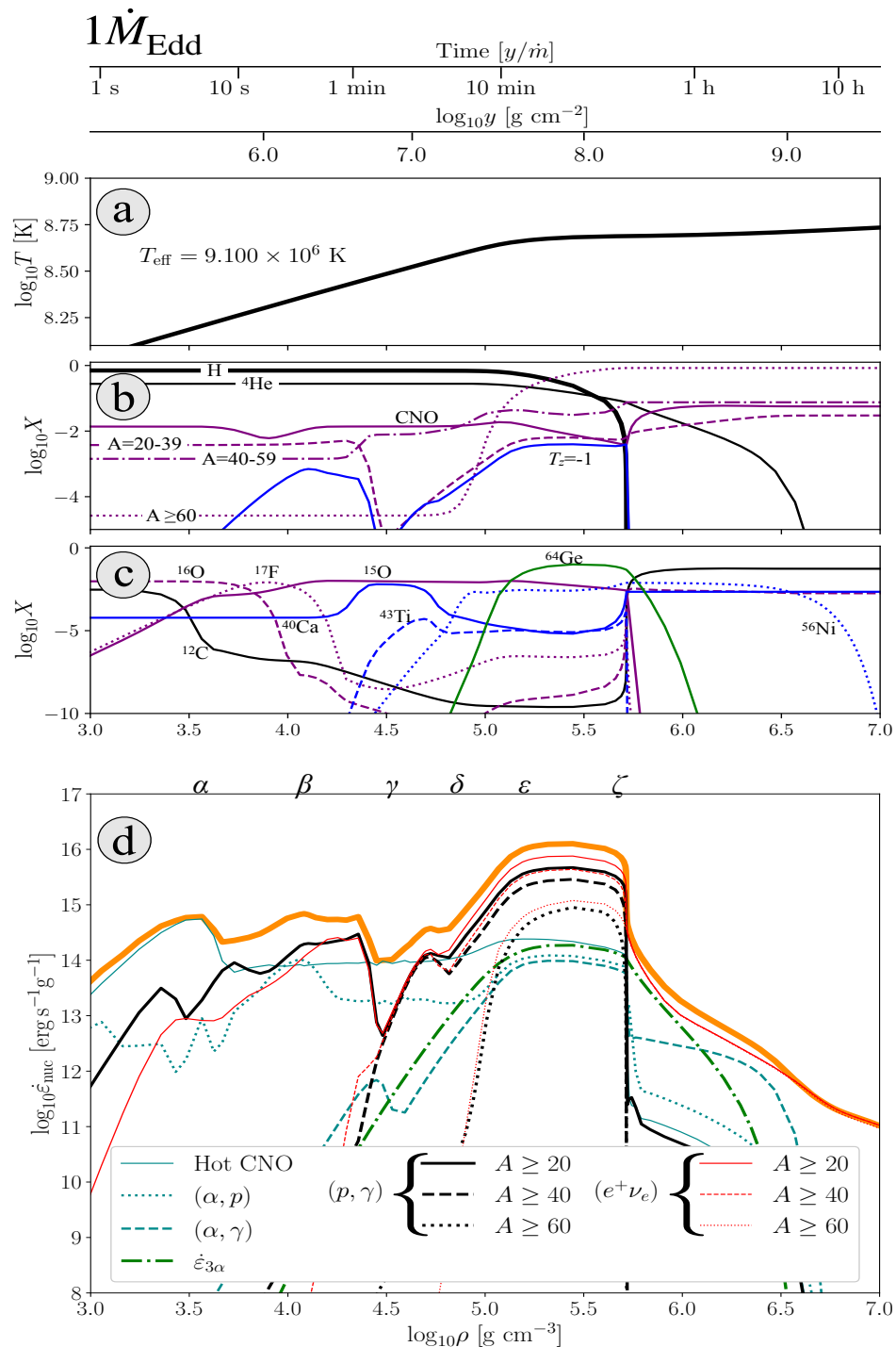
# ANALYSIS OF STATIONARY STATES

EXAMINE TIME-INDEPENDENT ENVELOPES AT HIGH ACCRETION RATES

CONSTRUCTION OF A NUMERICAL CODE WITH 380 SPECIES (WITH ROOM FOR MORE/ LESS NUCLIDES)

