

THE INITIAL STATE: OMNE INITIUM DIFFICILE EST.

Fakultät für Physik Universität Bielefeld



Oscar Garcia-Montero

- GARCIA@PHYSIK.UNI-BIELEFELD.DE







Bundesministerium für Bildung und Forschung

UNDERSTANDING QCD: COMPLEMENTARITY

EW relatively well understood Fun QCD shenanigans not fully understood in (see soft photon puzzle)

Systematic build-up of system size (complexity frontier)

Kinematics complex but some limits are simple

 $h_1 + h_2$



Clear-cut kinematics

Excellent setting to test QCD nonlinearities







THE TENOUSLY THERMAL QGP

- Heavy-Ion Collisions create a -very complicated Isolated Quantum System which is —— Initially far away from any equilibrium Self-interacting
- A system battling to thermalize against all odds.



- Expanding against the vacuum



WHAT CAN WE LEARN? FROM THE TENOUSLY THERMAL QGP

- Thermalisation How can isolated QCD systems thermalize so fast? What drives the attractor?
- OCD matter
 OCD matter
 OCD Thermodynamics
- Small Systems: What makes a fluid, a fluid?





Every endeavour we take on in HICs depends heavily on the initial assumptions of the energy and charge deposition of the models.

INITIAL CONDITIONS

As of today, I could compile a list of current, pressing avenues on the initial states

Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure

B,Q,S Charge deposition and the search for the CP

From medium to small systems

- Better quantification of ICs for large systems

Initial condition for hard probes





INITIAL CONDITIONS

As of today, I could compile a list of current, pressing avenues on the initial states

Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure B,Q,S Charge deposition and the search for the CP 🗢 From medium to small systems 🗲 - Better quantification of ICs for large systems Initial condition for hard probes









INITIAL CONDITIONS

As of today, I could compile a list of current, pressing avenues on the initial states

Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure B,Q,S Charge deposition and the search for the CP 🗢 From medium to small systems 🗲 - Better quantification of ICs for large systems Initial condition for hard probes









LET'S TAKE A LOOK FIRST AT THE LONGITUDINAL STRUCTURE





CLOSER LOOK: LONG. STRUCTURE OF SMALL SYSTEMS



The theoretical assumptions measured small system flow coeffincients are not consistent with



BOOST INVARIANCE IS...





BOOST INVARIANCE IS... NOT A GOOD APPROXIMATION*



*And this is the most averaged, coarse-grained observable we can measure!



BOOST INVARIANCE IS... NOT A GOOD APPROXIMATION





*And this is the most (





*And this is the most (



BARYON LONG. CORRS.









RAPIDITY RESOLUTION LARGE BARYON DENSITIES





HOWEVER,

ICs not well theoretically constrained around the intermediate energies

It is not fully understood which are the right initial degrees of freedom for these collisions

160

For this, models are not available along this change in $\sqrt{s_{NN}}$



10

RAPIDITY RESOLUTION LARGE BARYON DENSITIES

Baryon stopping is also seen at larger energies, leading to zones of of high n_B

Rapidity is a finer-resolution probe of the critical regime than $\sqrt{s_{NN}}$ for the LHC Run3 upgrade

[Brewer et. al., PRC 98, 061901 (2018)]

At higher energies (LHC) the -midrapiditymuch better constrained

A robust extension to 5D may result in a smaller uncertainty in large- μ_B observables.



11

RAPIDITY RESOLUTION LARGE BARYON DENSITIES

Baryon stopping is also seen at larger energies, leading to zones of of high $n_{\!B}$

Rapidity is a finer-resolution probe of the critical regime than $\sqrt{s_{NN}}$ for the LHC Run3 upgrade

[Brewer et. al., PRC 98, 061901 (2018)]

At higher energies (LHC) the -**midrapidity**- ICs are much better constrained

A robust extension to 3D may result in a smaller uncertainty in large- μ_B observables.







We need a well controlled 3D initial energy, and charge (BQS) deposition to initialise -precision physics era- EbE simulations

THE INITIAL STATE OF A HIC

What do we need?

