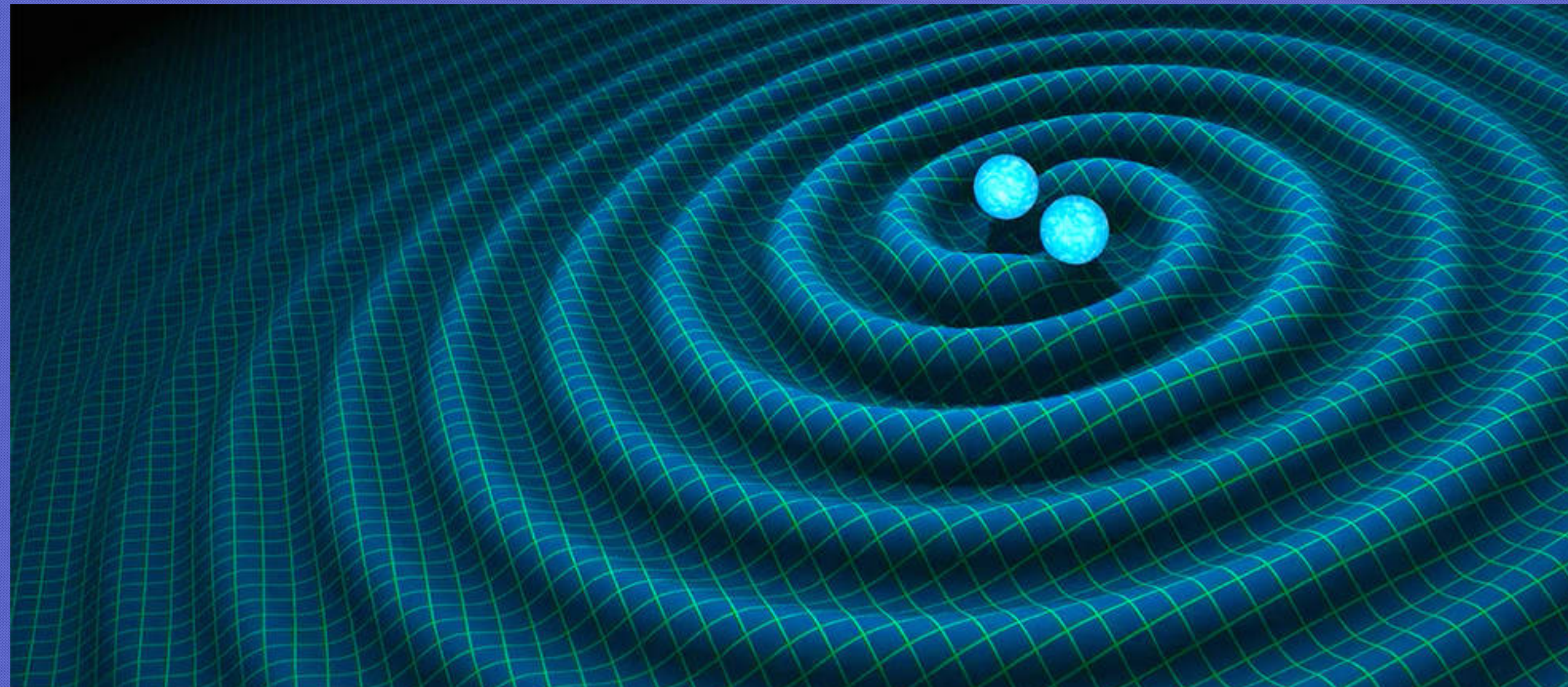


Simultaneously Constraining the Neutron Star Equation of State and Mass Distribution through Multimessenger Observations and Nuclear Benchmarks

Based on arXiv: 2408.15192 by Bhaskar Biswas & Stephan Rosswog



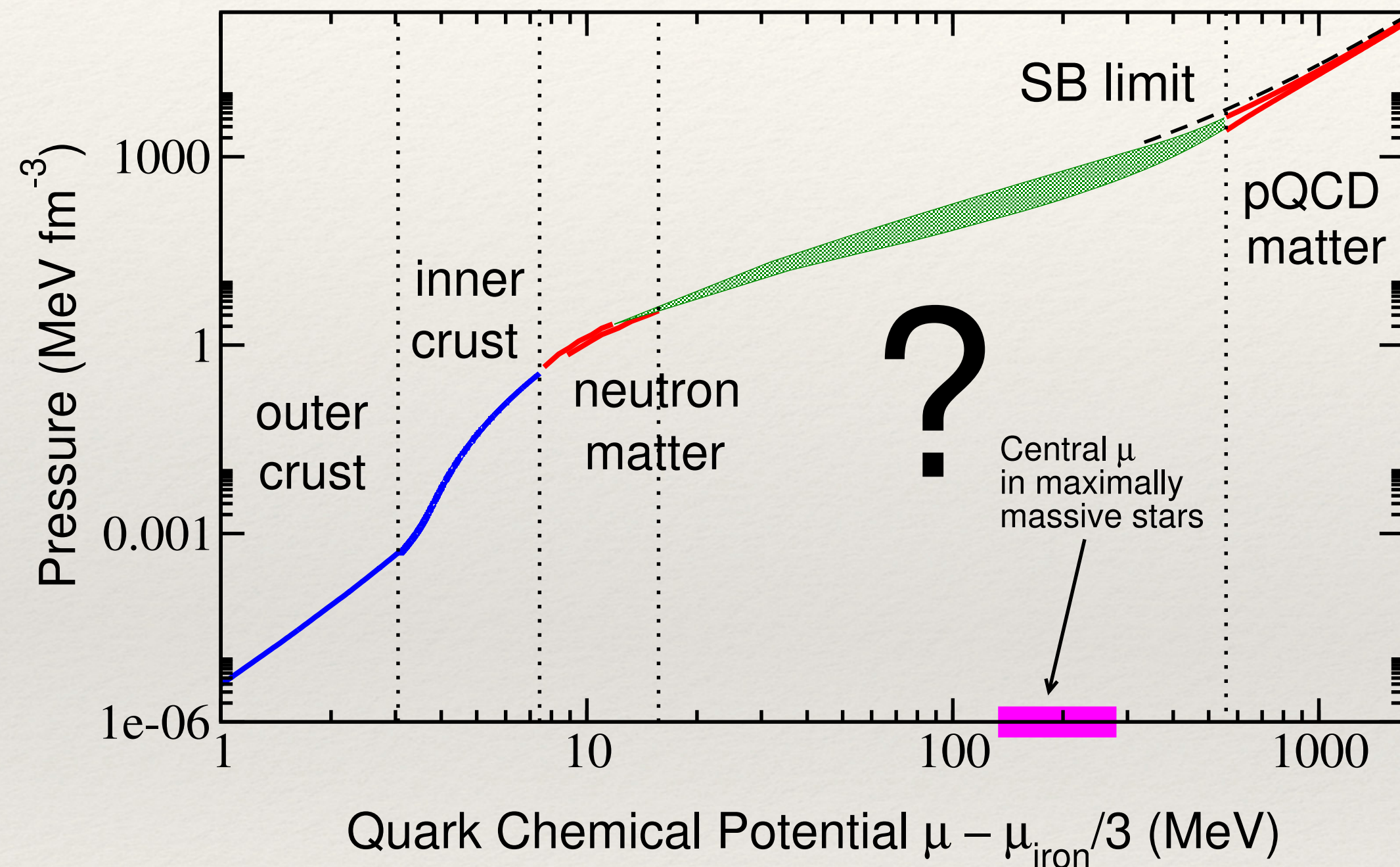
Bhaskar Biswas | Hamburg observatory

Institute for nuclear theory, Seattle

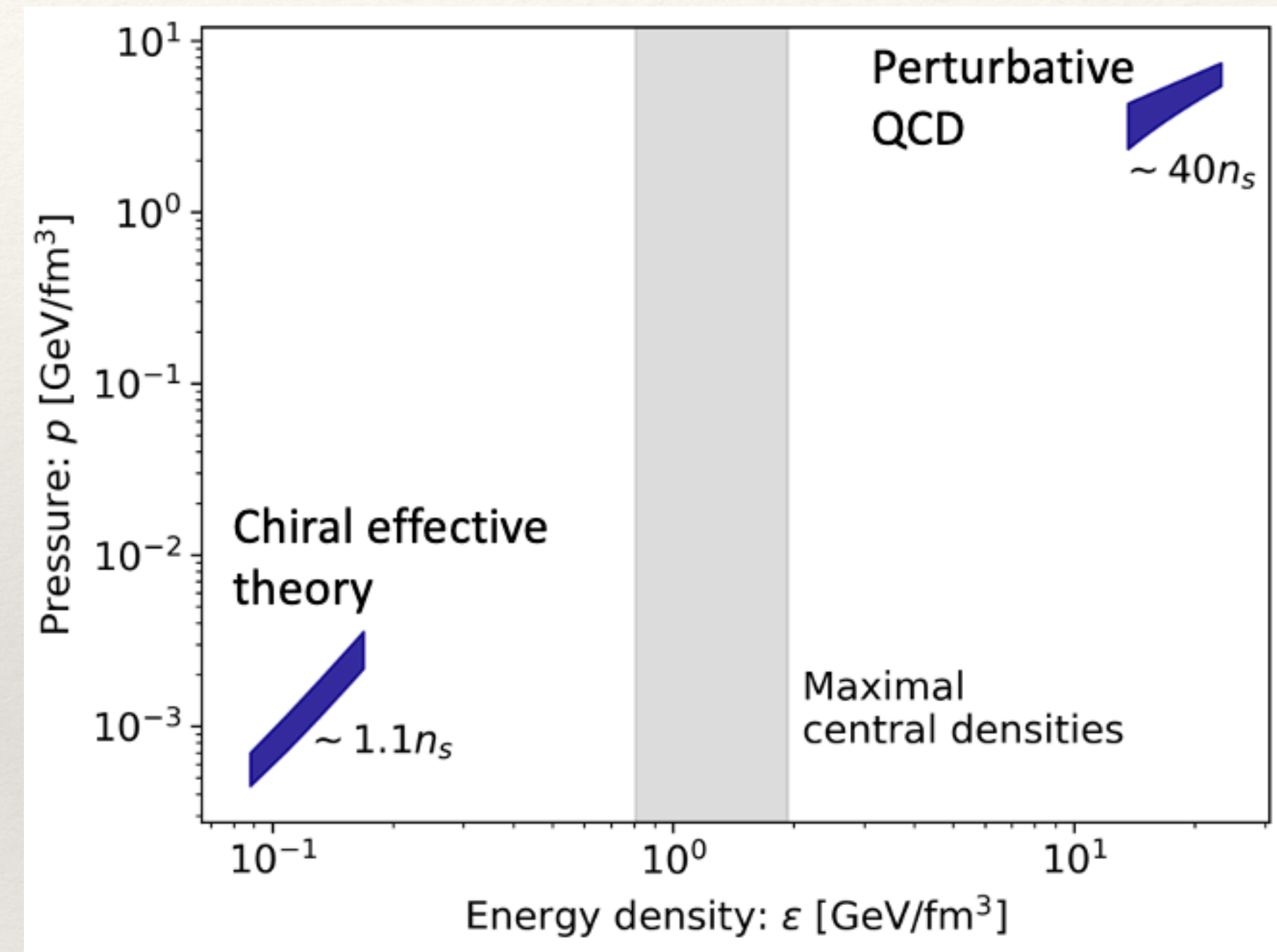
August 30, 2024

What we know about the EOS of neutron stars?