OWN'S CODE OUTPUT AS INITIAL CONDITION FOR MESA

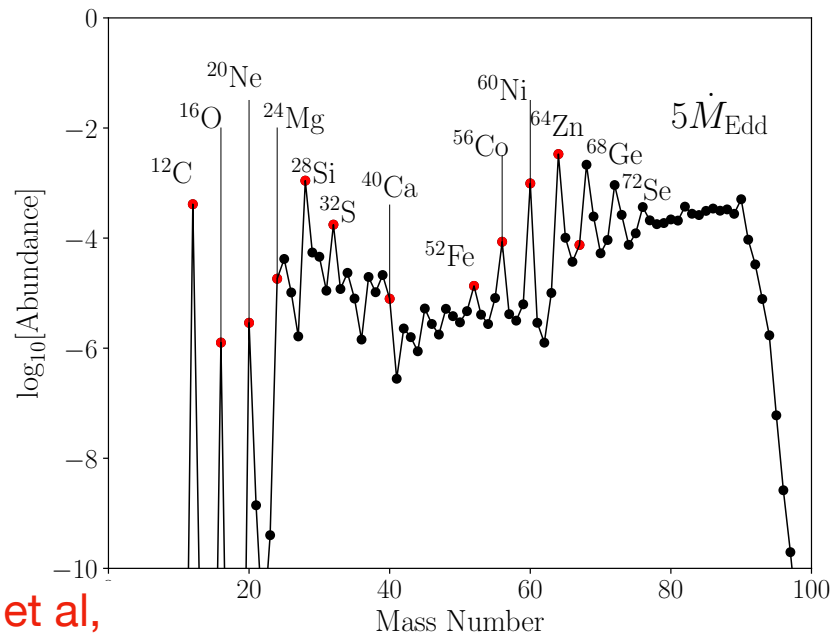
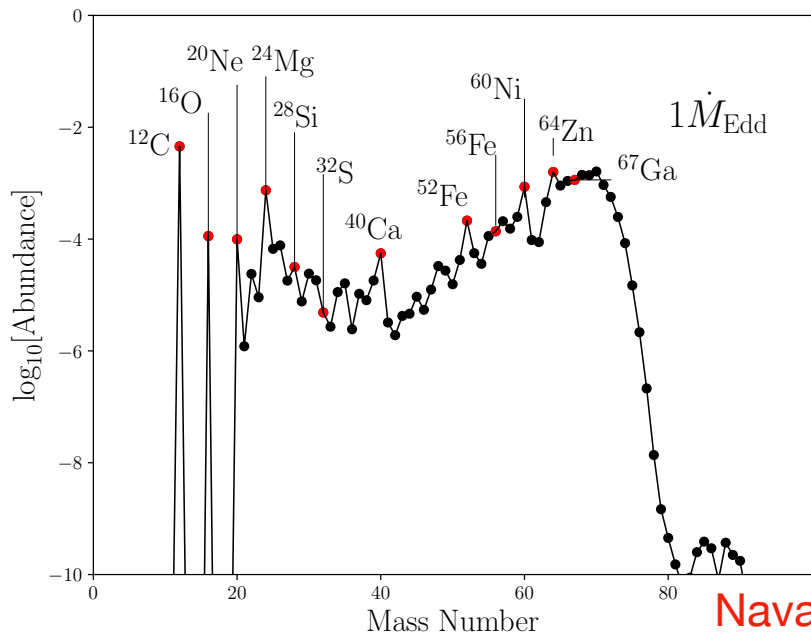
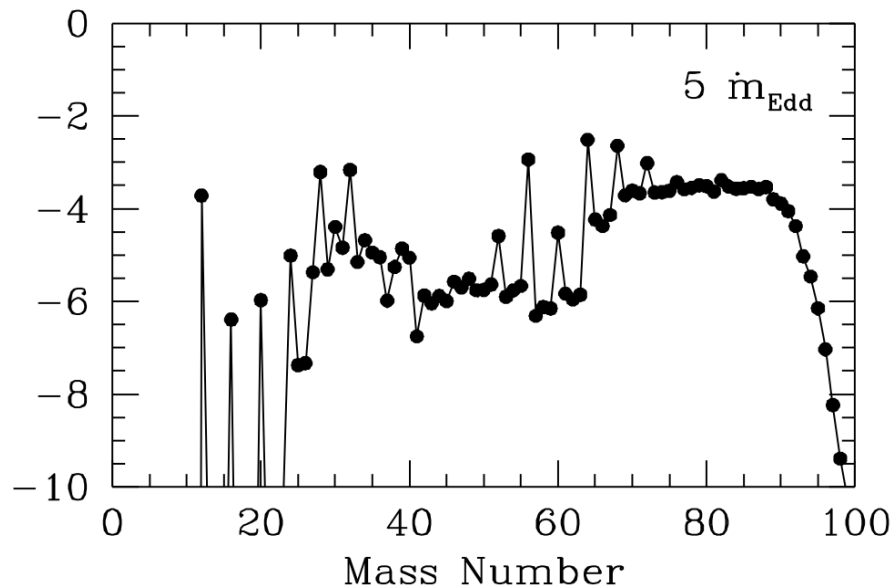
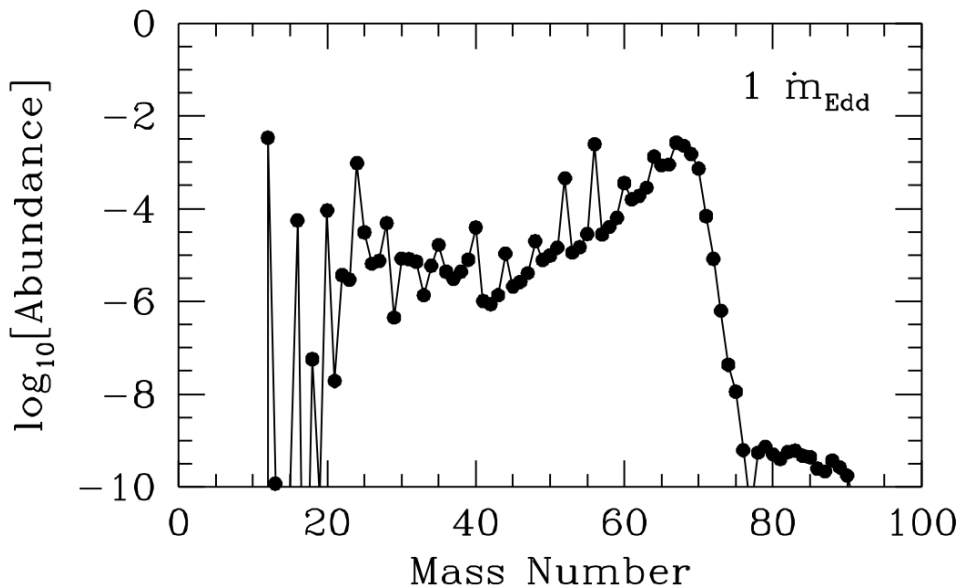
Nava-Callejas et al, 2024, arXiv:2403.13994 (RASTI, in press, <https://doi.org/10.1093/rasti/rzae055>)