IC is commonly taken to be up to the beginning of hydro evolution.

Then, the initial energy stress tensor, $T_{0, \text{hydro}}^{\mu\nu}$, is needed.







THE INITIAL STATE OF A HIC ... IN 3D.

What do we expect to have?

Nature of DoFs depends model-by-model

(1) Fireball energy deposition: C.o.M of collision favours midrapidity.

- High density of gluons, string breaking, etc.





THE INITIAL STATE OF A HIC ... IN 3D.

What do we expect to have?

Nature of DoFs depends model-by-model

(1) Fireball energy deposition: C.o.M of collision favours midrapidity.

- High density of gluons, string breaking, etc.

Quark scattering, baryon junction, hadrons?



(2B)





THE INITIAL STATE OF A HIC ... IN 3D.

What do we expect to have?

- Nature of DoFs depends model-by-model
- (1) Fireball energy deposition: C.o.M of collision favours midrapidity.
 - High density of gluons, string breaking, etc.
 - - Ouark scattering, baryon junction, hadrons? -



(2) Fragmentation region energy deposition: C.o.M of collision favours midrapidity.

(2) Fragmentation region charge deposition: Q,B and S (in fluctuations)



SO, WHERE ARE WE? WHAT IS THERE? AND... WHAT IS MISSING?

METHODS: STATE OF THE ART DoFs/motivation behind the energy and charge deposition



Collinear fact. Described by PDFs



Effective description Often parametrical

GEOMETRICAL



Overoccupied Color fields



METHODS: STATE OF THE ART DoFs/motivation behind the energy and charge deposition

LARGE-X

Collinear fact. Described by PDFs

AMPT, EKRT (Next Talk!)

Effective description Often parametrical

TRENTO

GEOMETRICAL

LOW-X

Overoccupied Color fields



METHODS: STATE OF THE ART DoFs/motivation behind the energy and charge deposition



Collinear fact. Described by PDFs



Effective description Often parametrical

GEOMETRICAL





DEEPLY INELASTIC SCATTERING (DIS)



- Using QED probe to test QCD properties
- Great control over kinematics



- Inclusive and exclusive channels (vector meson prod.,DVCS, etc)
- Great control over kinematics



NUCLEAR STRUCTURE

• PDFs from fit to Experiments (DIS) *x* ~ energy/momentum fraction carried by parton $Q^2 \sim$ resolution scale







NUCLEAR STRUCTURE

• PDFs from fit to Experiments (DIS) $x \sim \text{energy/momentum fraction carried by parton}$ $Q^2 \sim$ resolution scale

OCD evolution in Q^2 given by the DGLAP equation

X



NUCLEAR STRUCTURE

• PDFs from fit to Experiments (DIS) $x \sim \text{energy/momentum fraction carried by parton}$ $Q^2 \sim \text{resolution scale}$

• OCD evolution in Q^2 given by the DGLAP equation

• OCD non-linear evolution in x given by the BK equation





NUCLEAR STRUCTURE

• PDFs from fit to Experiments (DIS) $x \sim \text{energy/momentum fraction carried by parton}$ $Q^2 \sim$ resolution scale

OCD evolution in Q^2 given by the DGLAP equation

OCD non-linear evolution in x given by the BK equation

Balance between gluon emission and recombination leads t saturation of the gluon density (black disk limit $N \sim 1$)







NUCLEAR STRUCTURE

• Emergence of a *semi-hard* saturation scale Q_s is created dynamically

- \bullet Gluon distributions saturate with $k_{\perp} < Q_S$ $(r > Q_S^{-1}$ in pos. space)
- Parametrically, an simple form

With energy: $Q_S \sim x^{-\lambda}$

With system size

 $Q_{S} \sim A^{1/3}$






Soft Partons

Macroscopic Field A(x)