Kurkela, Fraga, Beilich, Vourinen, 2014



A. Kurkela, arXiv: 2211.11414



Low density EOS is well known; Challenges begin near saturation density

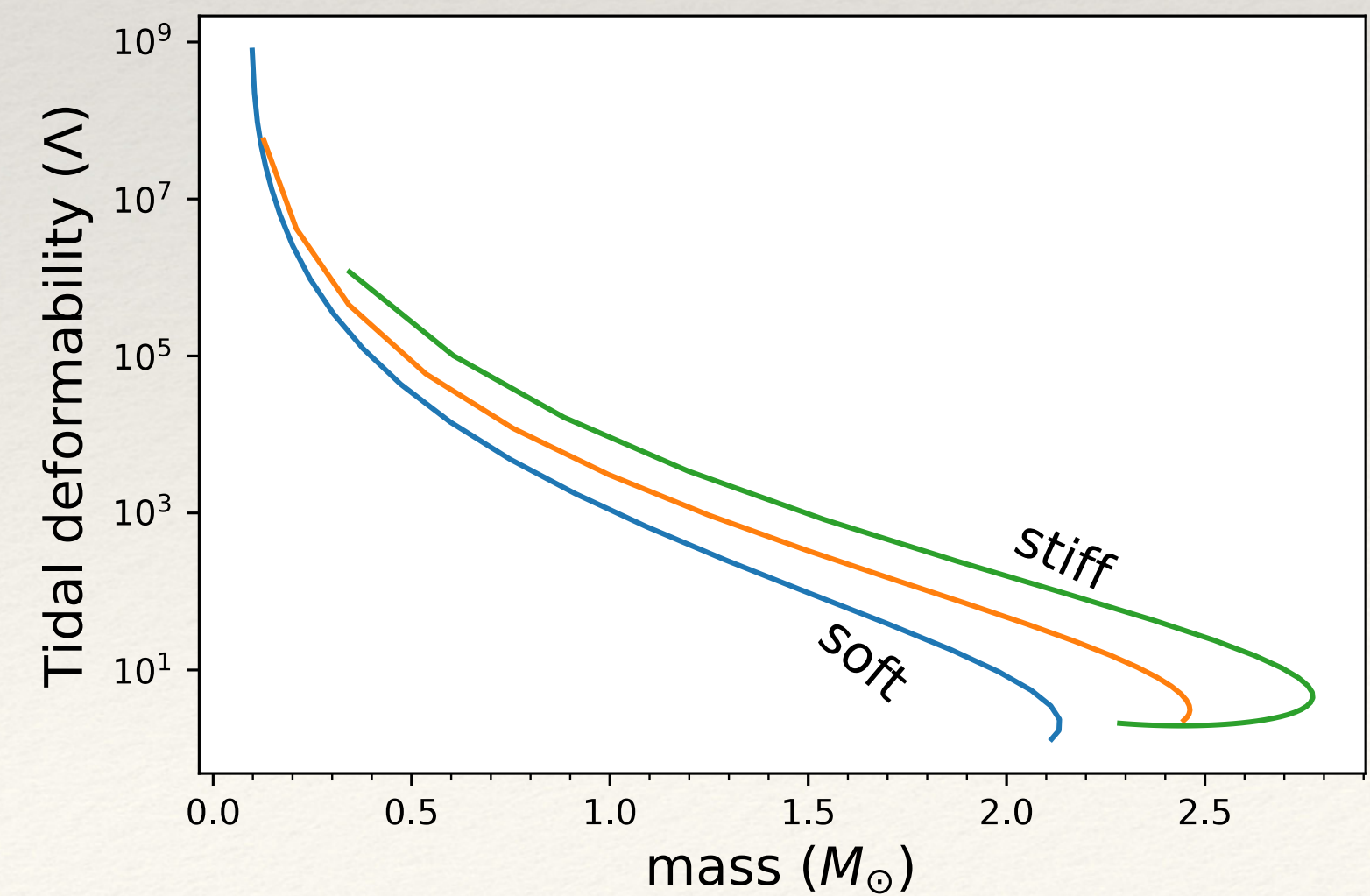
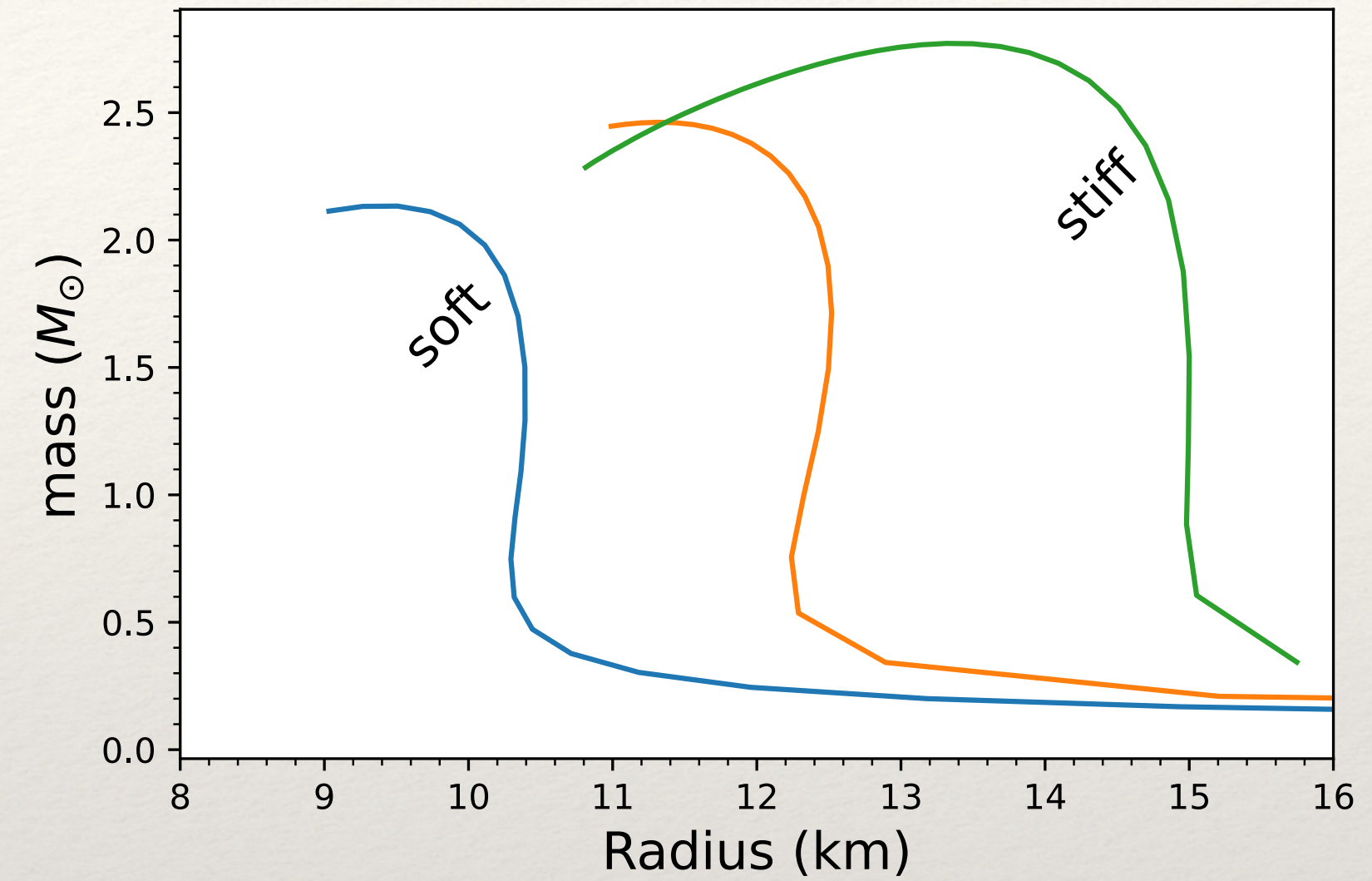
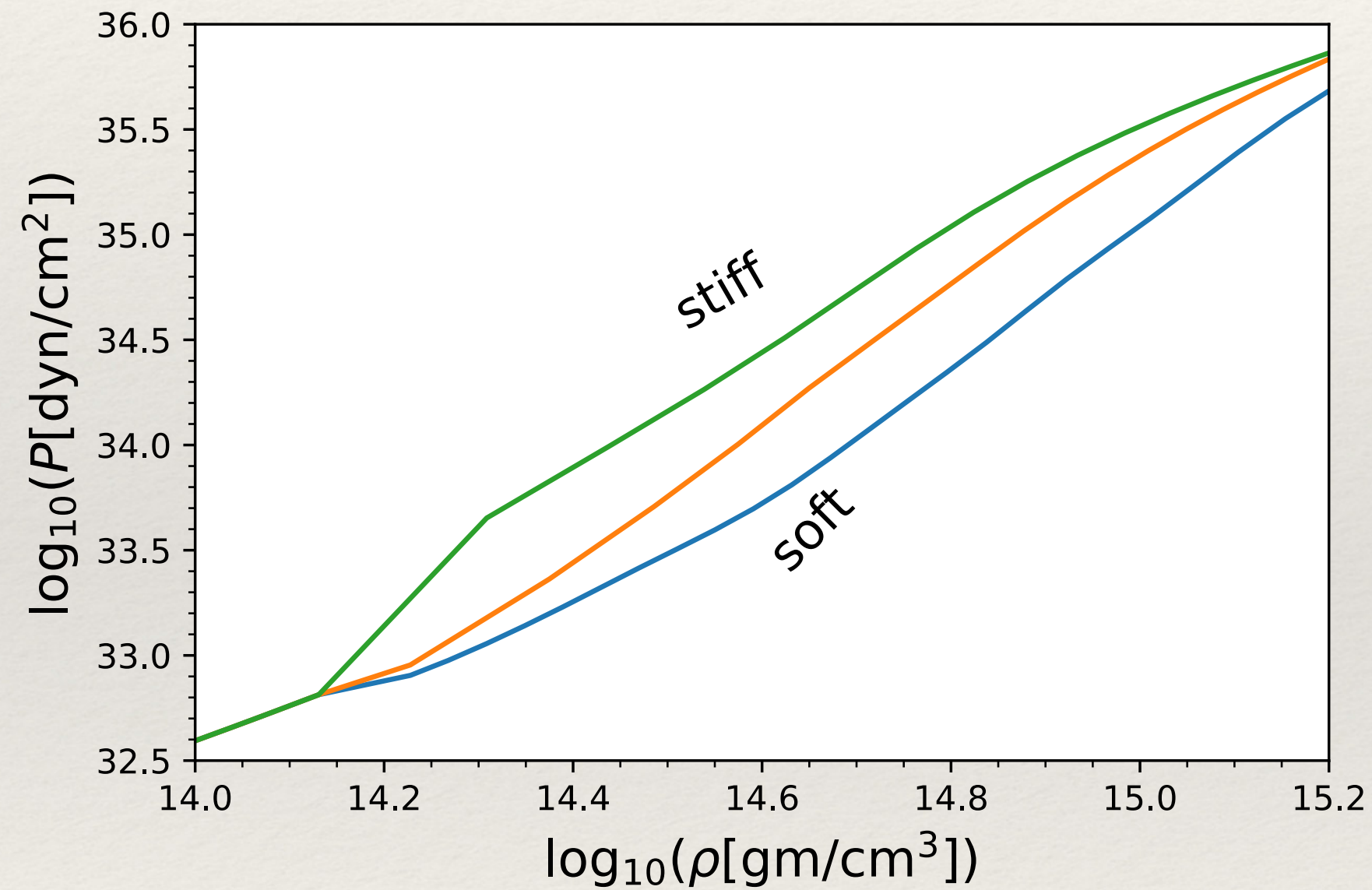
Tews et al., PRL, 110 (2013)
 Hebeler et al., ApJ 773 (2013)
 Drischler et al., PRL 125 (2020)

High density regime: pQCD, relative uncertainty $\pm 24\%$ at $\mu_B = 2.6$ GeV, $n \approx 40n_s$

Kurkela et al., PRD 81 (2009)
 Gorda et al., PRL 121 (2018)