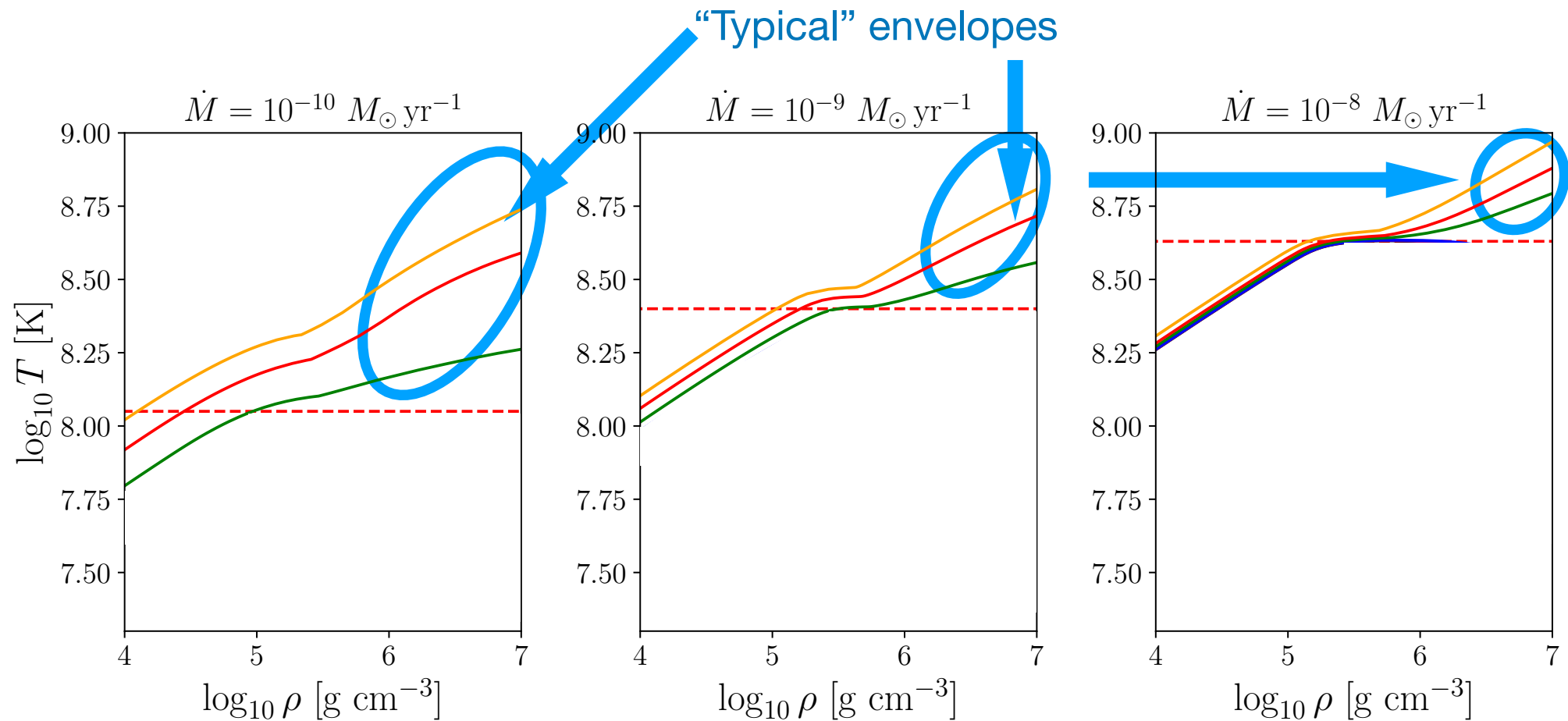
# COMPARISON WITH FORMER WORKS

Schatz et al, 1999

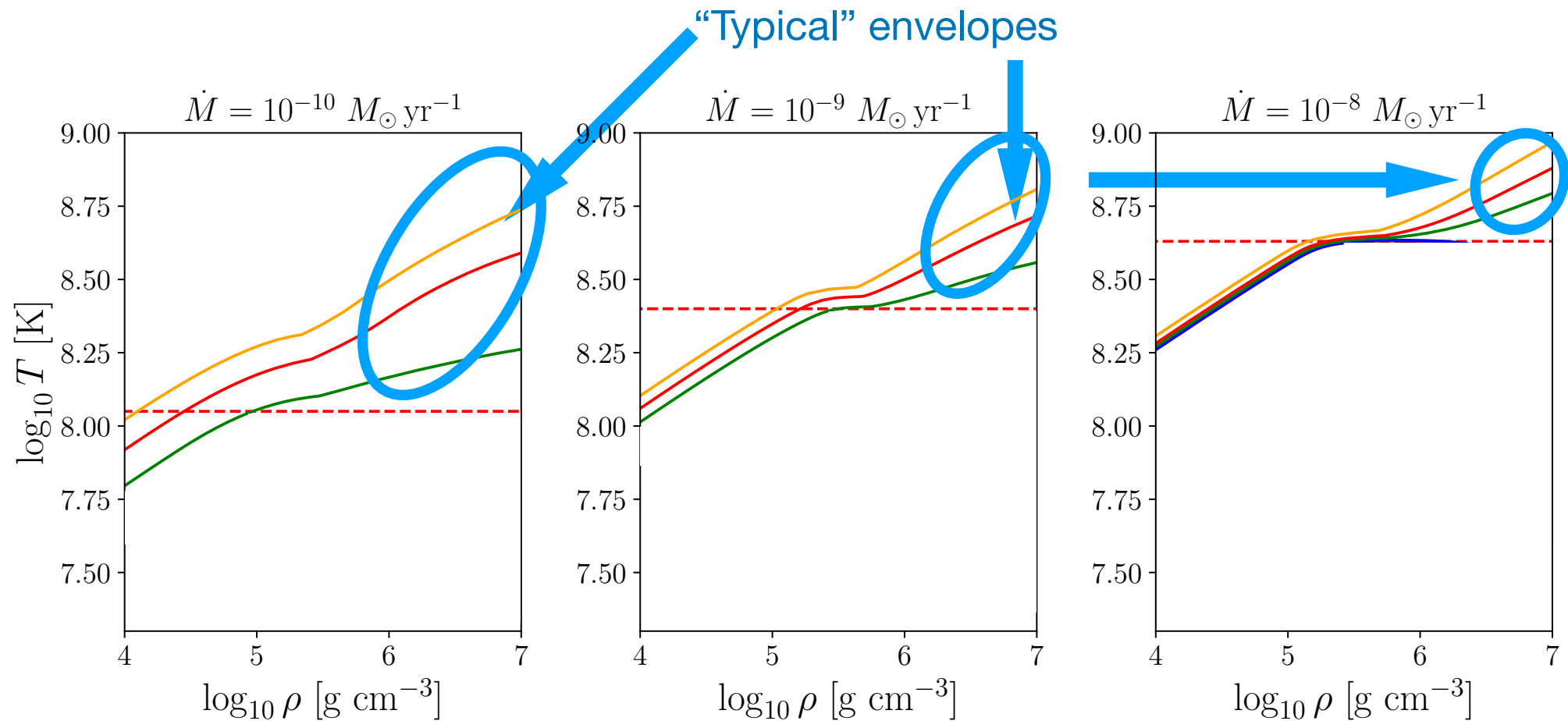


Nava-Callejas et al,  
2024

# STATIONARY STATES “FAMILIES”



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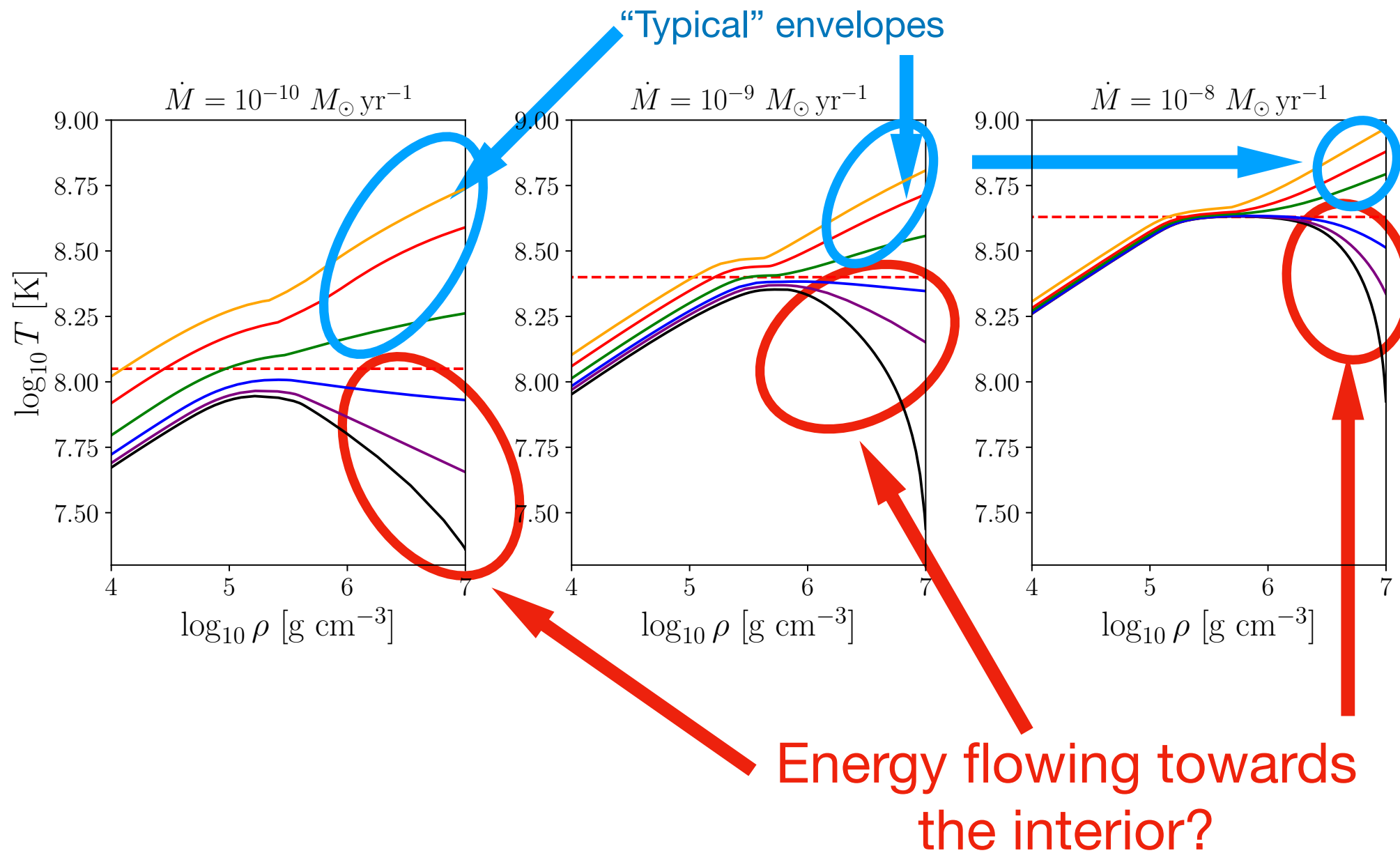


$T_{\text{eff}} \approx$  same as  $\dot{M} \rightarrow \dot{M}_{\text{Edd}}$ .

$\dot{M} - T_{\text{eff}} - L_b - T_b$  not very viable.