THE COLOR GLASS CONDENSATE GLUE Hard Partons **Soft Partons** Macroscopic Field Static Color Sources Q_s $J^{\mu}(x) = g \,\delta(x^{-}) \,\delta^{\mu+} \,\rho(\mathbf{x}_{\perp})$ A(x) $[D_{\mu},F^{\mu\nu}]=J^{\nu}$ Yang-Mills Equations $A_p^{\mu}(x) = -g \,\delta^{\mu +} \,\delta(x^{-}) \frac{1}{\nabla_{\perp}^2} \,\rho(\mathbf{x}_{\perp})$



THE COLOR GLASS CONDENSATE GLUE **Soft Partons** Hard Partons Static Color Sources Q_s $J^{\mu}(x) = g \,\delta(x^{-}) \,\delta^{\mu +} \,\rho(x_{\perp})$ A(x) $[D_{\mu}, F^{\mu\nu}] = J^{\nu}$ Yang-Mills Equations $A_p^{\mu}(x) = -g \,\delta^{\mu +} \,\delta(x^{-}) \frac{1}{\nabla_{\perp}^2} \,\rho(\mathbf{x}_{\perp})$ $\frac{\alpha_s}{Q_S^2(x)} \frac{x f_g(x, Q_S^2)}{\pi R^2} \sim 1$

Macroscopic Field





Soft Partons

Macroscopic Field

A(x)

 $W[x; \rho]$: gauge invariant probability distribution





Soft Partons

Macroscopic Field

A(x)



 $W[x; \rho]$: gauge invariant probability distribution

SPECIAL CASE

McLerran-Venugopalan Model

 $\langle \rho^a(\mathbf{x}_{\perp}) \rho^b(\mathbf{y}_{\perp}) \rangle = g^2 \,\delta^{ab} \,\mu^2 \delta^{(2)}(\mathbf{x}_{\perp} - \mathbf{y}_{\perp})$



SATURATION: IP-GLASMA

LO approximation for the CGC evolution of a dense-dense system.

IP-GLASMA

1) Sample nucleon positions (e.g. MC-Glauber) 2) Sample color currents from those nucleons $(J_{A,B})$ 3) Solve Yang-Mills in the presence of both currents and conservation laws for currents.

4) Get energy-stress tensor, $T^{\mu\nu}$

NOTE: EXTENSION TO **3D IS NOT TRIVIAL**



LOW-X





27

RAPIDITY RESOLUTION \leftrightarrow LONG. RESOLUTION LONGITUDINAL STRUCTURE





$q(\boldsymbol{p}, y)$

PERTURBATIVE CASE

Perturbative expansion on the sources allows simple kinematics, connection $x \leftrightarrow y$ straightforward

COMPLETE LO CASE

Every contribution of sources taken on account, solvable numerically, but connection $x \leftrightarrow y$ is very complex



SATURATION: 3D-IP-GLASMA

1) Sample nucleon positions (e.g. MC-Glauber)







SATURATION: 3D-IP-GLASMA

LO approximation for the CGC evolution of a dense-dense system.

IP-GLASMA 3+1D (V2)

1) Sample nucleon positions (e.g. MC-Glauber) 2) Sample color currents from those nucleons $(J_{A,B})$ but now your nuclei have an extent in z (more accurate in x^{\pm})

4) Solve Yang-Mills in 3+1D

5) Get $T^{\mu\nu}$ and evolution



[*Phys.Rev.D* 103 (2021) 1, 014003]









CGC IN 3D: THE MCDIPPER

Framework for comparison of saturation model predictions and creation of IC for HE Heavy-Ion Collisions

Perturbative realisation of the LO glasma graph + Baryon stopping by CGC



Monte-Carlo Dipole Parallel Event GeneRator





FROM MICRO TO MACRO

Low-x gluons dominate the midrapidity region

$$\frac{dN_g}{d^2 x d^2 p dy} = \frac{g^2}{8\pi^5 C_F p^2} \int \frac{d^2 q}{(2\pi)^2} \frac{d^2 k}{(2\pi)^2} (2\pi)^2 \delta(p+q-p) \times \Phi_1(x_1, x, q) \Phi_2(x_2, x, k)$$

