Jet substructure at RHIC and LHC

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JHEP 07 (2024) 230







## Observable definition: jet angularity

Jet angularity is defined as

$$\lambda_{\alpha} = \sum_{i \in \text{jet}} \frac{p_{t,i}}{p_{t,\text{jet}}} \left(\frac{\Delta R_{ij}}{R}\right)^{\alpha}, \quad \kappa = 1, \quad \alpha > 0$$

- Sum runs over all particles inside the jet
- Jet radius R
- Rapidity-azimuth distance  $\Delta R_{i,jet}$
- IRC (infrared and collinear) safe observable!

- LHA (Les Houches Angularity):  $\alpha = 1/2$
- Jet Width:  $\alpha = 1$
- Jet Thrust:  $\alpha = 2$



#### Impact of Multiple Partonic Interactions



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Image credit: 2203.11601

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- Protons are composite objects so several (semi-)hard partonic interactions can occur per one pp collision!
- Such processes generally know as Multiple Partonic Interactions (MPI)
- MPI cause multiple uniform soft emissions which "contaminate" jet substructure





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#### Fixed order (FO) jet substructure calculations



- A "standard" 2-to-2 QCD process cannot be used for jet substructure calculations (no substructure!)
- So one needs to take 2-to-2 process and add more emissions to it
- Jet substructure can be studied already for the 2-to-3 processes
- It is called fixed-order (FO) calculation.
- However, higher order corrections e.g. 2-to-4, 2-to-5 etc. in general are difficult to calculate

#### Resummation: leading log (LL)



2-to-3 cross section gets a di-log enhancement:

 $d\sigma \sim d(\log \theta^2) \, d(\log z)$ 

Let's define a simple IRC safe jet substructure observable:

$$\tau = z\theta^2$$

In case of multiple emissions:

$$\tau = \sum_{i=\text{gluon}} z_i \theta_i^2$$

#### Resummation: leading log (LL)



Multiple gluon emissions exponentiate:

$$P_q(x < \tau) = \exp\left(-\frac{\alpha_s}{\pi}\frac{C_F}{2}\log^2\tau\right)$$

Similar expression can be obtained for quark emissions:

$$P_g(x < \tau) = \exp\left(-\frac{\alpha_s}{\pi}\frac{C_A}{2}\log^2\tau\right)$$

Note that both expressions are finite if  $\tau \rightarrow 0$  whereas FO result diverges!

For more details see: 1709.06195

#### Resummation: next-to-leading log (NLL)

In general:

$$P_{q/g} = 1 + \alpha_S \left( c_{22}L^2 + c_{21}L + \dots \right) + \alpha_S^2 \left( c_{24}L^4 + c_{23}L^3 + \dots \right) + \dots$$

Both LL and NLL resummation can be performed separately for quark and gluon production channels!

Therefore, resummed expressions can be used to define "quark" and "gluon" jets!

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### Resummation and matching to fixed order (FO) results



## Resummation and matching to fixed order (FO) results



Matching to FO results:

- Excludes double counting between overlapping phase space regions.
- Provides finite results at small values of observable of interest
- Matching "quark" and "gluon" jet contributions can be done separately which leads to NLL' accuracy level

#### CAESAR approach by Banfi, Salam and Zanderighi

CAESAR allows to automate resummation for each observable that can be parametrized as

$$\Sigma_{\rm res}(v) = \sum_{\delta} \Sigma_{\rm res}^{\delta}(v) , \text{ with}$$

$$\Sigma_{\rm res}^{\delta}(v) = \int d\mathcal{B}_{\delta} \frac{d\sigma_{\delta}}{d\mathcal{B}_{\delta}} \exp\left[-\sum_{l\in\delta} R_{l}^{\mathcal{B}_{\delta}}(L)\right] \mathcal{P}^{\mathcal{B}_{\delta}}(L) \mathcal{S}^{\mathcal{B}_{\delta}}(L) \mathcal{F}^{\mathcal{B}_{\delta}}(L) \mathcal{H}^{\delta}(\mathcal{B}_{\delta}) ,$$
• Born cross section  $\frac{d\sigma_{\delta}}{d\mathcal{B}_{\delta}}$ 
• Soft function  $\mathcal{S}$ 