Drastic variation of  $L_b$  &  $T_b$

# STATIONARY STATES “FAMILIES”



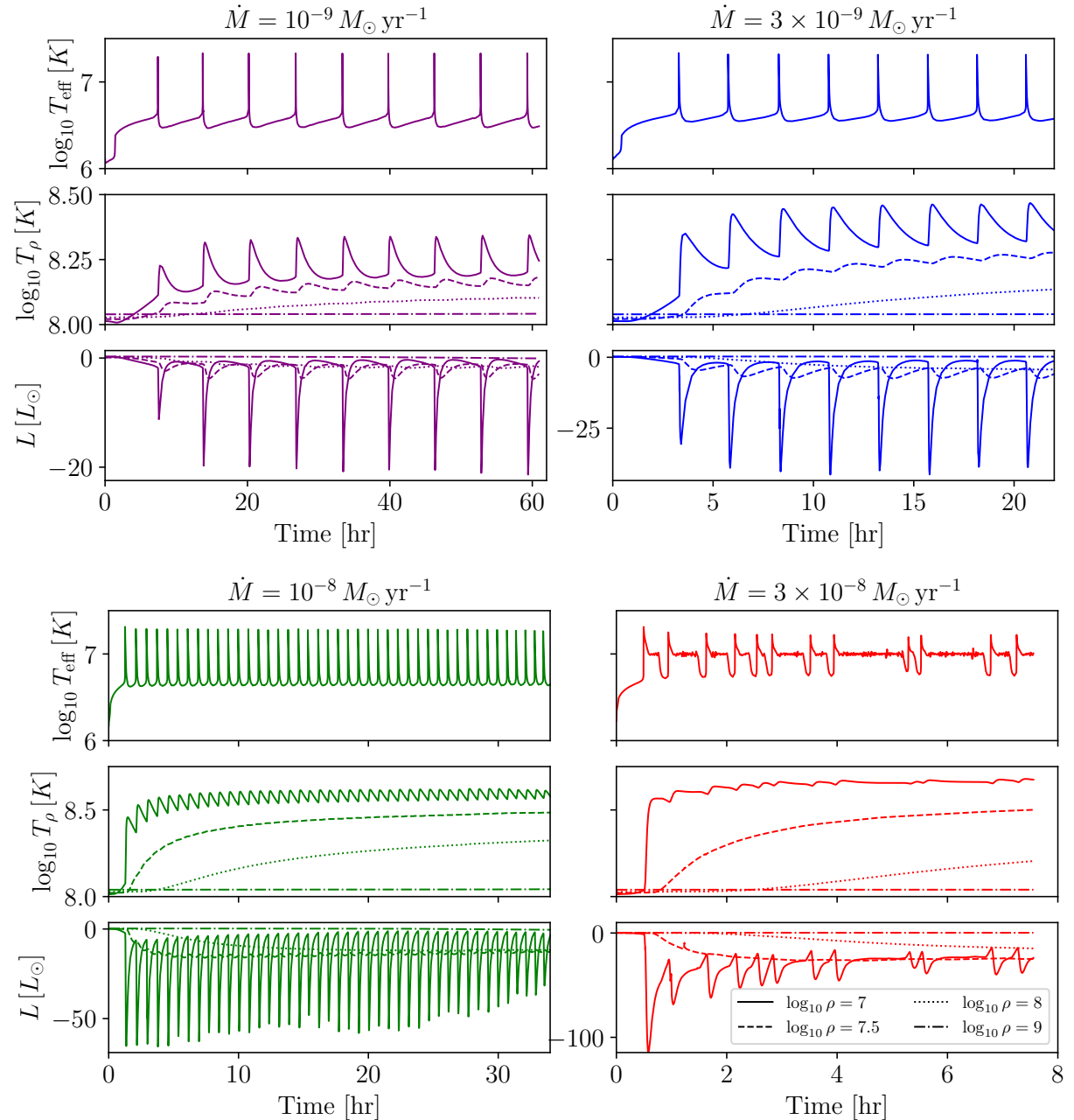
CHAPTER 2

# THERMAL EVOLUTION: A FIRST LOOK

(UNDER THE IRON SEA)

# ENERGY TOWARDS THE INTERIOR?

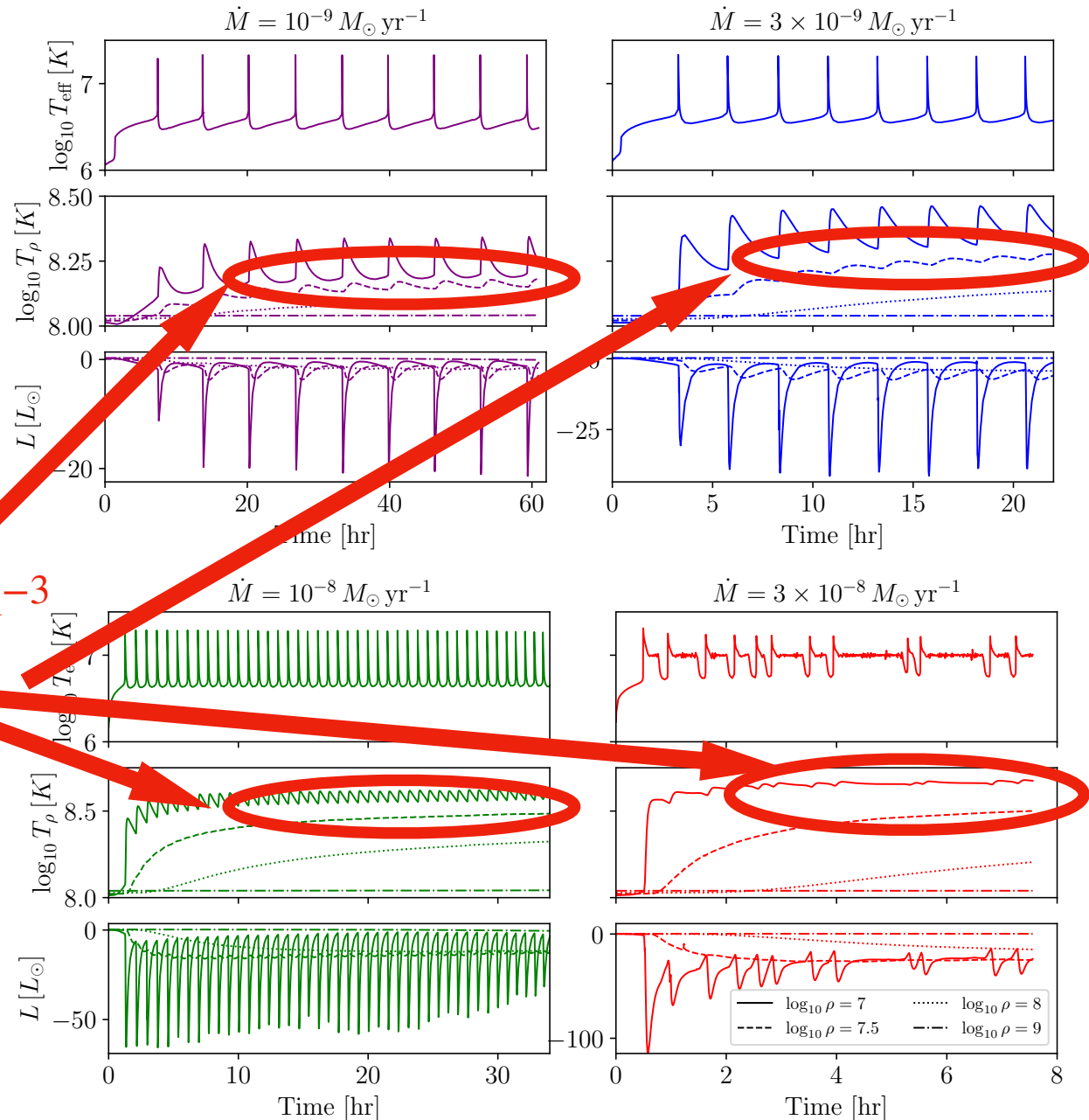
MESA: Energy  
flowing towards  
the interior is  
viable