EOS & observables

EOS, $P = P(\rho)$



- ❖ Radio observables — M
- ❖ X-ray observables — M, R
- ❖ GW observables — M, Λ

Mass distribution of neutron stars in binary pulsar systems

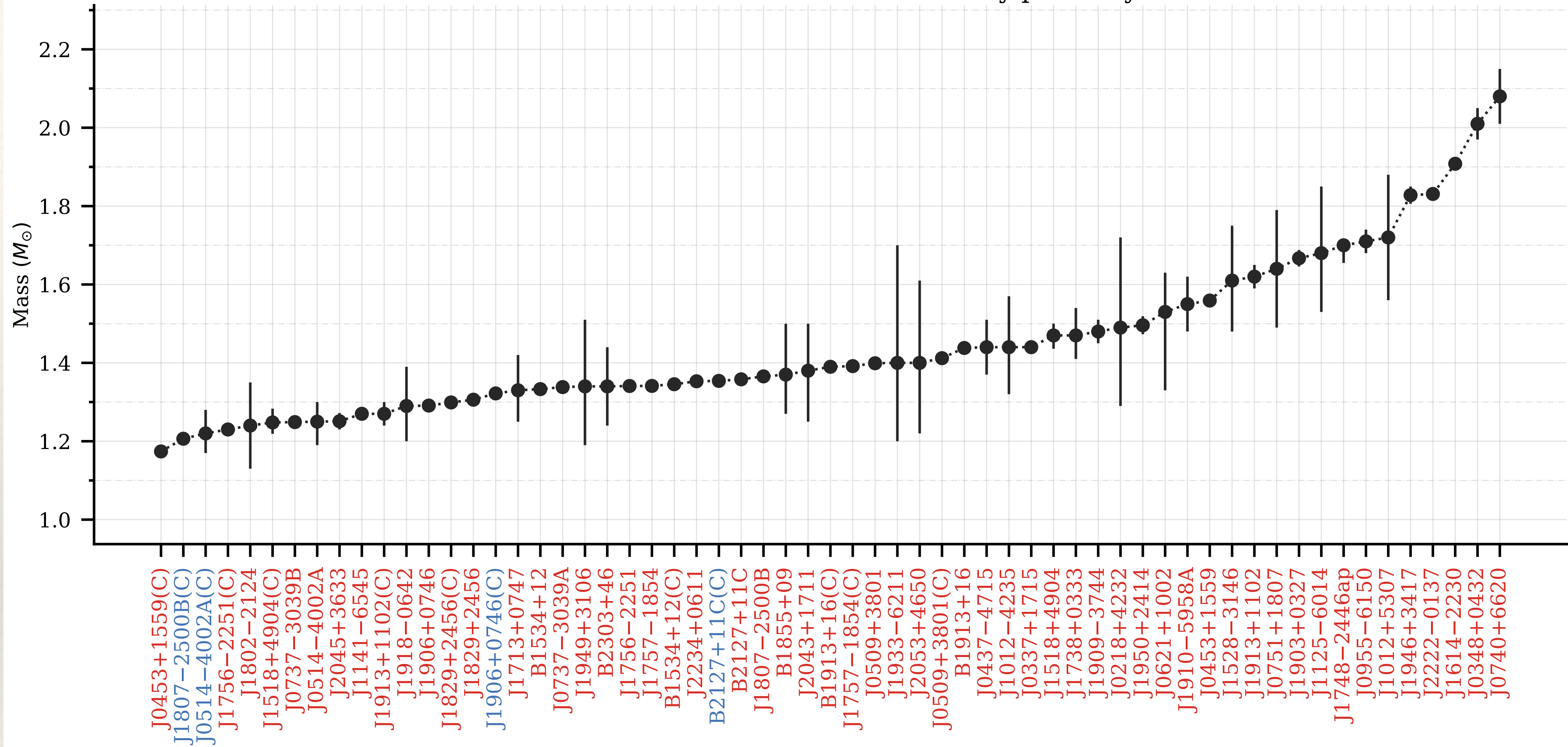
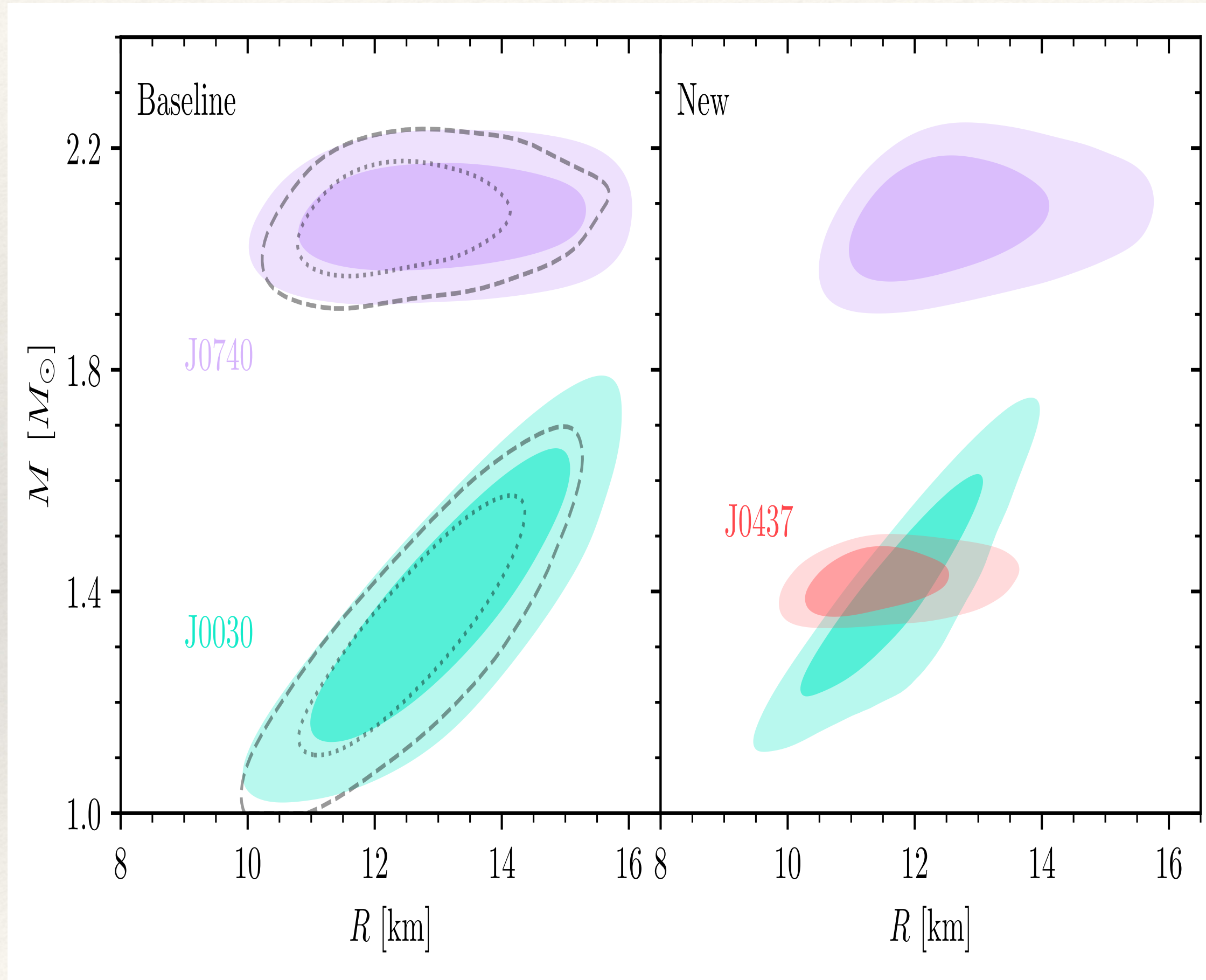


Figure: paulo freire and vivek k. krishnan 2024

A list of 136 known pulsar (PSR) masses can be found at Fan et al., PRD 109 (2024)

NICER M-R measurements



$$J0030 : M = 1.40^{+0.13}_{-0.12} M_{\odot}, R = 11.71^{+0.88}_{-0.83} \text{ km}$$

Or,

$$M = 1.70^{+0.18}_{-0.19} M_{\odot}, R = 14.44^{+0.88}_{-1.05} \text{ km}$$

(Vinciguerra et al. 2023)

$$J0740 : M = 2.07 \pm 0.07 M_{\odot}, R = 12.49^{+1.28}_{-0.88} \text{ km}$$

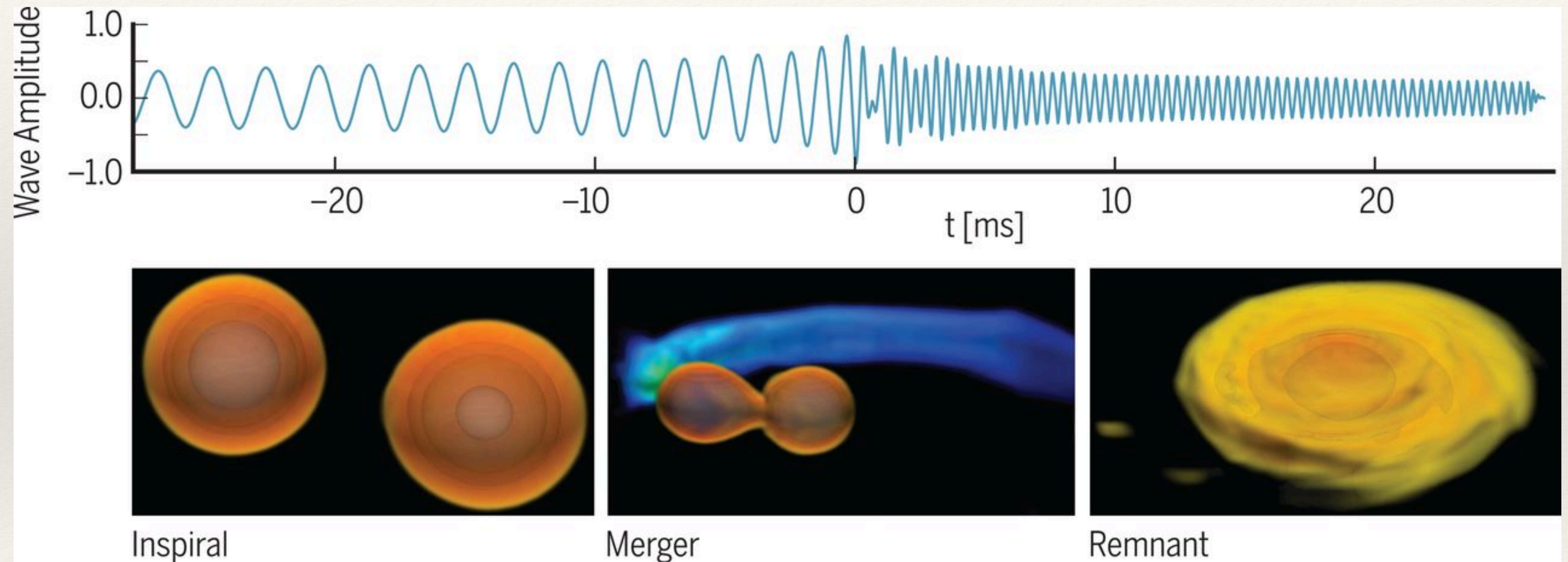
(Salmi et al. 2024)

$$J0437 : M = 1.418 \pm 0.037 M_{\odot}, R = 11.36^{+0.95}_{-0.63} \text{ km}$$

km

(Choudhury et al. 2024)