- At forward/backward rapidities, particle production dominated by baryon stopping

$$\frac{dN_{q_f}}{d^2 \mathbf{x} d^2 \mathbf{p} dy} = \frac{x_1 q_f^A(x_1, \mathbf{p}^2, \mathbf{x}) \ D_{\text{fun}}(x_2, \mathbf{x}, \mathbf{p})}{(2\pi)^2} + \frac{x_2 q_f^A(x_2, \mathbf{p}^2, \mathbf{x}) \ D_{\text{fun}}(x_1, \mathbf{x}, \mathbf{p})}{(2\pi)^2}$$

Systematically Improvable e.g. by including NLO $gg \rightarrow q\bar{q}$ production through gluon fusion

CONSERVED CHARGE DEPOSITION FROM THE CGC FORMALISM







CGC IN 3D: THE MCDIPPER

Framework for comparison of saturation model predictions and creation of IC for HE Heavy-Ion Collisions

HOW DOES IT WORK?

• Model input: gluon unintegrated distribution functions: (uGDF) + (collinear) parton distribution functions (PDFs)

Gluon production: k_1 factorization ~ UGD²

Quark production hybrid formalism ~ PDF \otimes UGD

 η, T_1, T_2 Compute energy and charges using single particle production formulas and tabulate (η, T_1, T_2)

• Use Glauber sampling to produce events -fast- using (η, T_1, T_2) as an EbE input.

[GM, Schlichting, Elfner, PRC 109 (2024) 4, 044916]

Monte-Carlo Dipole Parallel Event GeneRator





$$(B\tau)_0 = \sum_f B_f \int d^2 \mathbf{p} \left[\frac{dN_f}{d^2 \mathbf{x} d^2 \mathbf{p} dy} - \frac{dN_{\bar{f}}}{d^2 \mathbf{x} d^2 \mathbf{p} dy} \right]$$

TUNING **FIXING THE K-FACTOR** Input model parameters can be fixed by other experiments e.g. DIS (e+p, e+A,...) - Overall normalisation of $(e_g \tau)_0$ treated as a free parameter, K_{g} , to account for perturbative corrections - Tune K_g using E_{\perp} in pp min. bias collisions at $\sqrt{s_{NN}} = 5.02 \,\text{TeV}$ $K_g = 1.25 \{\text{GBW}\}$ $K_g = 1.85 \ \{\text{IP-Sat}\}$ - Multiplicity can be then estimated using $\left\langle \frac{\mathrm{d}N_{\mathrm{ch}}}{\mathrm{d}y} \right\rangle = \frac{4}{3} \frac{N_{\mathrm{ch}}}{S} C_{\infty}^{3/4} \left(4\pi \frac{\eta}{s} \right)^{1/3} \left(\frac{\pi^2}{30} \nu_{\mathrm{eff}} \right)^{1/3} \int \mathrm{d}^2 \mathbf{x} \left[\tau e(y, \mathbf{x}) \right]_0^{2/3}$

[PRL. 123, 262301]





CHARGE DEPOSITION

- Non-trivial interaction between x-dependence of gluon uGDs and quark PDFs gives tails in the charge deposition

Even at higher rapidities, non-zero baryon stopping is found!



(see PRC 108 (2023) 4, 4)



CHARGE DEPOSITION

 Non-trivial interaction between x-dependence of gluon uGDs and quark PDFs gives tails in the charge deposition

Even at higher rapidities, non-zero baryon stopping is found!

Midrapidity baryon charge deposition follows an exponential shift in the rapidity shift

$$\frac{\mathrm{dB}}{\mathrm{d}\eta} \bigg|_{\eta=0} \sim e^{-\alpha_B y_{\text{beam}}} \quad \text{with} \quad y_{\text{beam}} \approx \frac{1}{2} \log \left[\frac{\sqrt{2}}{n} \right]_{\eta=0}$$





THE MCDIPPER+CLVISC SOME INTERESTING RESULTS (...TO ME)



Minimal IC tuning.