- Ratio of PDFs  $\mathcal{P}$
- Multiple emission function  $\mathcal{F}$
- Collinear radiator  $R_l$
- Kinematic cuts  $\mathcal{H}$

CAESAR = Computer Automated Expert Semi-Analytical Resummer, see the original paper by A.Banfi, G.Salam and G. Zanderighi 0407286

## Parton-level (PL) CAESAR predictions



- ✓ The resumation is performed at NLL accuracy level
- ✓ The NLL results are matched to NLO FO results leading to NLO+NLL' accuracy level
- The calculations are automated and are available as a CAESAR resummation plugin to SHERPA MC 2404.04168, 2112.09545, 2104.06920

## Parton-level (PL) CAESAR predictions



- Our results for jet angularities are at highest available accuracy NLO+NLL' level
- Result are available for LHA, Jet Width and Jet Thrust (for ungroomed and groomed jets)
- The increase in accuracy of calculation reduces the size of uncertainty bands. Usually data has smaller errorbars (at least at the LHC) hence further improvement in accuracy of the calculation is desirable (though it is very challenging)

### Parton-level (PL) vs. hadron-level (HL) distributions



- Perturbative calculations do not describe physics at low energy scales
- Two major NP-contributions are due to MPI and hadronization
- Unlike the LHC case, at RHIC the NP-effects dominate

## Parton-level vs. hadron-level distributions



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- Two major NP-contributions are due to MPI and hadronization
- Unlike the LHC case, at RHIC the NP-effects dominate
- Large NP-contirbutions are predominantly coming from fragmentation of jets made out of a single parton causing bin-bigration

#### MPI multiplicity at RHIC



TABLE I. PYTHIA 8 settings and tuning parameters.

Setting	Default	New
PDF:pSet	13	17
MultipartonInteractions:ecmRef	$7 { m TeV}$	$200  {\rm GeV}$
${\it Multipart on Interactions: bprofile}$	3	2
Tuning Parameter	Default	Range
MultipartonInteractions: pT0Ref	$2.28 { m GeV}$	$0.5-2.5 \mathrm{GeV}$
Multipart on Interactions: ecmPow	0.215	0.0 - 0.25
MultipartonInteractions:coreRadius	0.4	0.1 - 1.0
MultipartonInteractions:coreFraction	0.5	0.0 - 1.0
ColourReconnection:range	1.8	1.0 - 9.0

#### Detroit PYTHIA tune (2110.09447)

#### MPI multiplicity at RHIC



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Detroit tune parameter choice essential means suppression of MPI production at RHIC!

#### Impact of MPI on jet substructure



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Different MPI tunes lead to somewhat different shapes of jet angularities

#### Incorporation of non-perturbative corrections

 Hadron level to parton level ratio: one simulates the same observable at parton and hadron levels then multiplies resummed predictions by the ratio

$$\lambda_{\alpha}^{\mathrm{HL}} = \lambda_{\alpha}^{\mathrm{PL}} \times \left(\frac{\lambda_{\alpha}^{\mathrm{HL,MC}}}{\lambda_{\alpha}^{\mathrm{PL,MC}}}\right)$$

 Shape functions, as in the work of Korchemsky, Sterman arXiv:hep-ph/9902341 where the hadron level result is given by a convolution

$$\frac{d\sigma}{d\lambda_{\alpha}^{\rm HL}} = \int d\epsilon \ f(\epsilon) \int d\lambda_{\alpha}^{\rm PL} \frac{d\sigma}{d\lambda_{\alpha}^{\rm PL}} \delta\left(\lambda_{\alpha}^{\rm HL} - \lambda_{\alpha}^{\rm PL} - C_{\alpha}^{\beta, z_{\rm cut}} \epsilon^{\gamma_{\alpha}^{\beta}}\right)$$