GW waveform of two merging NSs



Pic credit: S. Bernouzzi

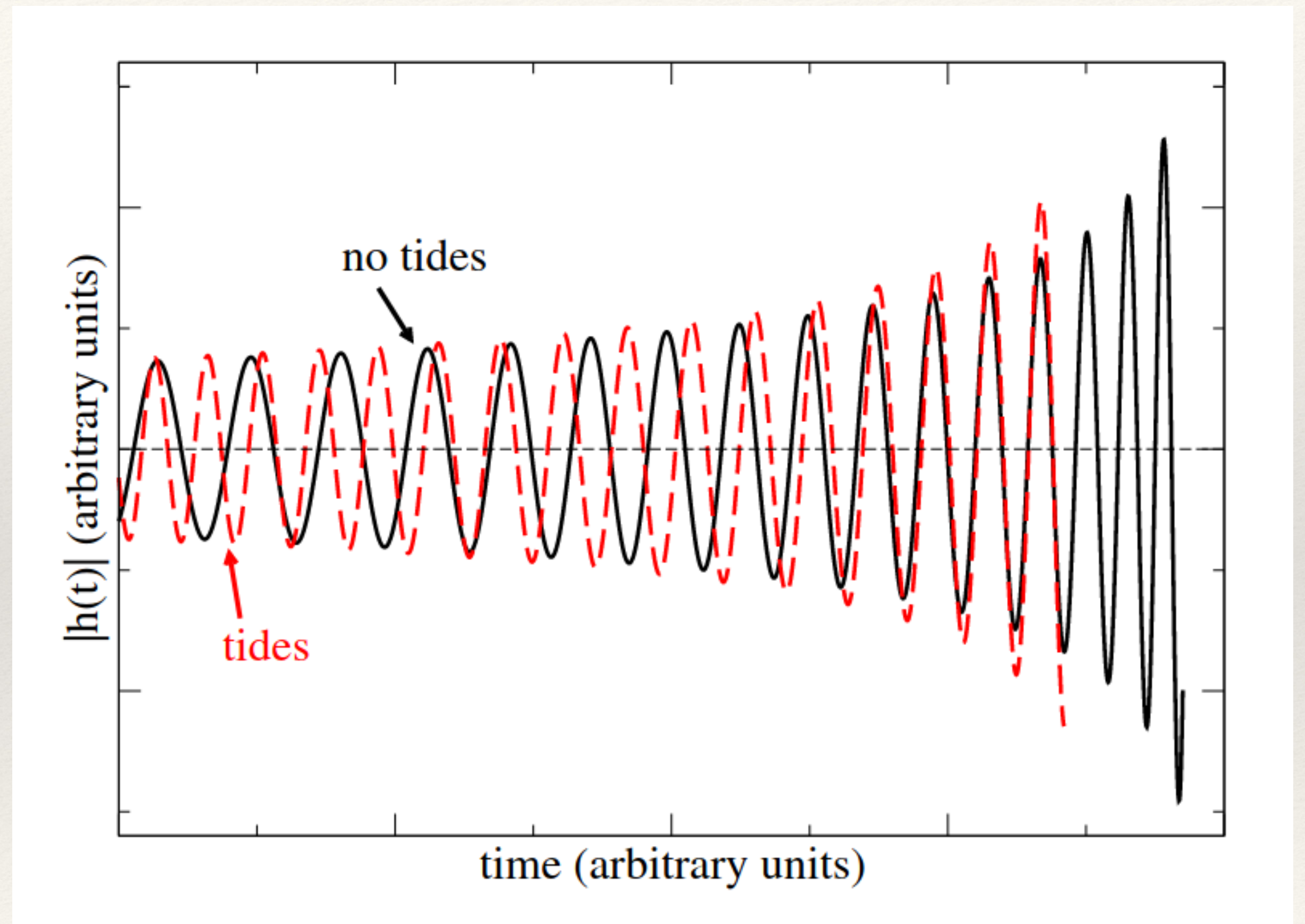
Fundamental physics with Inspiral Phase

In inspiral phase, tidal deformation of neutron star leaves an imprint on GW waveform which can tell us about the EOS

$$Q_{ij} = -\lambda \epsilon_{ij}$$

$$\lambda = \frac{2}{3} k_2 R^5$$

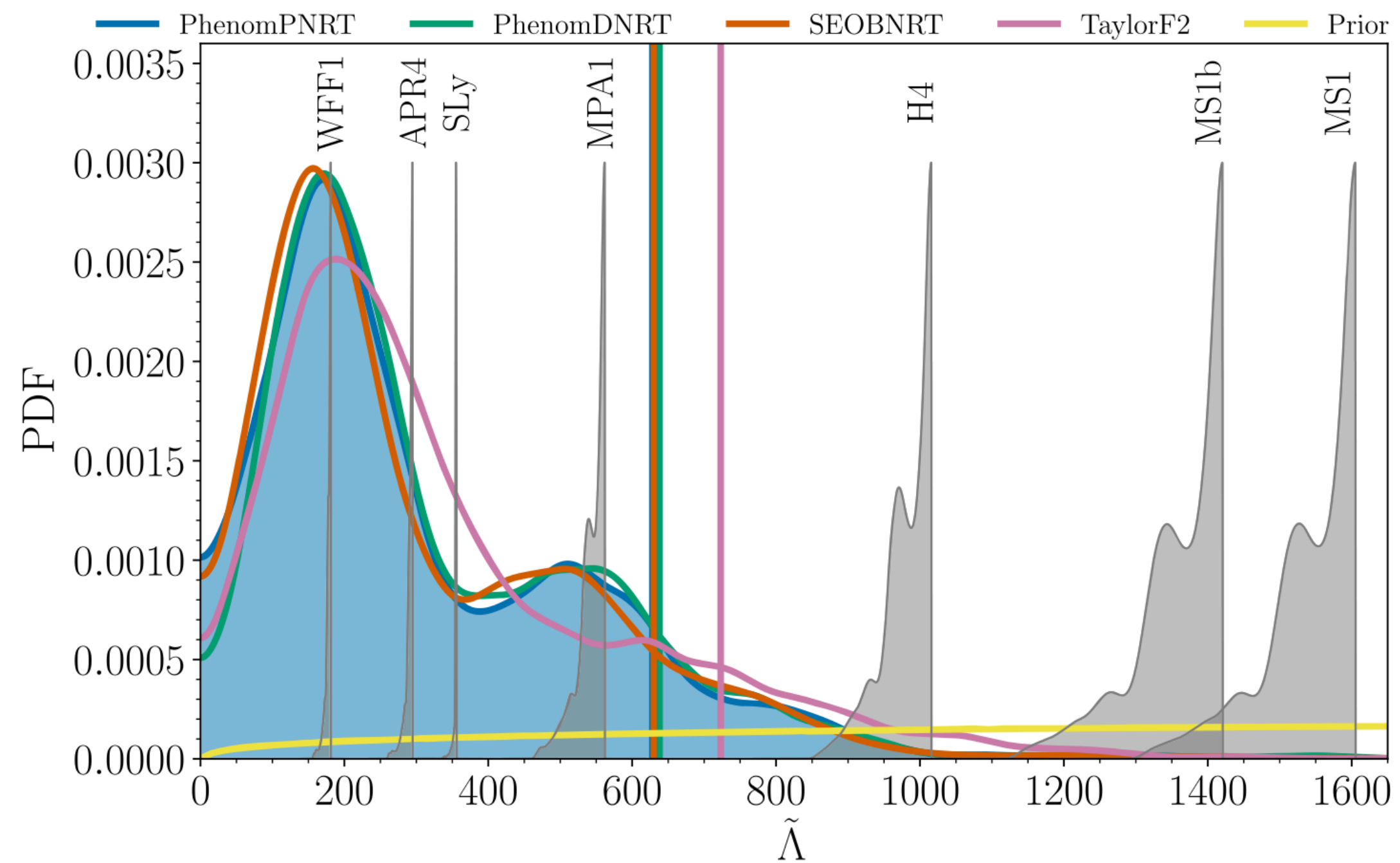
λ and k_2 are the tidal deformability and tidal Love number respectively