[GM, Schlichting, Zhu, in preparation]



Added hotspot fluctuations



THE MCDIPPER+CLVISC SOME INTERESTING RESULTS (...TO ME)



Decorrelation due to non-trivial *x*-dependence of uGHs and PDFs

Additional fluctuations needed to explain flow decorrelation. WIP: charge fluctuations in the valence sector (PDF sampling of valence charges)

[GM, Schlichting, Zhu, in preparation]



Consistency is key.

We should strive to use IC models in HICs that can model and describe simultaneously collisions for smaller systems (e+A, p+A).

THE ELECTRON-ION COLLIDER





CORE IDEAS OF THE EIC

How are quarks and gluons, and their spins, **distributed in space and momentum** inside the nucleon?



How do **color charges**, (and colorless jets) interact with a **nuclear medium?**







SYNERGIES LHC-EIC

CHALLENGES IN ICs-HICS • Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure - *B,Q,S* Charge deposition and the search for the CP From medium to small systems Better quantification of ICs for large systems Initial condition for hard probes

CORE IDEAS OF THE EIC

How are quarks and gluons, and their spins, **distributed in space and momentum** inside the nucleon?



B

How do **color charges**, (and colorless jets) interact with a **nuclear medium?**







SYNERGIES LHC-EIC

CHALLENGES IN ICS-HICS

- Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure
- B,Q,S Charge deposition and the search for the CP
- From medium to small systems
- Better quantification of ICs for large systems

Initial condition for hard probes

CORE IDEAS OF THE EIC

How are quarks and gluons, and their spins, **distributed in space and momentum** inside the nucleon?



How do **color charges**, (and colorless jets) interact with a **nuclear medium?**

Does gluon density **saturate at high energies in nuclei**? Is this a universal property in all nuclei, even the **proton**?





SYNERGIES LHC-EIC

CHALLENGES IN ICS-HICS

- Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure
- B,Q,S Charge deposition and the search for the CP
- From medium to small systems
- Better quantification of ICs for large systems
- Initial condition for hard probes

CORE IDEAS OF THE EIC

How are quarks and gluons, and their spins, **distributed in space and momentum** inside the nucleon?

How do **color charges**, (and colorless jets) interact with a **nuclear medium?**

Does gluon density **saturate at high energies in nuclei**? Is this a universal property in all nuclei, even the **proton**?



B

44

CHALLENGES IN ICS-HICS

- Initial condition: $\sqrt{s_{NN}}$ dependence and longitudinal structure
- B,Q,S Charge deposition and the search for the CP
- From medium to small systems
- Better quantification of ICs for large systems
- Initial condition for hard probes

CORE IDEAS OF THE EIC

How are quarks and gluons, and their spins, **distributed in space and momentum** inside the nucleon?

How do **color charges**, (and colorless jets) interact with a **nuclear medium?**

Construction of the second sec



B



TESTING SATURATION MODELS





TESTING SATURATION MODELS





TESTING SATURATION MODELS





TESTING SATURATION MODELS A DIPOLE STORY

• Inclusive DIS cross-section:

$$\sigma_{T,L}^{\gamma^*A} = \sum_{f} \int d^2 \mathbf{b} d^2 \mathbf{r} dz \left| \psi_{T,L}^{\gamma^* \to q\bar{q}}(\mathbf{r}, z, Q^2) \right|^2 N(\mathbf{b}, \mathbf{r})$$

• Can be expressed as a function of structure functions, e.g.

$$e^{2}F_{2}(x,Q) = Q^{2} \left(\sigma_{T}^{\gamma}\right)$$
$$e^{2}F_{L}(x,Q) = Q^{2}\sigma_{L}^{\gamma^{*}A}$$

 \bullet Compare linear DGLAP and non-linear BK effects in $F_{2,L}$

How? Expanding $N(\mathbf{b}, \mathbf{r}, x)$ and matching

[Phys.Rev.D 105 (2022) 11, 114017]

F_i difference(%) (¹⁹⁷Au)