• Parton-to-hadron transfer matrices, see arXiv:2112.09545

$$\sigma^{\mathrm{HL}}(\vec{v}_h) = \mathcal{T}(\vec{v}_h | \vec{v}_p) \times \sigma^{\mathrm{PL}}(\vec{v}_p)$$

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- The transfer matrices can be extracted from MC simulations
- One needs to "put event generation on pause" when parton shower reach non-perturbative scale and calculate  $\lambda_{\alpha}^{\rm PL}$
- After that one "resume" event generation and calculate  $\lambda_{\alpha}^{\rm HL}$
- The correlations between  $\lambda_{\alpha}^{\rm PL}$  and  $\lambda_{\alpha}^{\rm HL}$  are used to build TMs



## Transfer matrices (TM)



- Transfer matrices were obtained with SHERPA MC
- The information on correlation between partons and hadrons in each event is embedded
- The clearly visible off-diagonal structures indicate strong bin-migration caused by non-perturbative effects
- Unlike the approach of the shape functions the TM are not bounded to any particular functional form

### TM vs. HL/PL ratio



 The approach based upon HL/PL ratio

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neglects bin migration

• Therefore, does nor provide correct shift of the distribution

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#### For the moment let's move from RHIC to CMS



#### sPHENIX detector (credit: BNL)



CMS detector (credit: CERN)

#### TM vs. HL/PL ratio vs. CMS data (ungroomed jets)



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- CMS data 2109.03340
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## And now let's get back to sPHENIX



#### sPHENIX detector (credit: BNL)



#### CMS detector (credit: CERN)

#### Main predictions: NLO+NLL'+NP results



- We corrected our NLO+NLL' results for non-perturbative effects using TM approach
- Our approach is more accurate than standard MC@NLO SHERPA simulations (SHERPA parton shower is at LL accuracy)
- Our uncertainty estimate is more accurate and includes variation of larger number of parameters
- Our results are automated and available as a resummation plugin to SHERPA



- We expect a new state of matter (called QGP) to born in AA and pA collisions
- Particles produced via hard QCD interaction and parton shower can interact with the QGP scattering centers



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- Thermalization of QGP creates a huge soft background



- There are different MC models of jet-medium interactions, e.g. HIJING, JEWEL, PQM, HYBRID, JETSCAPE, Q-Pythia, LBT...
- We used two light-weighted Pythia6 based MC models: Q-Pythia and JEWEL
- Q-Pythia: is using modified Altarelli-Parisi splitting functions (BDMPS-Z formalism)
- JEWEL: 2-to-2 rescatterings between parton shower partons and QGP scattering centers is included in parton shower evolution



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- Parton shower is unitary and hence conserves energy
- As a consequence there is no energy exchange
   between "QGP medium" and parton shower which has drastic consequences
- JEWEL, in turn, "injects" QGP particles into parton shower evolution which leads to energy exchange between QGP and parton shower









## Summary

• We obtained NLO+NLL' accuracy level results for 3 different types of jet angularities:

Les-Houches Angularity (LHA), Jet Width and Jet Thrust for both groomed and ungroomed jets. These results are automated (as a SHERPA MC plugin) and are available on request

- We found that MPI at RHIC are strongly suppressed and the non-perturbative contribution to the jet substructure is given mostly by hadronization (fragmentation) effects.
- The hadronization corrections were incorporated via transfer matrices extracted from SHERPA MC
- At RHIC hadronization causes strong bin-migration (significantly off-diagonal transfer matrices)
- Jet substructure can be used to test jet quenching models however a solid understanding of the vacuum case is required.
- The obtained AA results suggest necessity to improve the Q-Pythia model

# THANK YOU FOR LISTENING!