Pic. Credit : Z. Carson

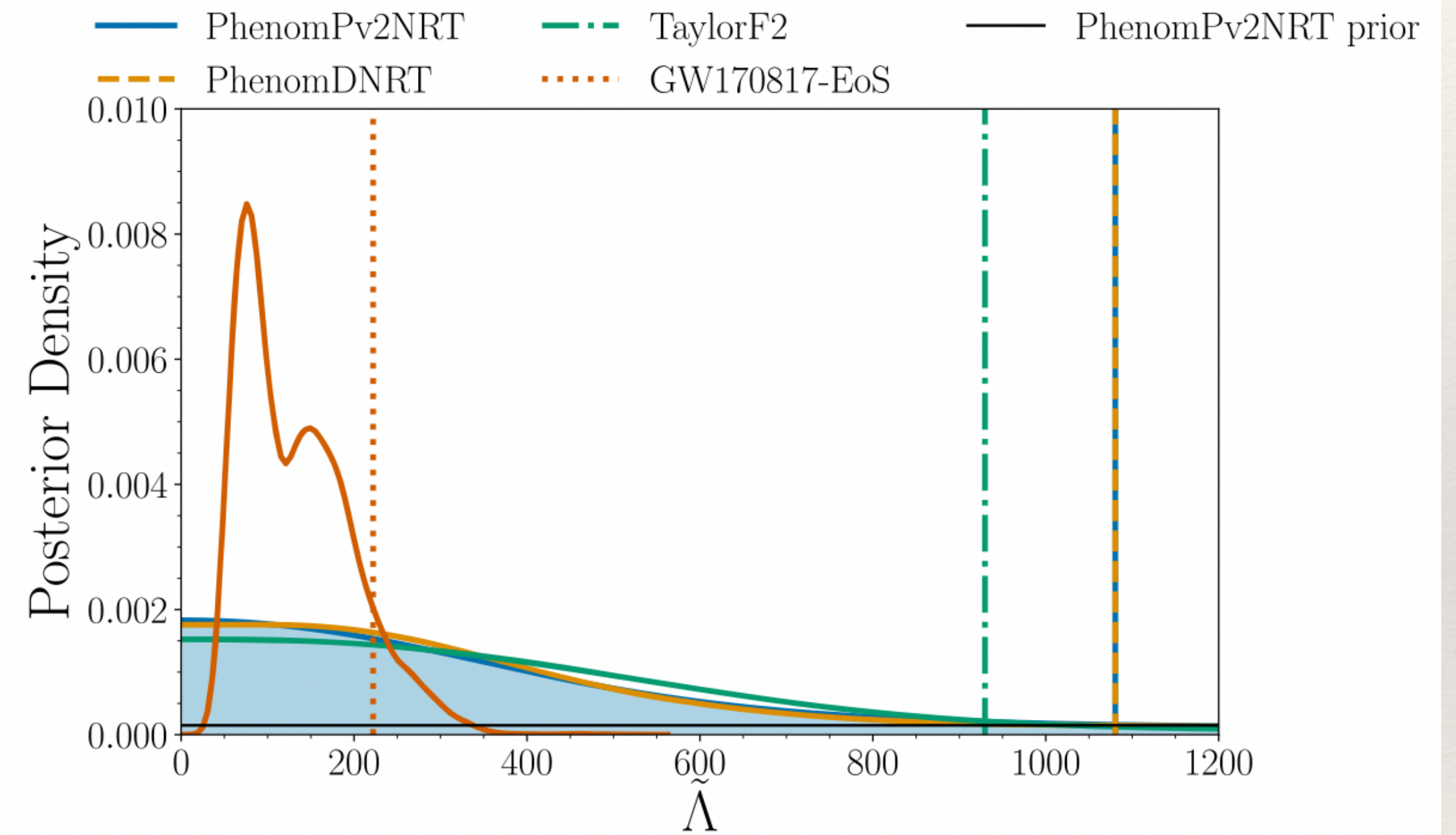
Tidal deformability from BNS mergers

GW170817, LVK PRX 2019



- ❖ Presence of EM counterpart
- ❖ Information on tidal deformation

GW190425, LVK ApJL 2020

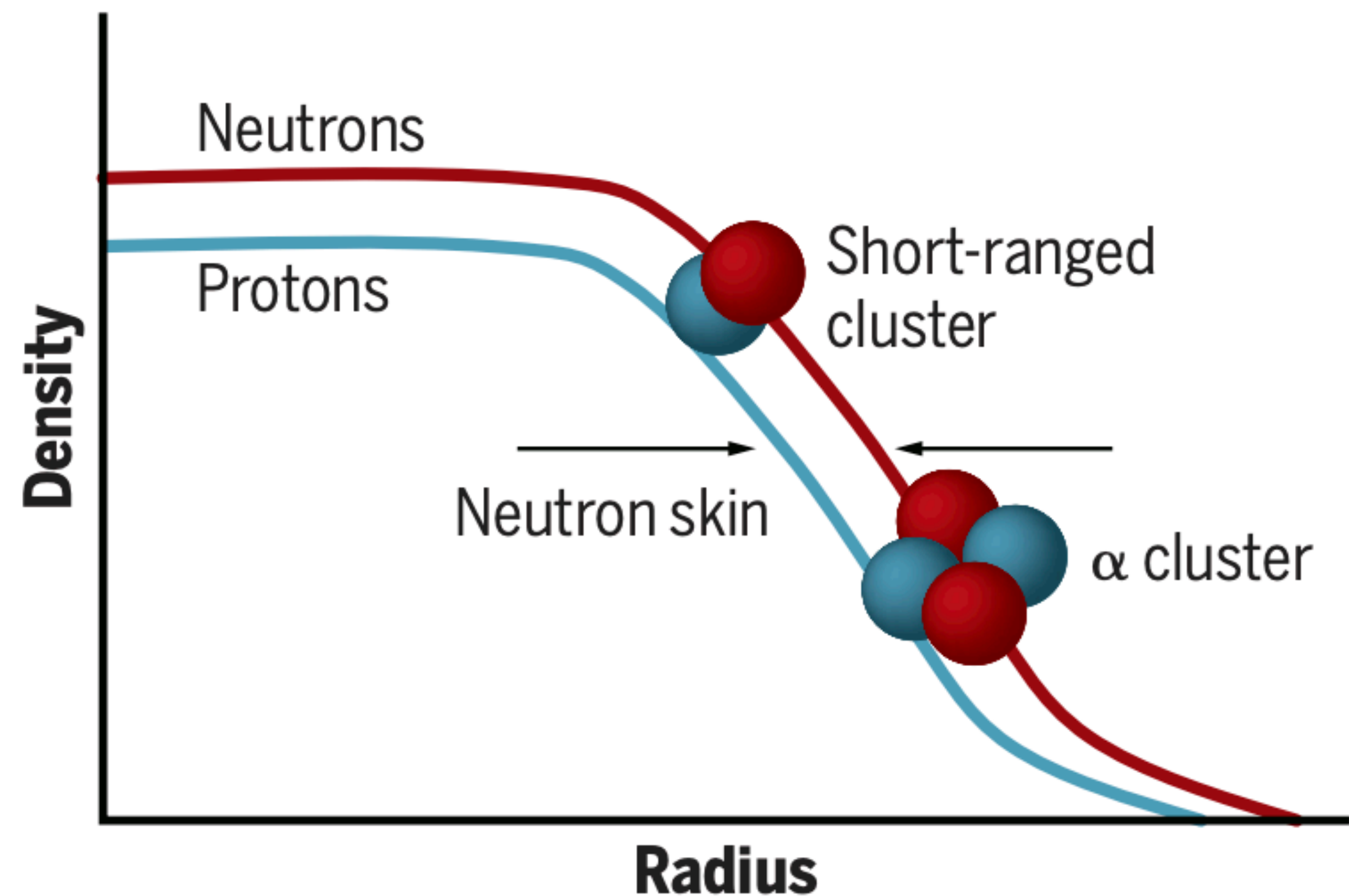


- ❖ EM counterpart is not detected
- ❖ Weak measurements of tidal deformability

New terrestrial experiments

Hen, Science 371, 232 (2021)

Nucleon density in neutron-rich nuclei



- ❖ Neutron skin thickness strongly correlates with pressure
- ❖ PREX-II measured the neutron skin thickness of ^{208}Pb , $R_{\text{skin}}^{208} = 0.283 \pm 0.071$
- ❖ CREX measured the neutron skin thickness of ^{40}Ca , $R_{\text{skin}}^{40} = 0.121 \pm 0.026$
- ❖ Skin thicknesses are strongly correlated with slope parameter L ,

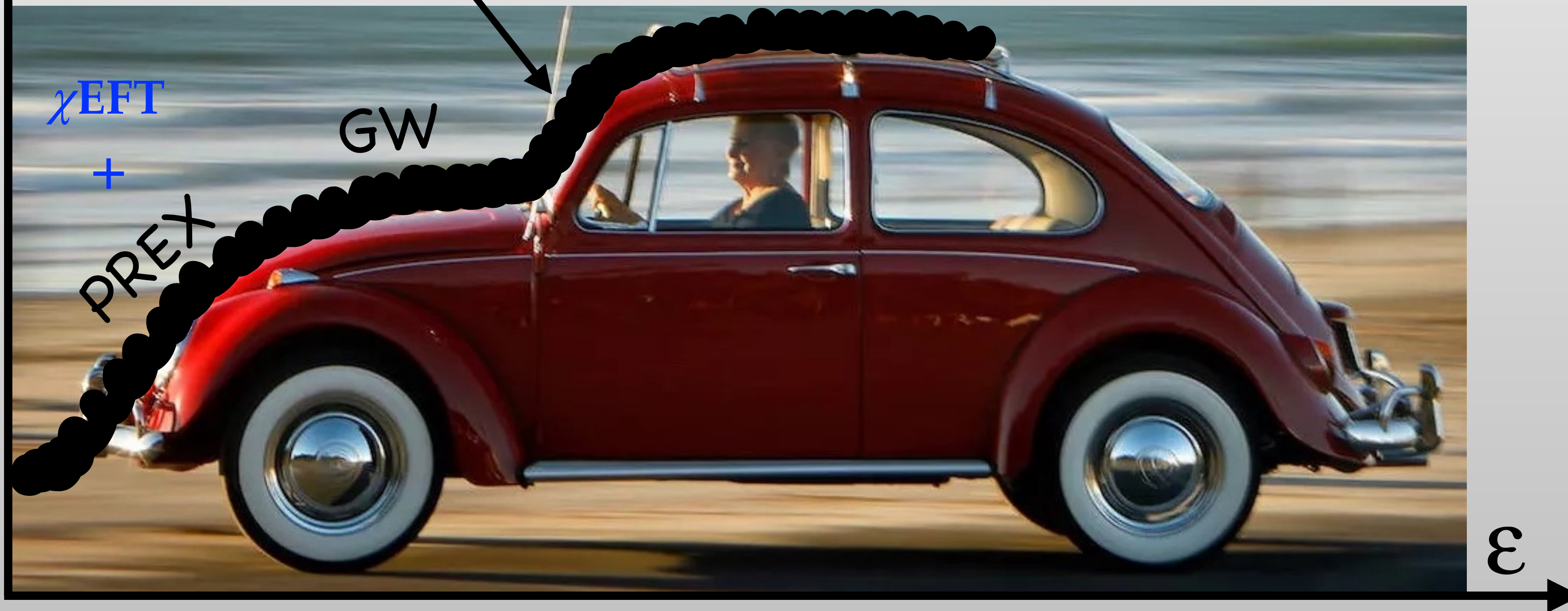
$$R_{\text{skin}}^{208}[\text{fm}] = 0.101 + 0.00147 \times L[\text{MeV}] .$$