HADRON CORRELATIONS

- The semi-inclusive channel $e + A \rightarrow h_1 + h_2 + e' + X$ is quite sensitive
- Multiple scatterings with the soft gluons within the target serve to broaden the back-to-back peak for outgoing particles
 - When the relative momentum $q_{\perp} \sim Q_{s'}$ interacting $q\bar{q}$ feels maximally the saturated glue.
- Also, photon-hadron/photon jet should be sensitive to saturation effects.
- Progress towards NLO: [Caucal et al, arXiv:2405.19404]





Coherent: Fully diffractive

 $e + A \rightarrow e + A + J/\psi$

Incoherent: Breaks up the nucleus.

 $e + A \rightarrow e + (A' + X) + J/\psi$







Coherent: Fully diffractive Incoherent: Breaks up the nucleus.

 $e + A \rightarrow e + A + J/\psi$

 $e + A \rightarrow e + (A' + X) + J/\psi$

Coherent: Sensitive to average geometry
Diffractive peaks → details of target, non-linearities, etc.





Coherent: Fully diffractive

Incoherent: Breaks up the nucleus.

 $e + A \rightarrow e + A + J/\psi$ $e + A \rightarrow e + (A' + X) + J/\psi$

 Coherent: Sensitive to average geometry Diffractive peaks \rightarrow details of target, non-linearities, etc.

 Incoherent: Sensitive to EbE fluctuations Sensitive to nuclear structure







Coherent: Fully diffractive $e + A \rightarrow e + A + J/\psi$

Incoherent: Breaks up the nucleus.

 $e + A \rightarrow e + (A' + X) + J/\psi$

Coherent: Sensitive to average geometry Diffractive peaks \rightarrow details of target, non-linearities, etc.

 Incoherent: Sensitive to EbE fluctuations Sensitive to nuclear structure

> Ab initio computations of nuclear densities can help include **nucleonic** *n*-point correlations into initial geometry









[PRL 131 (2023) 6, 062301]





Coherent: Fully diffractive $e + A \rightarrow e + A + J/\psi$

Breaks up the nucleus.

 $e + A \rightarrow e + (A' + X) + J/\psi$

 Coherent: Sensitive to average geometry Diffractive peaks \rightarrow details of target, non-linearities, etc.

 Incoherent: Sensitive to EbE fluctuations Sensitive to nuclear structure

> Ab initio computations of nuclear densities can help include **nucleonic** *n*-point correlations into initial geometry

Flanking from both LHC and EIC?







Nuclear structure and flow










SUMMARY AND CONCLUSIONS

Many models. We need also a way to discriminate models of the initial stages.

Necessary: Models should establish themselves *conceptually* (if not computationally) consistent throughout wide range of energies and systems.

Exciting Future: The EIC poses as an excellent complement to the HICs program. The ICs can be refined using its measurements.

3D is now. Understanding the longitudinal structure of the initial energy deposition is a necessity for the studies on small systems



CHARGE DEPOSITION

- Non-trivial interaction between x-dependence of gluon uGDs and quark PDFs gives tails in the charge deposition

Even at higher rapidities, non-zero baryon stopping is found!

Midrapidity baryon charge deposition follows a power-law trend

$$\frac{\mathrm{dB}}{\mathrm{d}\eta} \bigg|_{\eta=0} \sim \left(\sqrt{s_{NN}}\right)^{\alpha}$$

10⁵ 30 - 40% 0-5% 5 – 10% 40 - 50% ··•· 60 – 70% 10 - 20% 104 20 – 30% •• 70 - 80% 10³ Charge $B_{\Lambda_{\pi}}$ 10² Baryon 10^{1} Deposited 10 10^{-} 10^{-2} 10^{-3} 10² 10³ $\sqrt{s_{\rm NN}}$ (GeV)





 $dB/d\eta_{s}$

CHARGE DEPOSITION

- Non-trivial interaction between x-dependence of gluon uGDs and quark PDFs gives tails in the charge deposition

Even at higher rapidities, non-zero baryon stopping is found!