# ENERGY TOWARDS THE INTERIOR?

MESA: Energy  
flowing towards  
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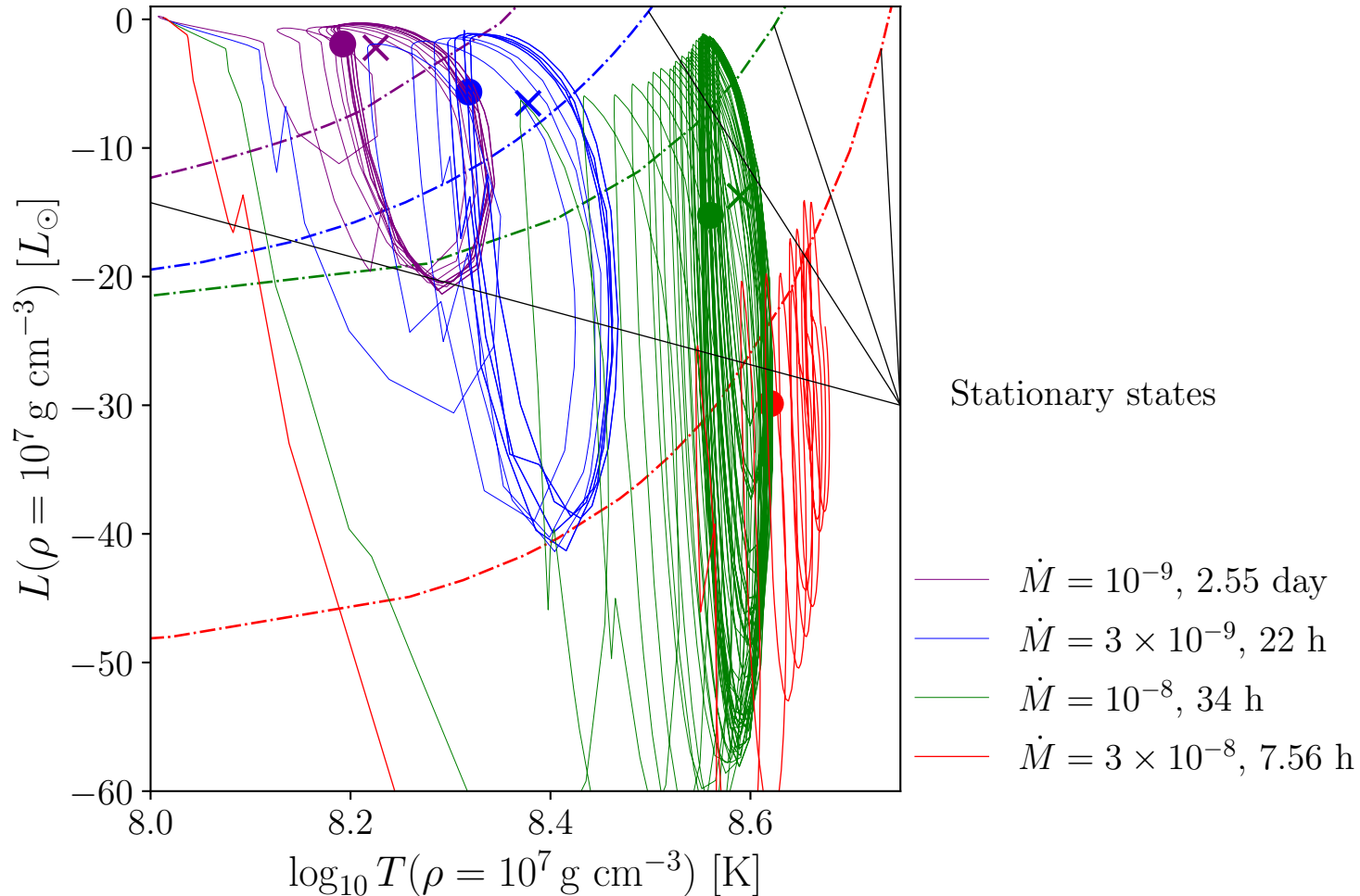
Are these  $\rho \sim 10^7 \text{ g cm}^{-3}$   
regions reaching a  
~stationary state?



# ENERGY TOWARDS THE INTERIOR?

- No convection/  
thermohaline

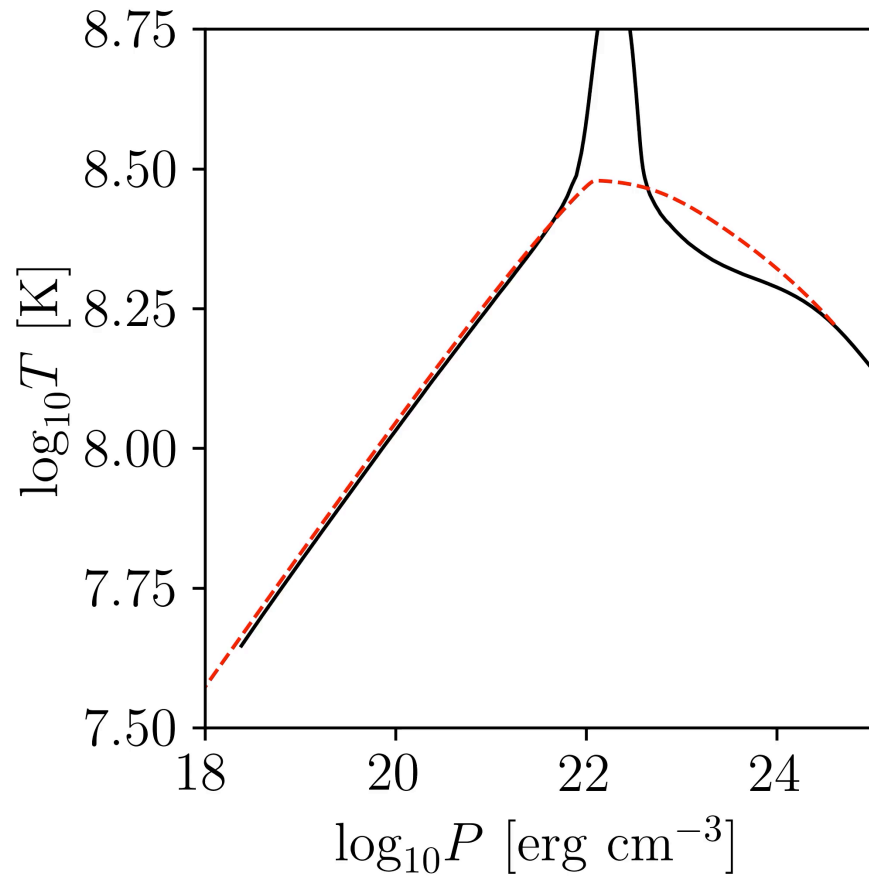
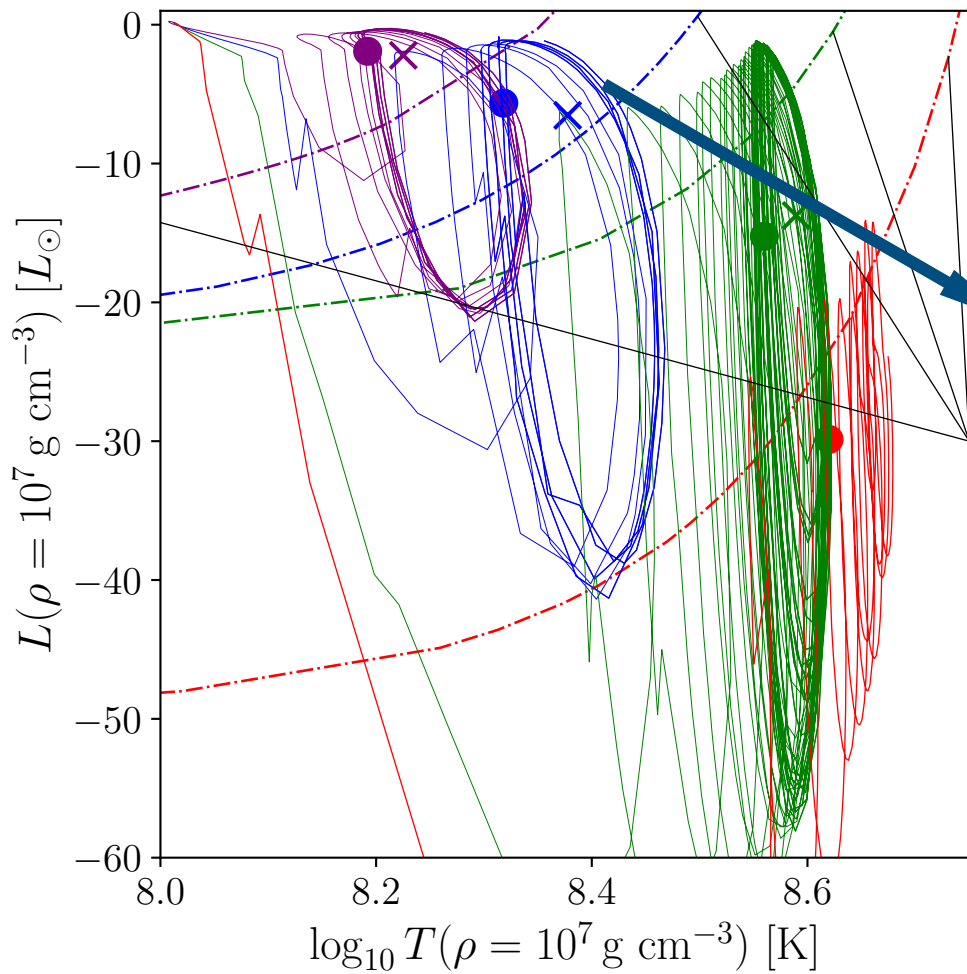
- No GR  
corrections (for fair  
comparison)