$$R_{\text{skin}}^{48} = 0.0416 + 0.6169 R_{\text{skin}}^{208} .$$

$\rho(\varepsilon)$

VW-Beetle Equation of State

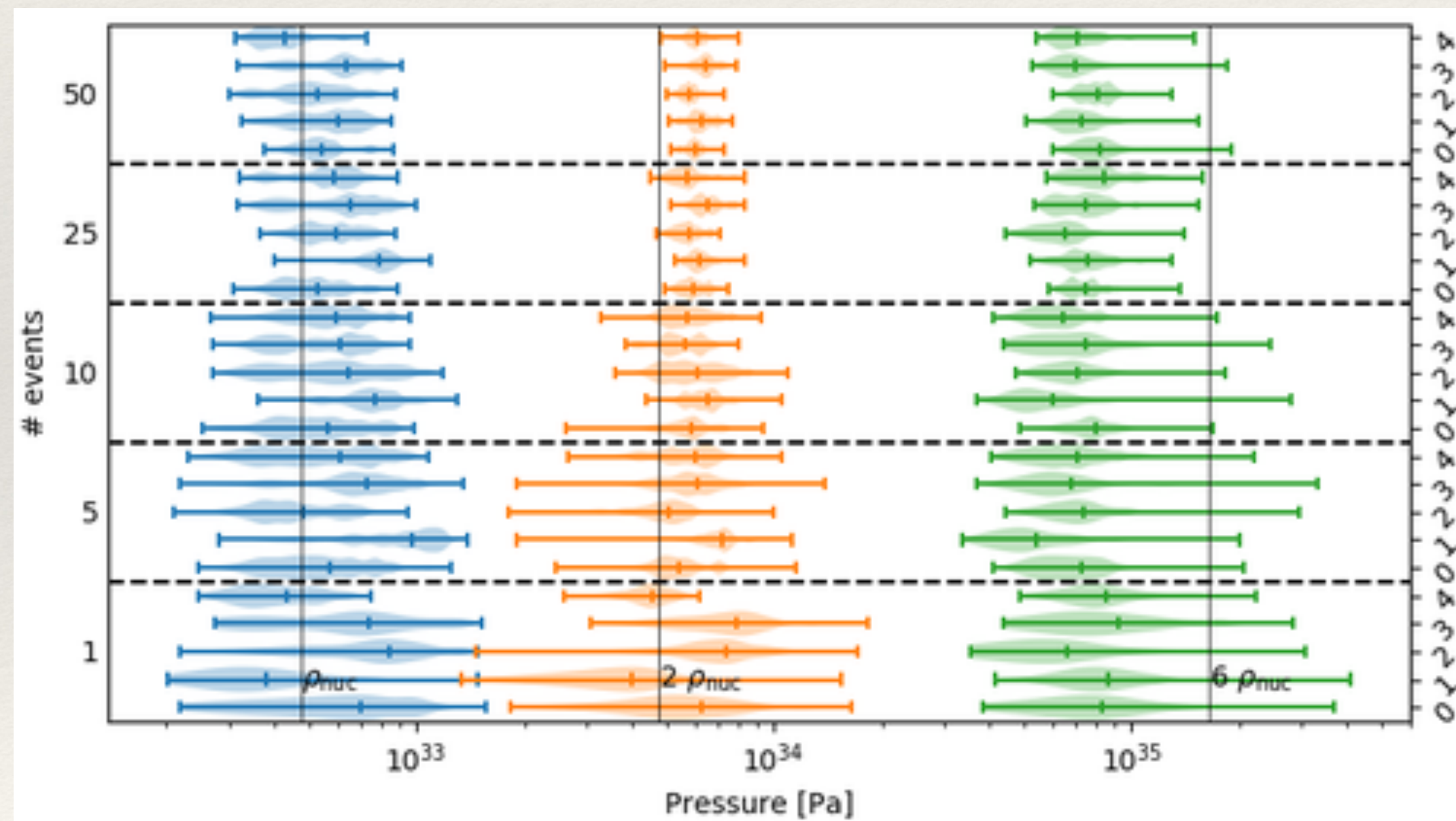
NICER + Heavy Pulsars + pQCD



Bayesian approach to constrain NS EOS

Wrong population model biases EOS inference

Wysocki et al., arXiv: 2001.01747



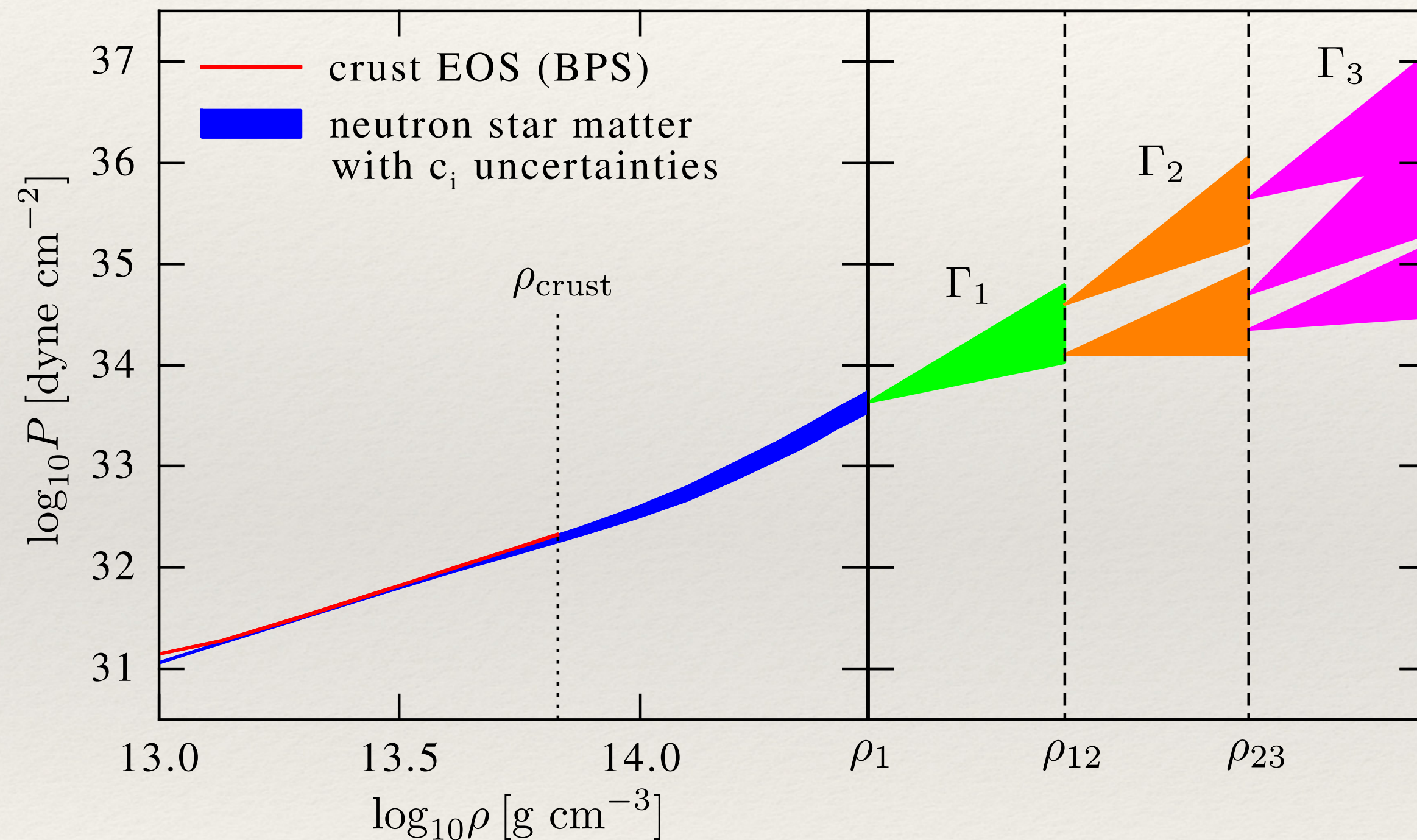
Bayesian statistics to simultaneously infer
NS EOS and population model

$$\diamond P(\theta | d) \propto P(\theta) \prod_i P(d_i | \theta),$$

Posterior Prior Likelihood

$\theta \in$ (EOS and mass population parameters)

Hybrid nuclear+PP EoS parameterization



Pic credit: Hebeler et al. ApJ, 773 (2013)

- ❖ In outer crust Sly EOS is used
- ❖ Then below $1.1\rho_0$ saturation properties of nuclear matter is used

$$e(\rho, \delta) \approx e_0(\rho) + e_{\text{sym}}(\rho)\delta^2$$

$$e_0(\rho) = e_0(\rho_0) + \frac{K_0}{2}\chi^2 \dots,$$

$$e_{\text{sym}}(\rho) = e_{\text{sym}}(\rho_0) + L\chi + \frac{K_{\text{sym}}}{2}\chi^2 + \dots$$

$$\delta = (\rho_n - \rho_p)/\rho,$$

$$\chi = (\rho - \rho_0)/3\rho_0$$

- ❖ At high densities piecewise-polytrope is used with varying transition densities

Mass distribution model

- ❖ For simplicity we assume all NSs in the universe follow double Gaussian distribution

$$P_{\text{NN}}(M|\mu_1, \sigma_1, \mu_2, \sigma_2, w, M_{\text{min}}, M_{\text{max}}) = \frac{[w\mathcal{N}(M|\mu_1, \sigma_1)/B + (1-w)\mathcal{N}(M|\mu_2, \sigma_2)/C]}{U(M|M_{\text{min}}, M_{\text{max}})},$$

$$U(M|M_{\text{min}}, M_{\text{max}}) = \begin{cases} \frac{1}{M_{\text{max}} - M_{\text{min}}} & \text{if } M_{\text{min}} \leq M \leq M_{\text{max}}, \\ 0 & \text{else.} \end{cases}$$

- ❖ This assumption might not be true as GWs may follow a different distribution.
(Landry and Read, 2021)

But too less detections, to make any conclusion

Priors

- ❖ Some empirical parameters are kept fixed in our analysis

$$n_0 = 0.16 \text{ fm}^{-3}$$

$$e_0(n_0) = -15.9 \text{ MeV}$$

$$K_0 = 240 \text{ MeV}$$

$$e_{\text{sym}} = 31.7 \text{ MeV}$$

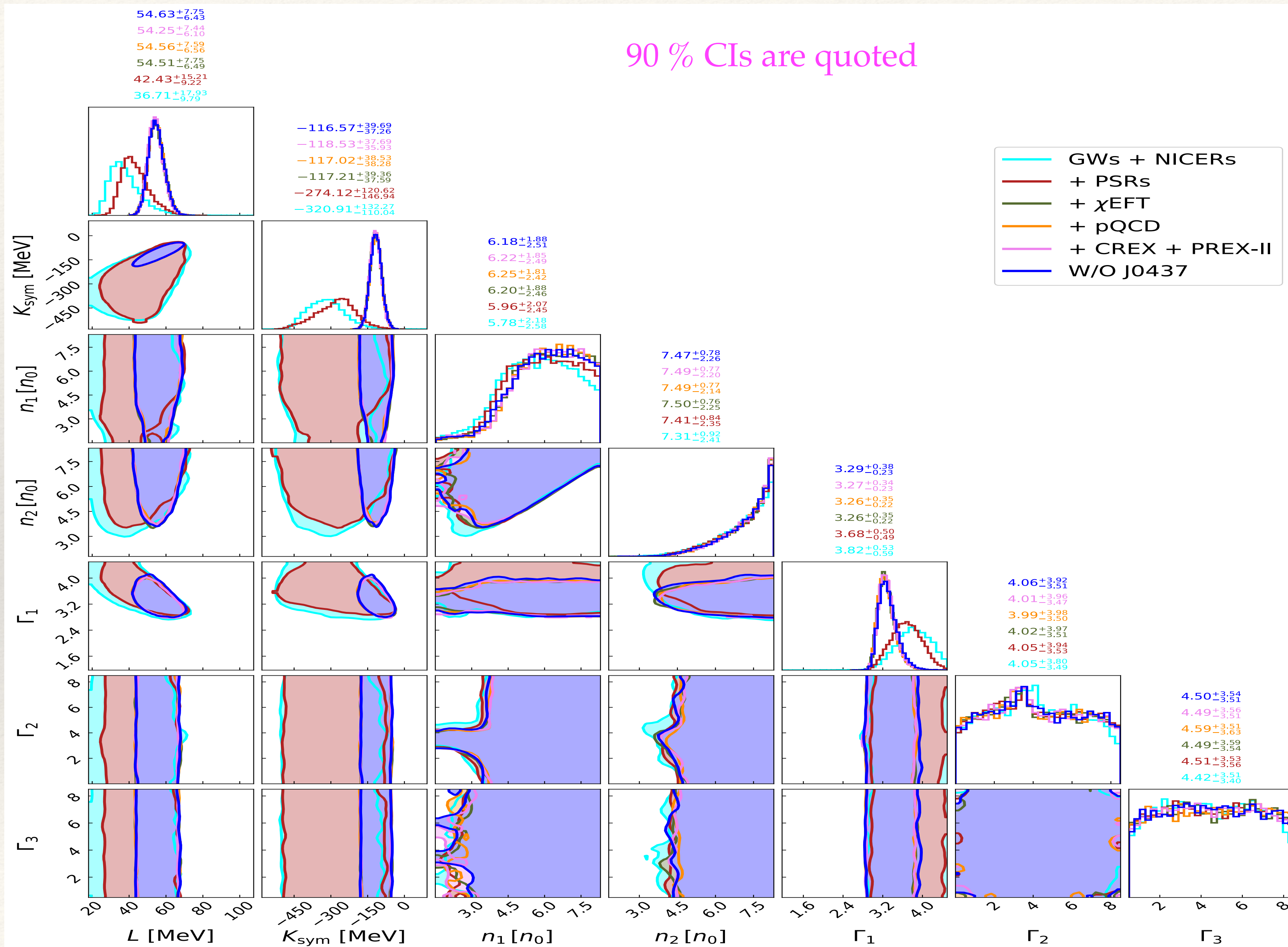
Uncertainty in n_0 and e_0 are already small.

K_0 and e_{sym} have weak influence on NS M, R, Λ .

- ❖ For all the parameters wide uniform priors are kept.

