



# Scalable Quantum Circuits for Confining Theories - Simulating the Schwinger Model using more than 100 qubits and One Trillion CNOT Gates

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Scalable Circuits for Preparing Ground States on Digital Quantum Computers: The Schwinger Model Vacuum on 100 Qubits

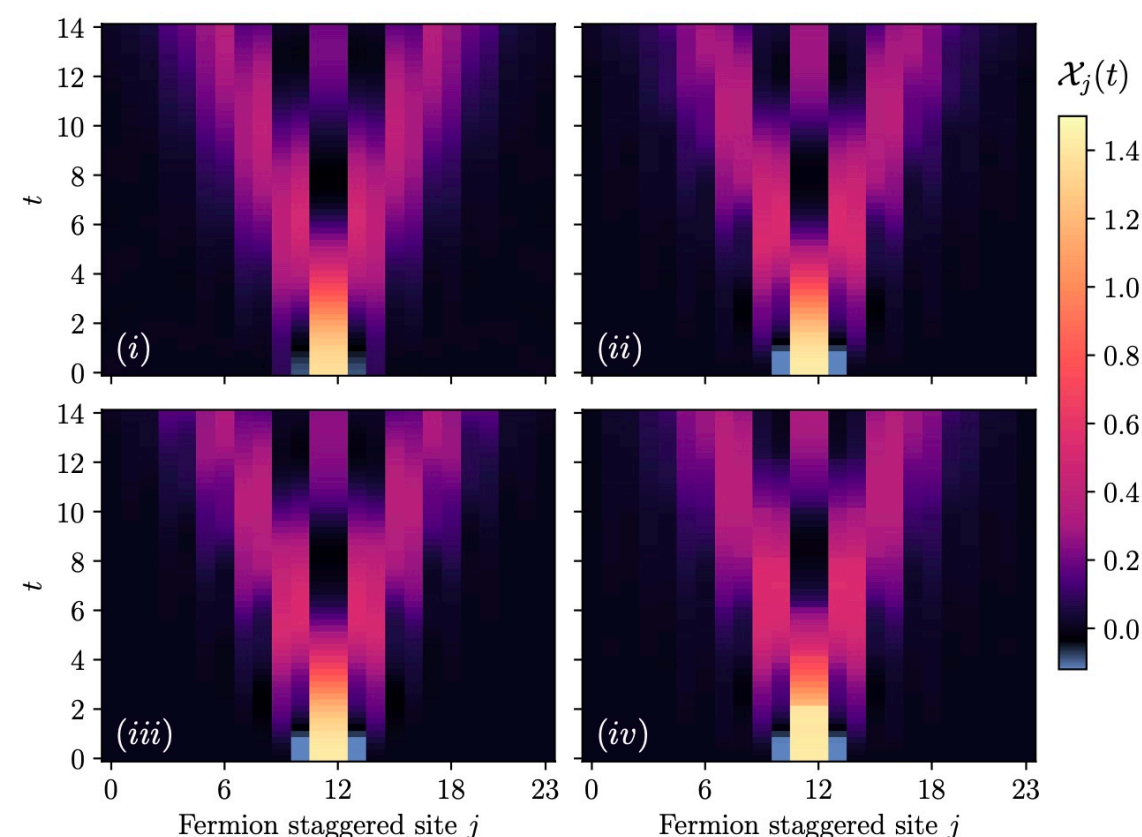
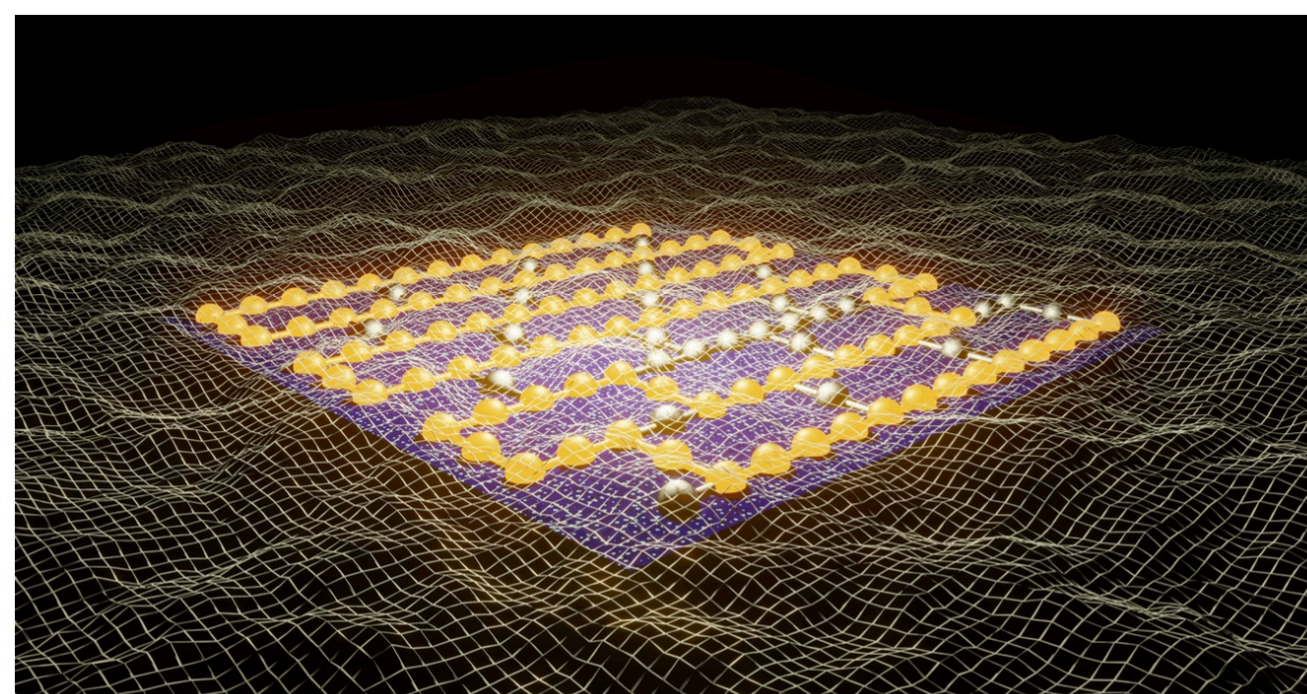
Roland C. Farrell, Marc Illa, Anthony N. Ciavarella, and Martin J. Savage  
PRX Quantum **5**, 020315 – Published 18 April 2024