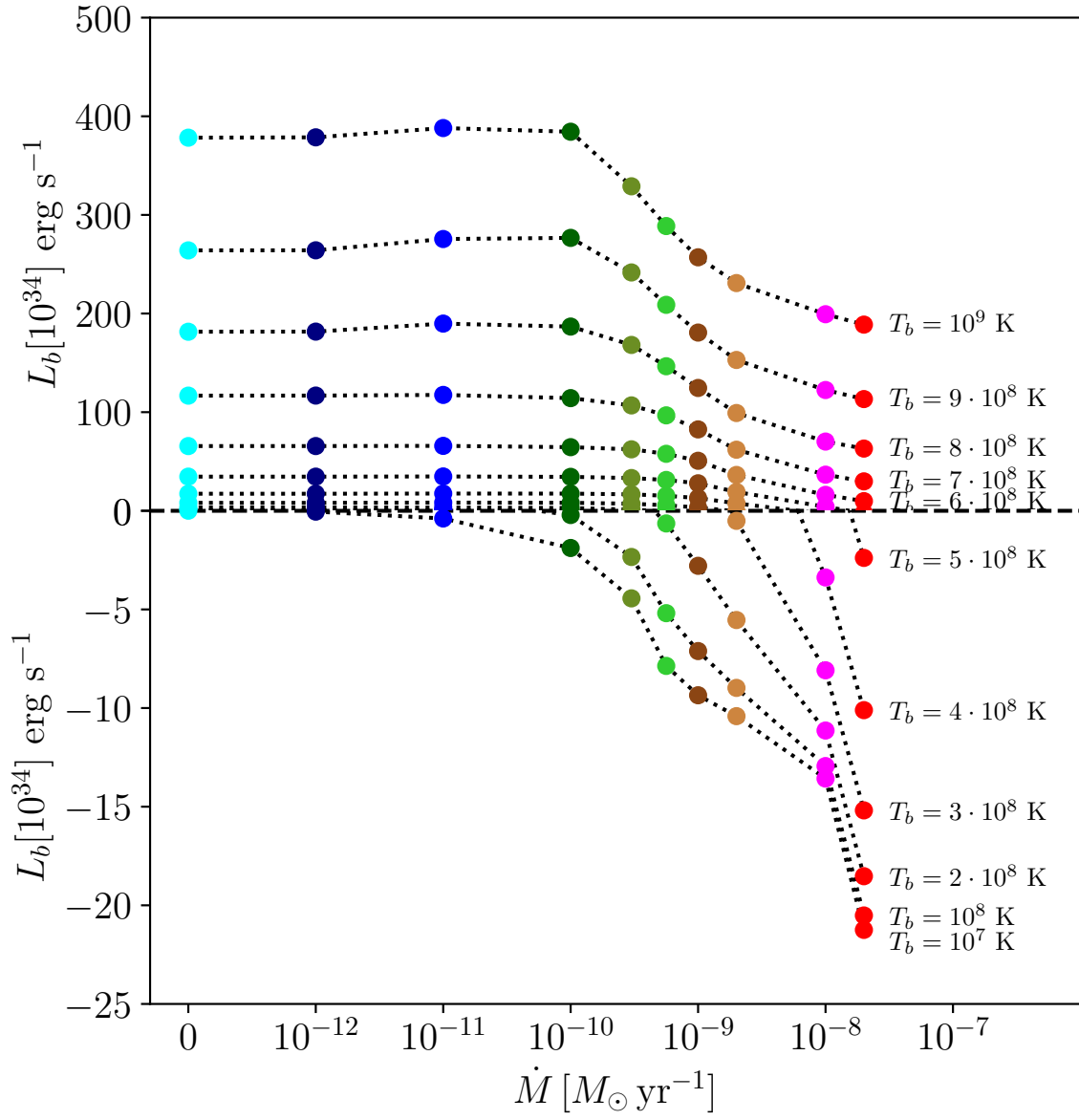
$\dot{M} - L_b - T_b$  seems viable.