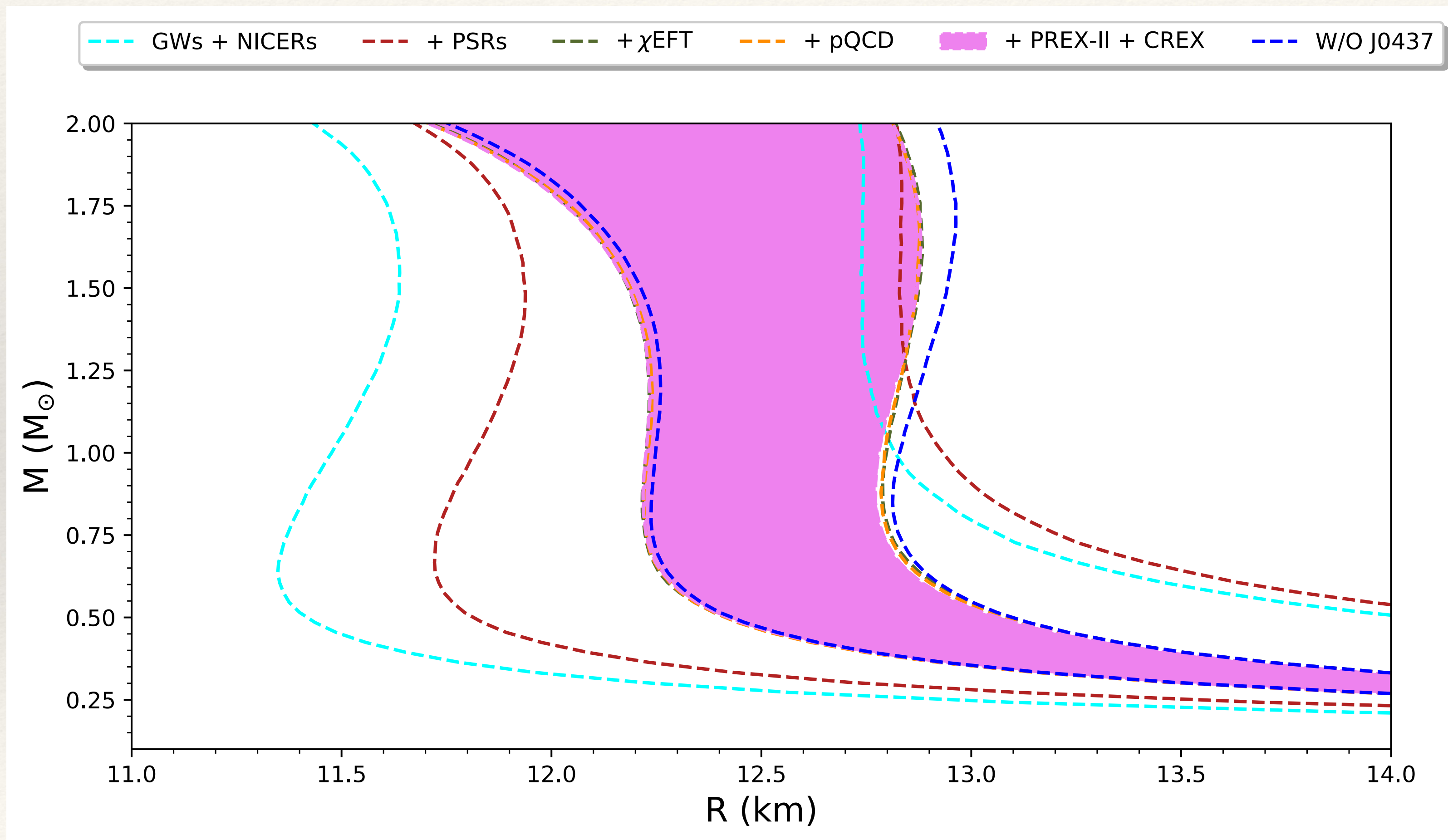
Model	Parameters	Units	Prior
EOS	L	MeV	$U(0, 150)$
	K_{sym}	MeV	$U(-600, 100)$
	n_1	n_0	$U(1.5, 8.3)$
	n_2	n_0	$U(n_1, 8.3)$
	Γ_1	-	$U(1, 4.5)$
	Γ_2	-	$U(0, 8.5)$
	Γ_3	-	$U(0.5, 8.5)$
Mass	μ_1	M_{\odot}	$U(0.9, \mu_2)$
	σ_1	M_{\odot}	$U(0.01, \sigma_2)$
	μ_2	M_{\odot}	$U(0.9, M_{\text{max}})$
	σ_2	M_{\odot}	$U(0.01, 1.0)$
	w	-	$U(0.1, 0.9)$

Posterior of EOS parameters



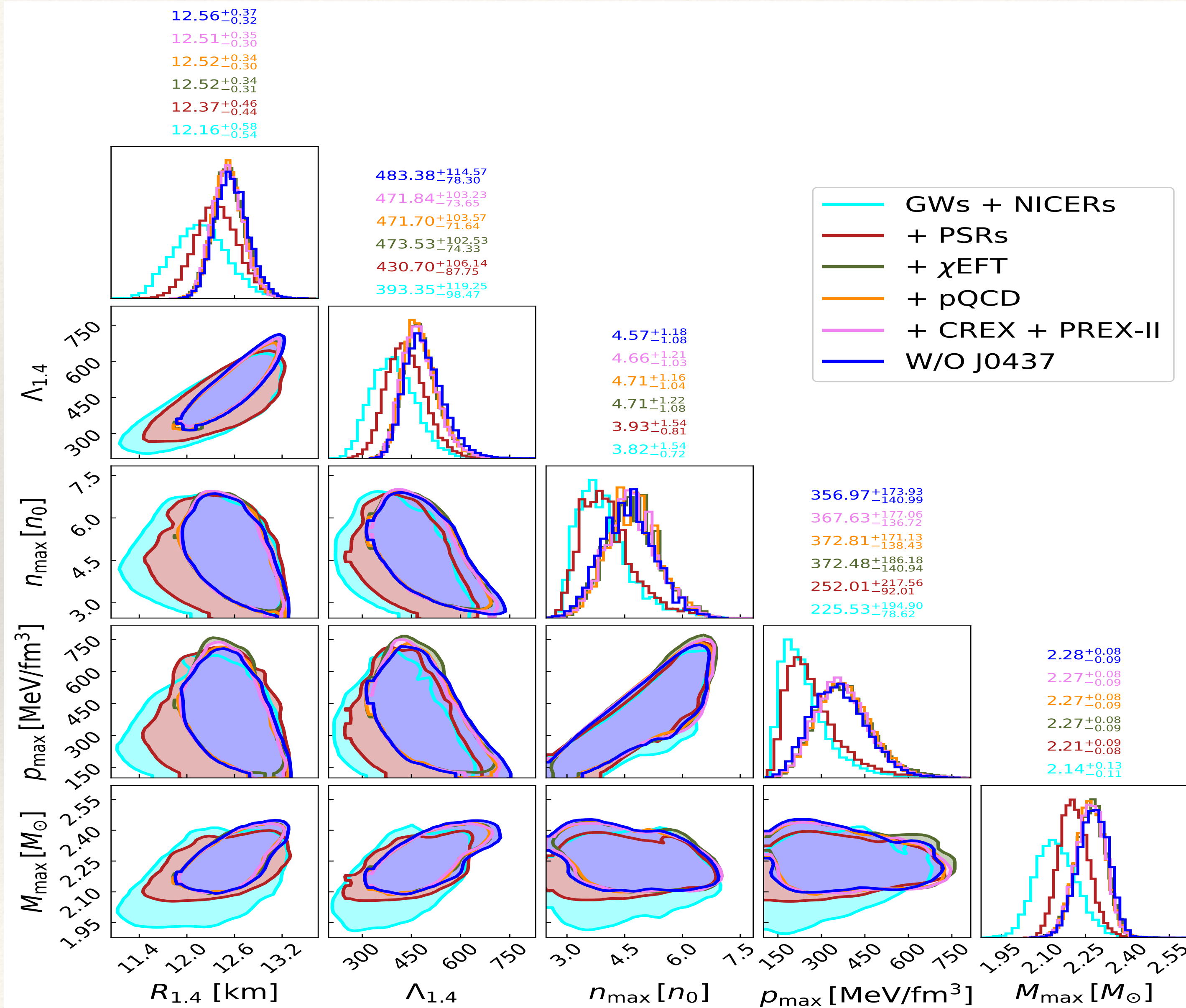
- ❖ Astrophysical Observations Constrain Nuclear Parameters
- ❖ Addition of 129 PSRs measurements have visible impact on the EOS parameters
- ❖ Significant Impact of χ EFT Calculations on Empirical Parameters
- ❖ Transition densities peaking at the higher end of the prior
- ❖ Γ_2 and Γ_3 are uninformative

Mass-radius band



- ❖ **Addition of PSRs** mass measurements overall **tightens** the M-R band
- ❖ **Significant impact** of χ EFT
- ❖ **No noticeable impact** by pQCD, CREX, and PREX-II
- ❖ PSR J0437 slightly **soften** the posterior