[GM, Schlichting, Elfner, PRC 109 (2024) 4, 044916]

13

CHARGE DEPOSITION

- Non-trivial interaction between x-dependence of gluon uGDs and quark PDFs gives tails in the charge deposition

Even at higher rapidities, non-zero baryon stopping is found!



(see PRC 108 (2023) 4, 4)



3D-TRENTO

Parametrical model of energy deposition of the HIC

Extension to 3D, TRENTo includes a central fireball and forward and backward fragmentation regions.

$$\epsilon(\mathbf{x}, \eta) = \epsilon_{\rm fb}(\mathbf{x}, \eta) + \epsilon_{\rm frag, +}(\mathbf{x}, \eta) + \epsilon_{\rm frag, -}(\mathbf{x}, \eta)$$

Central fireball is parametrized in rapidity

 $\varepsilon_{\rm fb}(\vec{x}_{\perp},\eta_s) = N_{\rm fb} \ \sqrt{T_A(\vec{x}_{\perp})} \ T_B(\vec{x}_{\perp}) \ f_{\rm fb}(\eta_s - \eta_{s,\rm cm}(x_{\perp})),$

GEOMETRICAL

[PRC 102 (2020)]

Plateau-fitting of the fireball







16

3D-TRENTO

Parametrical model of energy deposition of the HIC

Extension to 3D, TRENTo includes a central fireball and forward and backward fragmentation regions.

$$\epsilon(\mathbf{x}, \eta) = \epsilon_{\rm fb}(\mathbf{x}, \eta) + \epsilon_{\rm frag, +}(\mathbf{x}, \eta) + \epsilon_{\rm frag, -}(\mathbf{x}, \eta)$$

Central fireball is parametrized in rapidity

 $\varepsilon_{\rm fb}(\vec{x}_{\perp},\eta_s) = N_{\rm fb} \ \sqrt{T_A(\vec{x}_{\perp}) \ T_B(\vec{x}_{\perp})} \ f_{\rm fb}(\eta_s - \eta_{s,\rm cm}(x_{\perp})),$

Fragmentation deposition is constrained by *limiting* fragmentation

$$arepsilon_{\mathrm{frag},X}(ec{x}_{\perp},\eta_s) = rac{k_{\mathrm{T,min}}}{N_{\mathrm{frag}}} F_X(ec{x}_{\perp}) f_{\mathrm{frag}}(e^{-\eta_{s,\mathrm{max}}\pm ec{x}_{\perp}})$$

GEOMETRICAL

[PRC 102 (2020)]



 $^{\perp \eta_{s}})$



16

3D-TRENTO

Parametrical model of energy deposition of the HIC

Extension to 3D, TRENTo includes a central fireball forward and backward fragmentation regions.

$$\epsilon(\mathbf{x}, \eta) = \epsilon_{\rm fb}(\mathbf{x}, \eta) + \epsilon_{\rm frag, +}(\mathbf{x}, \eta) + \epsilon_{\rm frag, -}(\mathbf{x}, \eta)$$

Central fireball is parametrized in rapidity

 $\varepsilon_{\rm fb}(\vec{x}_{\perp},\eta_s) = N_{\rm fb} \ \sqrt{T_A(\vec{x}_{\perp})} \ T_B(\vec{x}_{\perp}) \ f_{\rm fb}(\eta_s - \eta_{s,{
m cm}}(x_{\perp}))$

Fragmentation deposition is constrained by limiting fragmentation

$$arepsilon_{\mathrm{frag},X}(ec{x}_{\perp},\eta_s) = rac{k_{\mathrm{T,min}}}{N_{\mathrm{frag}}} F_X(ec{x}_{\perp}) f_{\mathrm{frag}}(e^{-\eta_{s,\mathrm{max}}\pm ec{x}_{\perp}})$$

GEOMETRICAL

[PRC 102 (2020)]



 $^{ \scriptscriptstyle \perp \eta_s})$

No charge deposition. Useful for bayesian analysis