$$\dot{M} = 3 \times 10^{-9} M_{\odot} \text{ yr}^{-1}$$



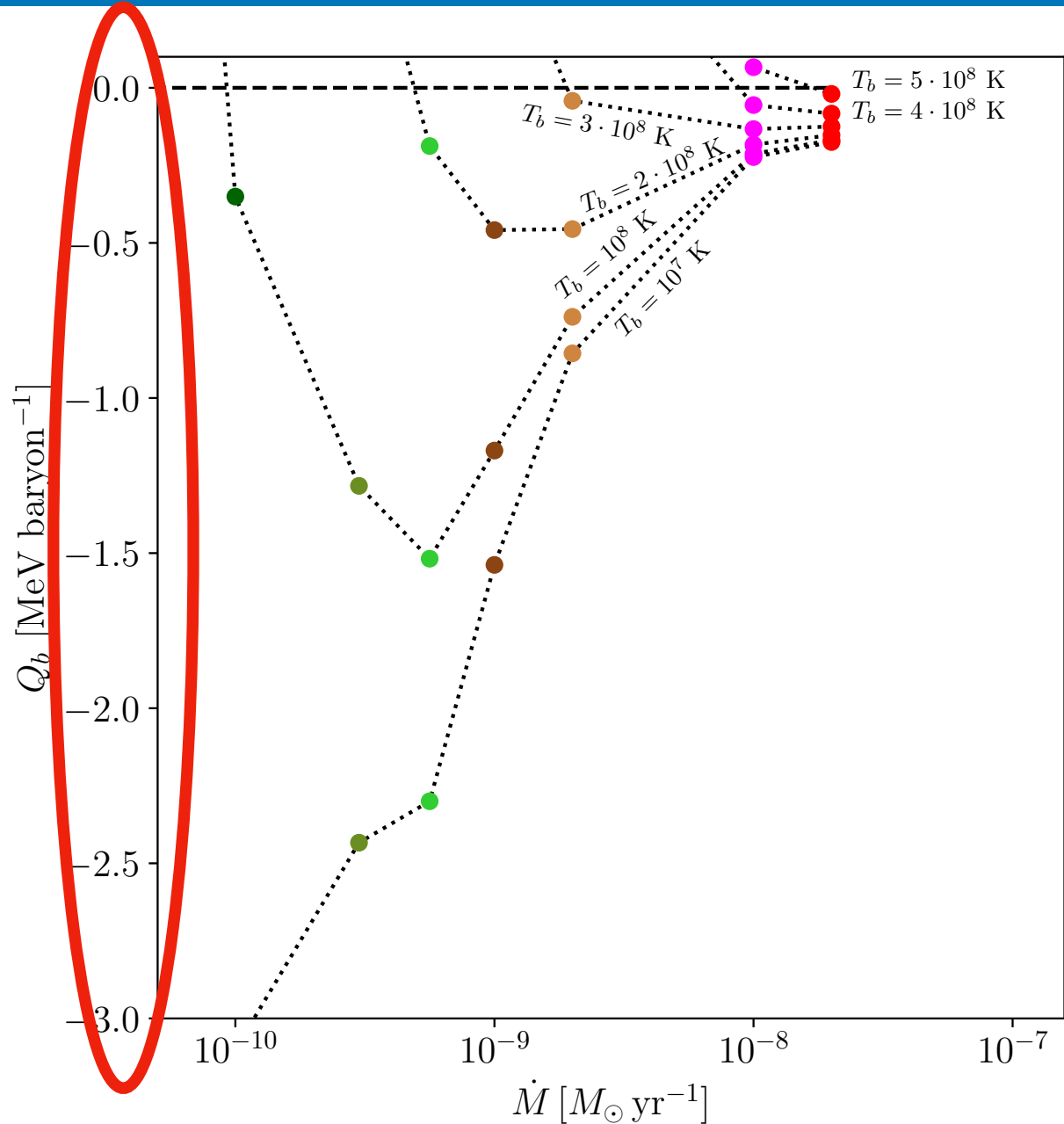
# BOUNDARY CONDITIONS FOR NSCOOL



# BOUNDARY CONDITIONS FOR NSCOOL

$$L_b \rightarrow Q_b$$

~Typical  
shallow  
heating  
values



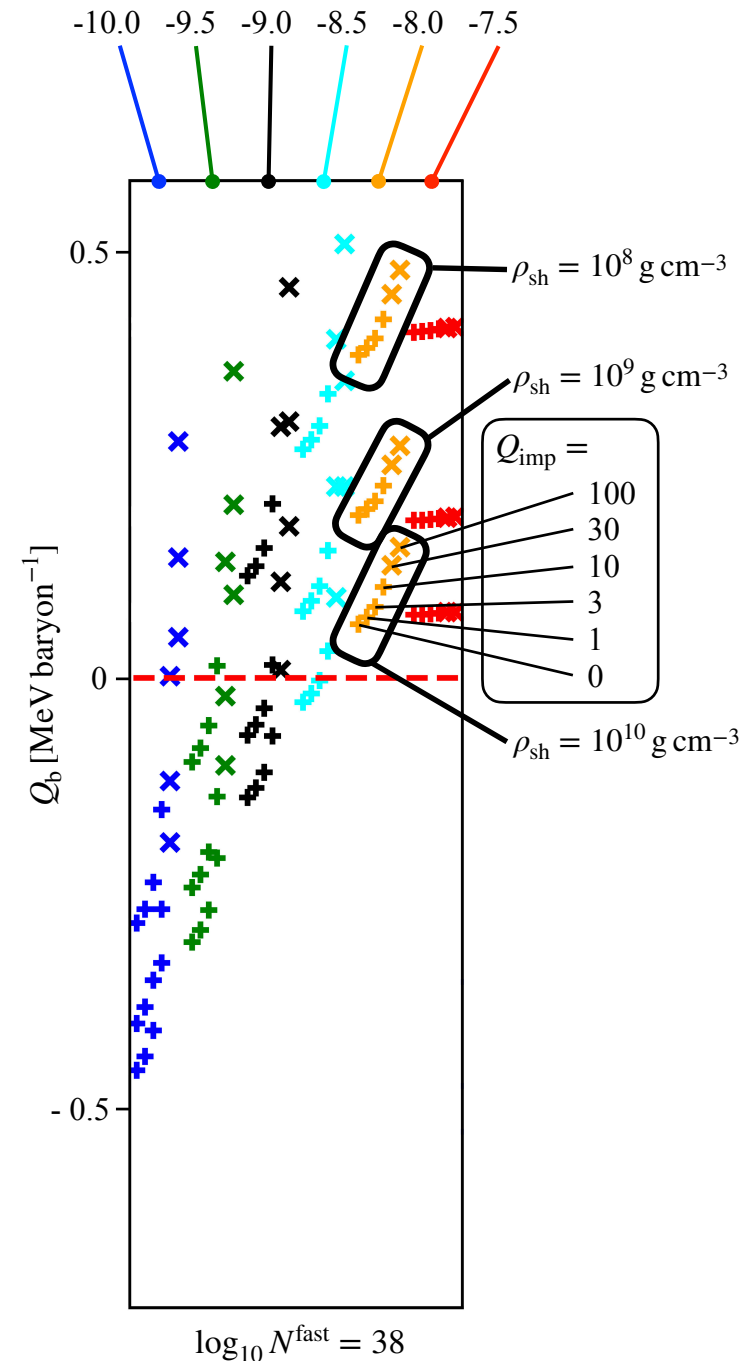
# ACTUAL RUNS WITH NSCOOL

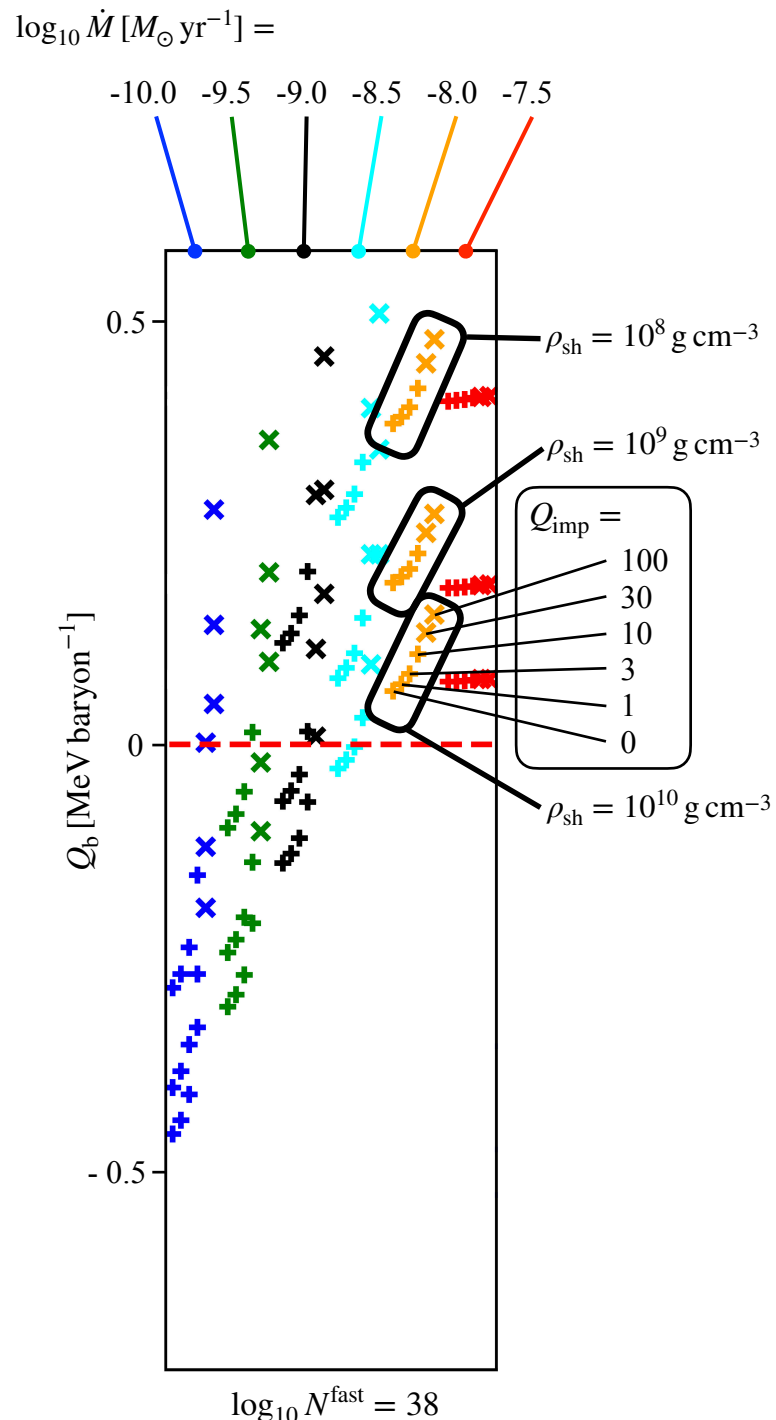
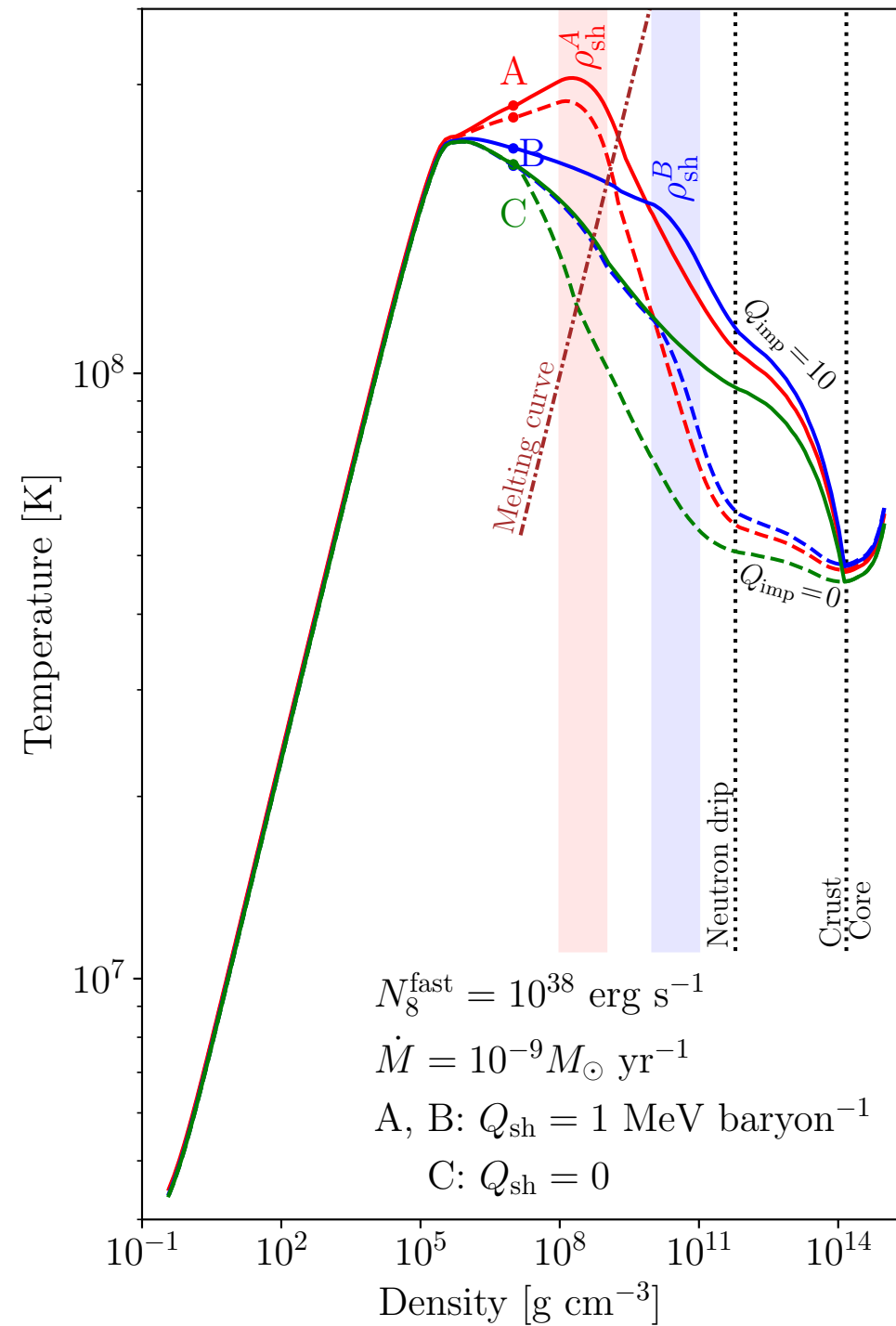
- Continuous & constant mass accretion for  $\sim 10^5$  years
- Different values of impurities in the crust:  $Q_{\text{imp}}$
- Additional *shallow heating* amount at different locations:  $Q_{\text{sh}}$  @  $\rho_{\text{sh}}$
- Fiducial neutrino cooling mechanism at core:  $L_\nu = N_{s/f} (T/10^8 \text{ K})^{p_{s/f}}$

$$N_s \in [10^{31}, 10^{35}] \text{ erg s}^{-1} \text{ \& } p_s = 8 \text{ (Slow)}$$

$$N_f \in (10^{35}, 10^{43}) \text{ erg s}^{-1} \text{ \& } p_f = 6 \text{ (Fast)}$$

$$\log_{10} \dot{M} [M_\odot \text{ yr}^{-1}] =$$





# EPILOGUE

(NATURALLY)

# ONGOING AND FUTURE WORK

- Energy might flow **from the exterior to the interior** of the star
- Stationary states:  $\dot{M} - T_b - L_b \sim$  good approximation
- Continuous accretion: energy keeps flowing **inwards**
- **For tomorrow:** Dany will provide further details on the simulations
- **Work in progress/future:** study transient sources & include additional effects (Core EOS, superfluidity....)