Constraints on a few key quantities



90 % CIs

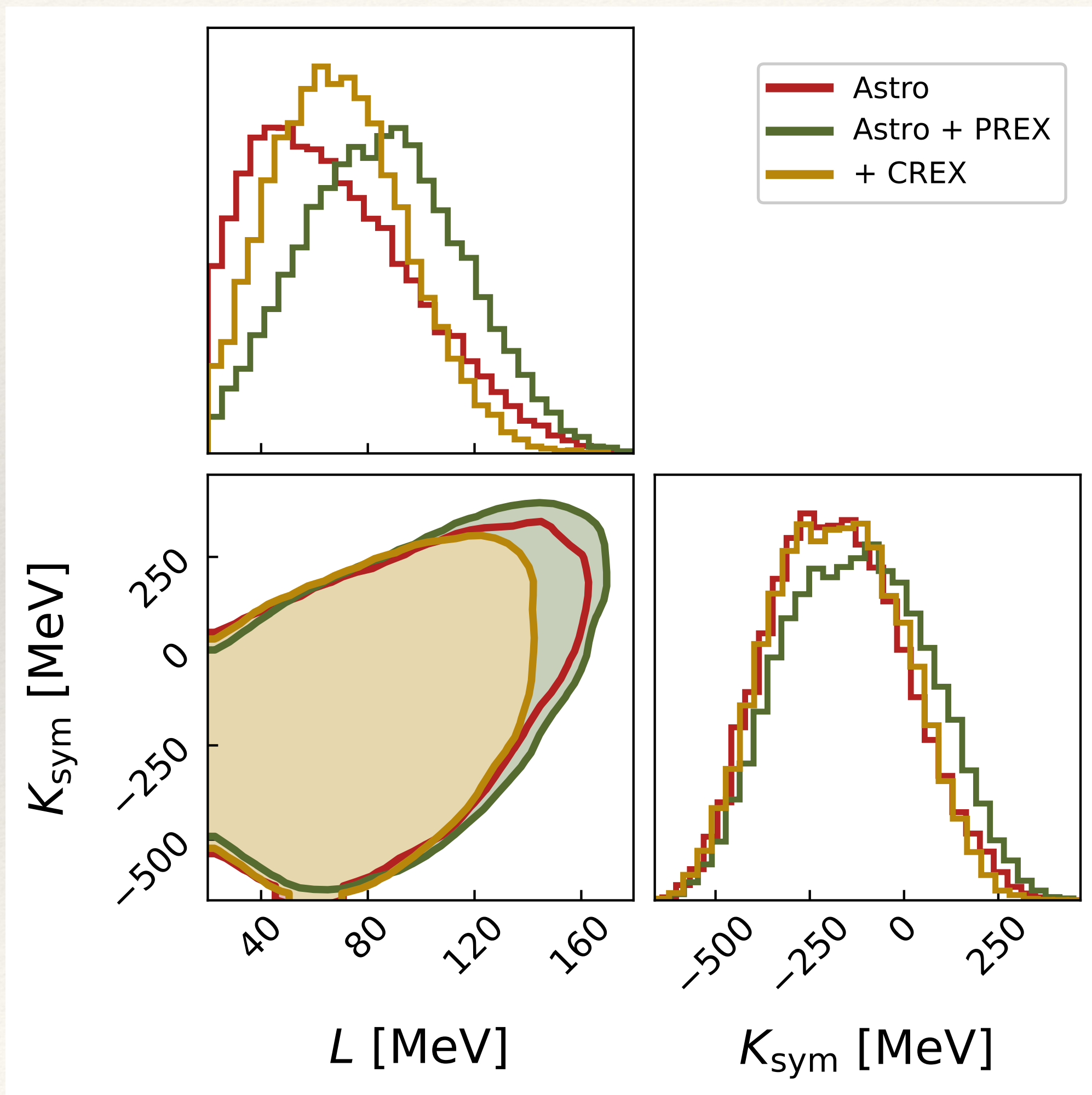
$$12.21 < R_{1.4} [\text{km}] < 12.86$$

$$398 < \Lambda_{1.4} < 575$$

$$3.63 < n_{\max} [n_0] < 5.87$$

$$2.18 < M_{\max} [M_{\odot}] < 2.35$$

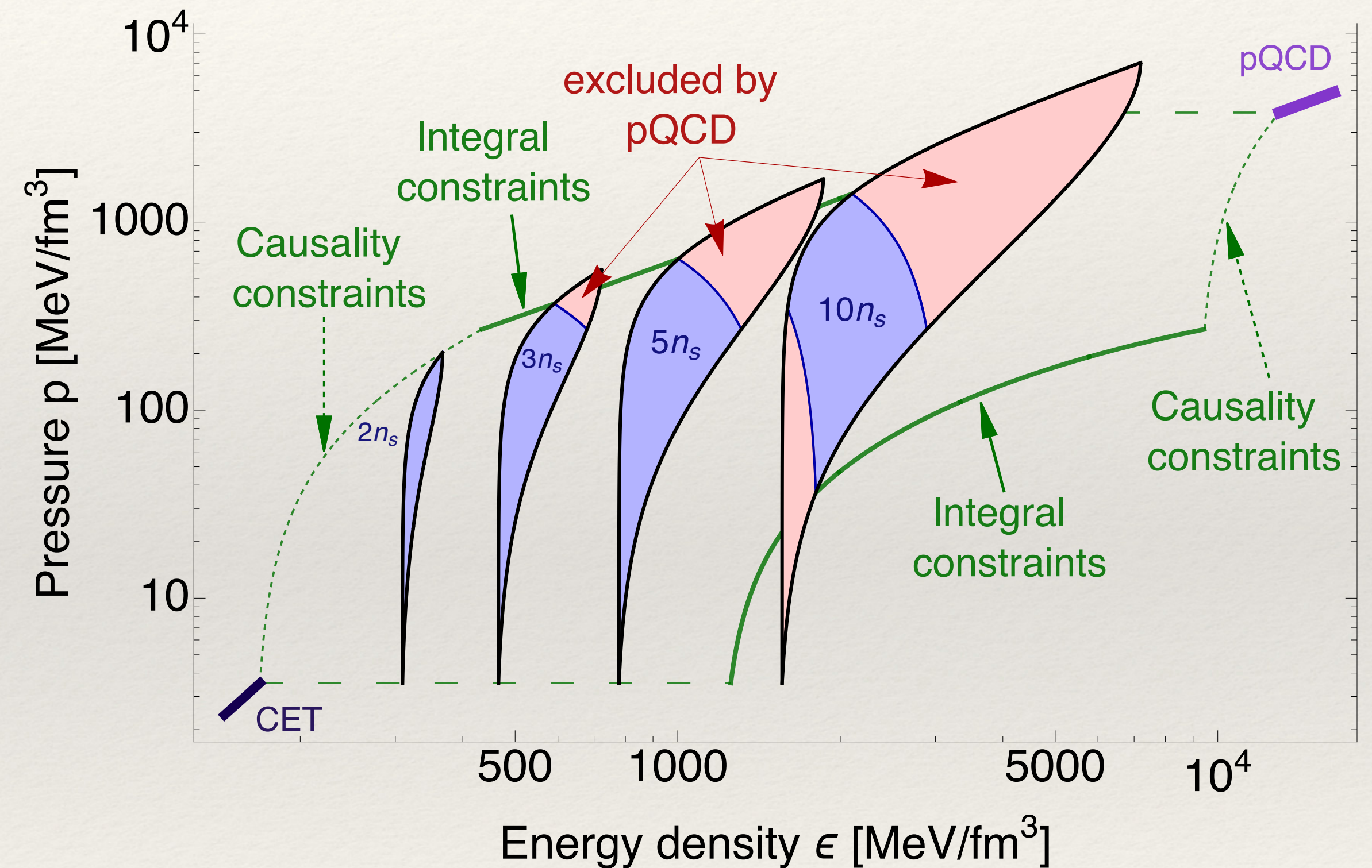
What's up with PREX-II & CREX?



- ❖ PREX-II and CREX measurements influences empirical parameters if χ^{EFT} constraints are not added
- ❖ The overall impact of PREX-II & CREX is overshadowed by χ^{EFT}

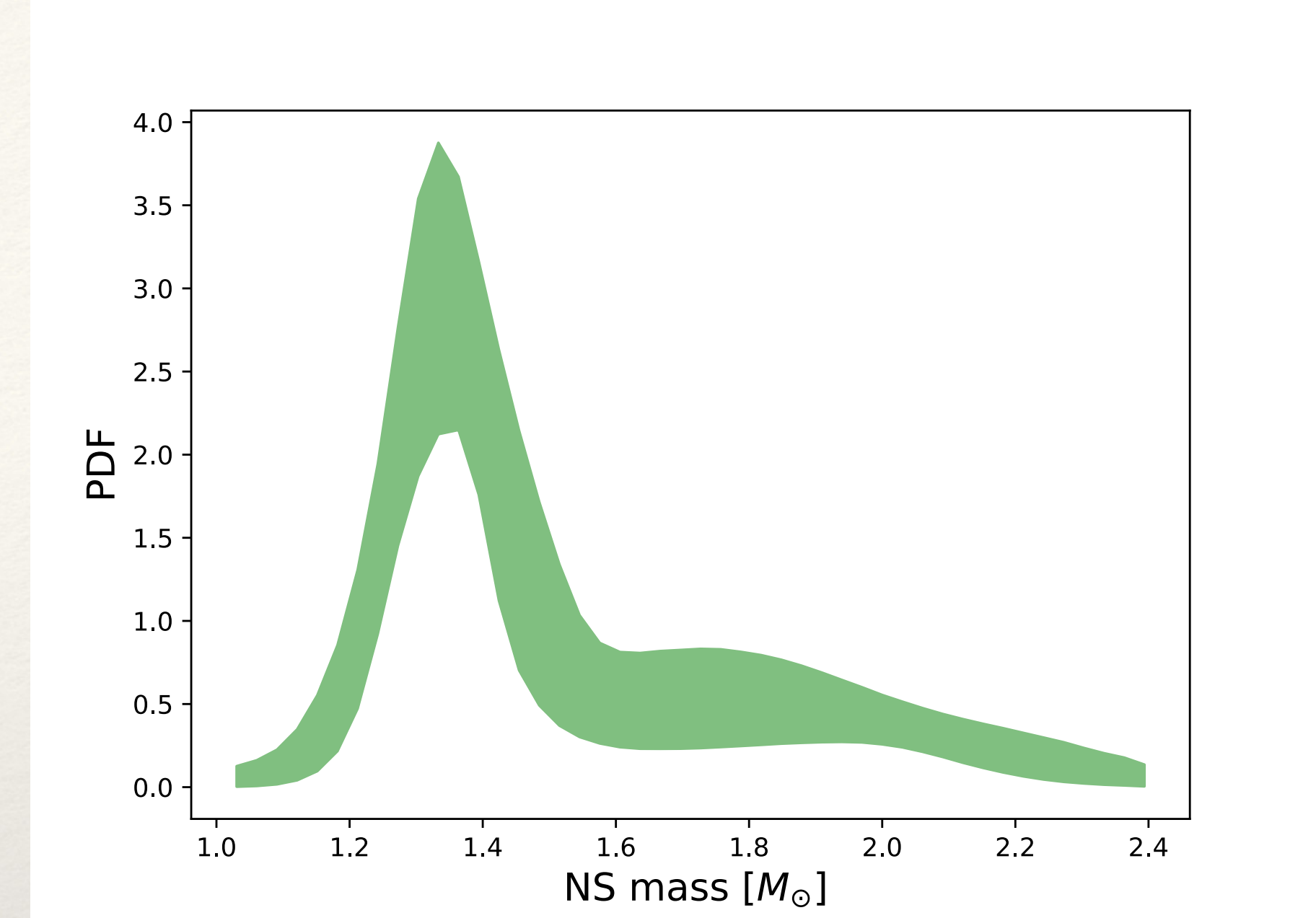
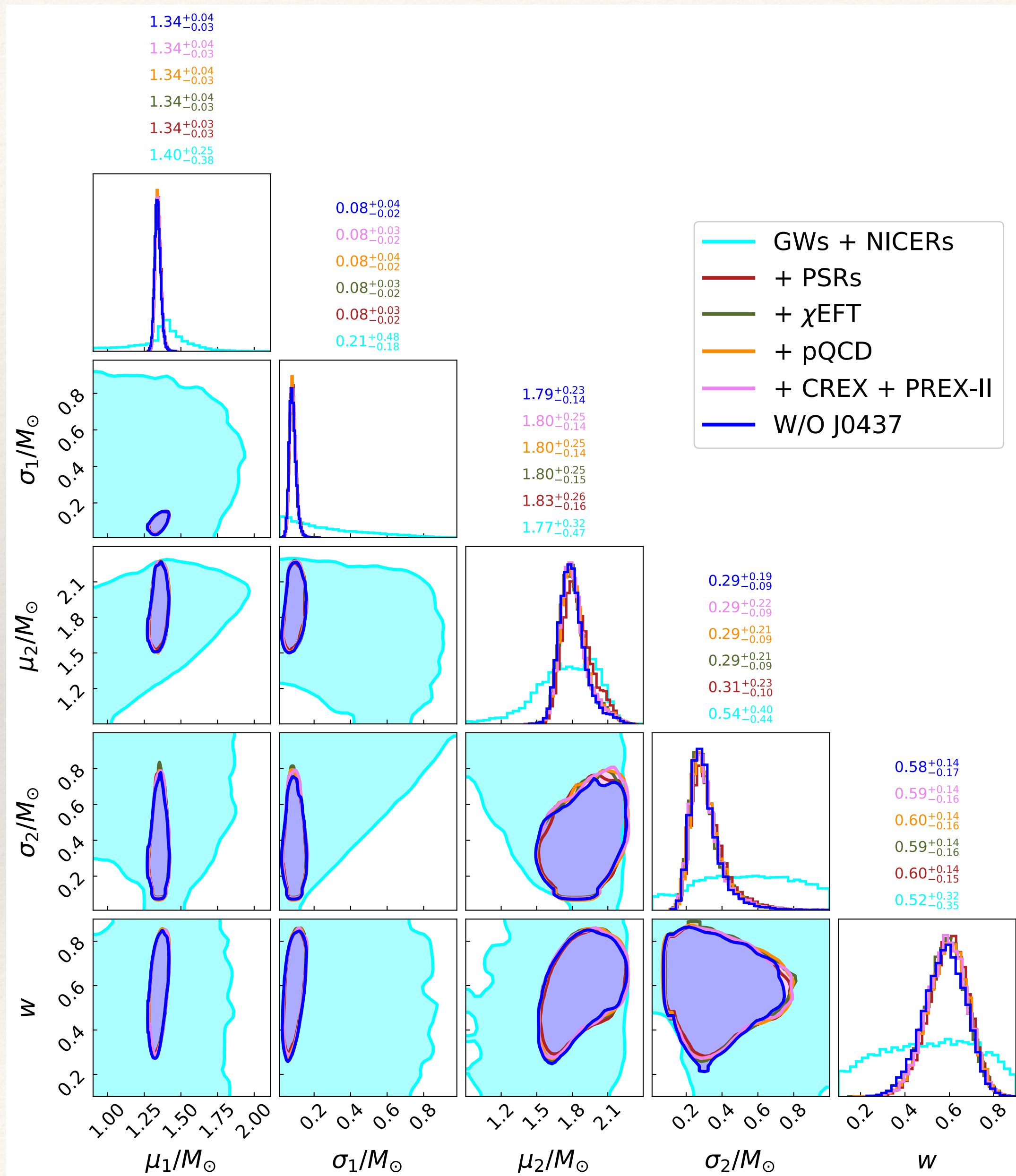
Why is pQCD uninformative?

- ❖ To check if an EOS is consistent with the pQCD prediction, we assume knowledge of the EOS at a low-density limit
- ❖ This choice is arbitrary
- ❖ Previous works used an ad hoc density of $n_{\text{low}} = 10 n_s$ and conclude pQCD can rule out soft EOSs above $2.2 n_0$
- ❖ We choose corresponds to central density of the maximum mass star and observe negligible impact



Komoltsev and Kurkela, PRL 128, 202701 (2022)

Posterior of NS mass distribution



- ❖ Overall constraint is dominated by the PSRs mass measurements
- ❖ Tight constraint on μ_1 and narrow spread
- ❖ Broader distribution for the secondary component

Take away points

- ❖ A comprehensive Bayesian framework to simultaneously infer NS EOS and population model is provided combining astrophysical observations and nuclear inputs
- ❖ Not only GWs and NICERs, the **addition of 129 PSRs** mass measurements overall **tightens** the M-R band
- ❖ **Significant Impact of χ EFT Calculations on Empirical Parameters and as well as the M-R band**
- ❖ PREX-II and CREX measurements influences empirical parameters **if χ EFT constraints are not added. The overall impact of PREX-II & CREX is overshadowed by χ EFT.**
- ❖ Constraints coming from pQCD have a **minimal effect** on EOS inference.