**PHYSICAL REVIEW D**  
covering particles, fields, gravitation, and cosmology

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Quantum simulations of hadron dynamics in the Schwinger model using 112 qubits

Roland C. Farrell, Marc Illa, Anthony N. Ciavarella, and Martin J. Savage  
Phys. Rev. D **109**, 114510 – Published 10 June 2024



Roland Farrell, Marc Illa, Anthony Ciavarella and Martin Savage  
InQubator for Quantum Simulation (IQUS), University of Washington

INT 15 October 2024



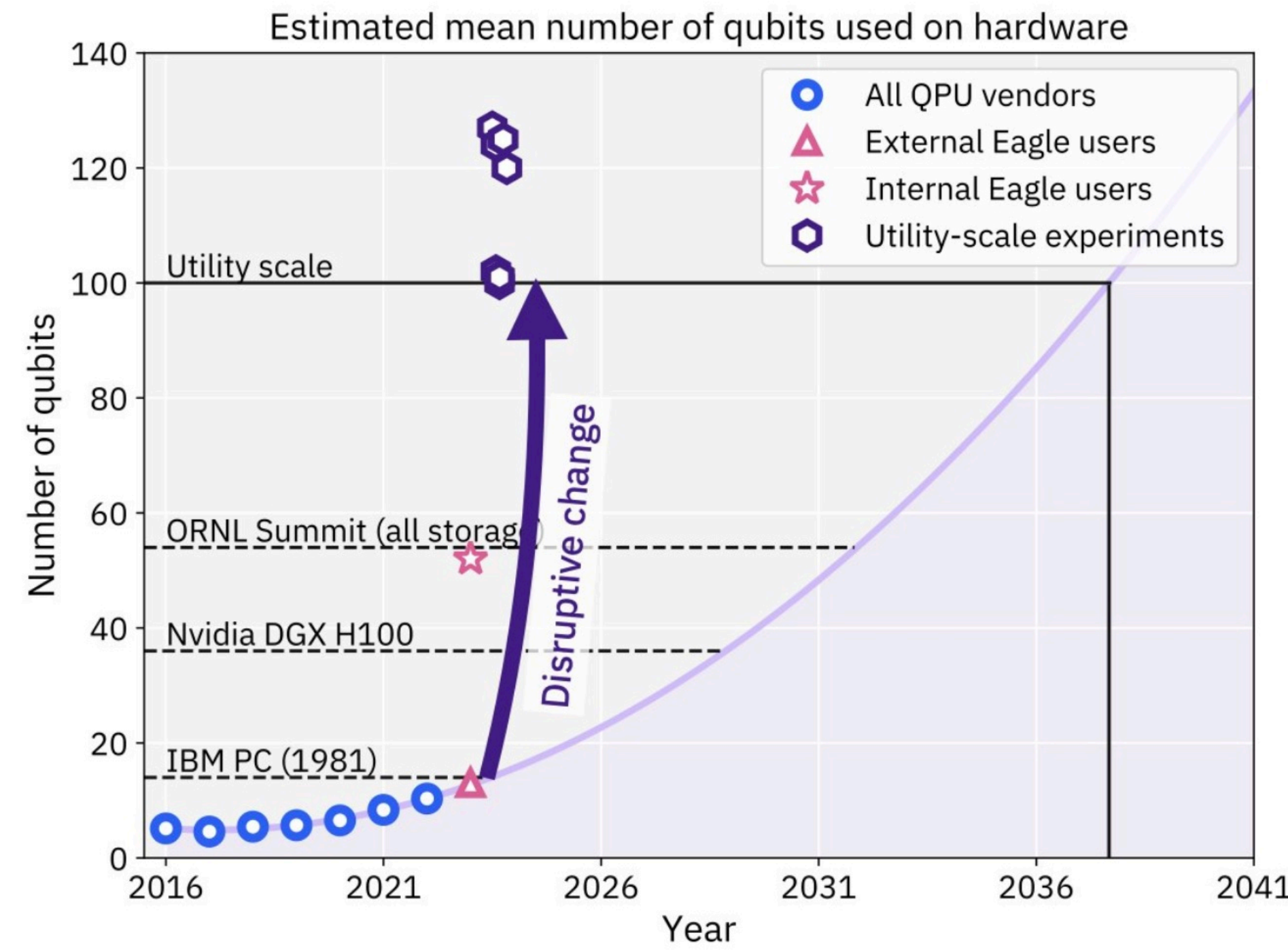
# IBM Quantum Summit - NYC December 2023



Jay Gambetta  
IBM Fellow & VP  
IBM Quantum

## Utility-scale experiments

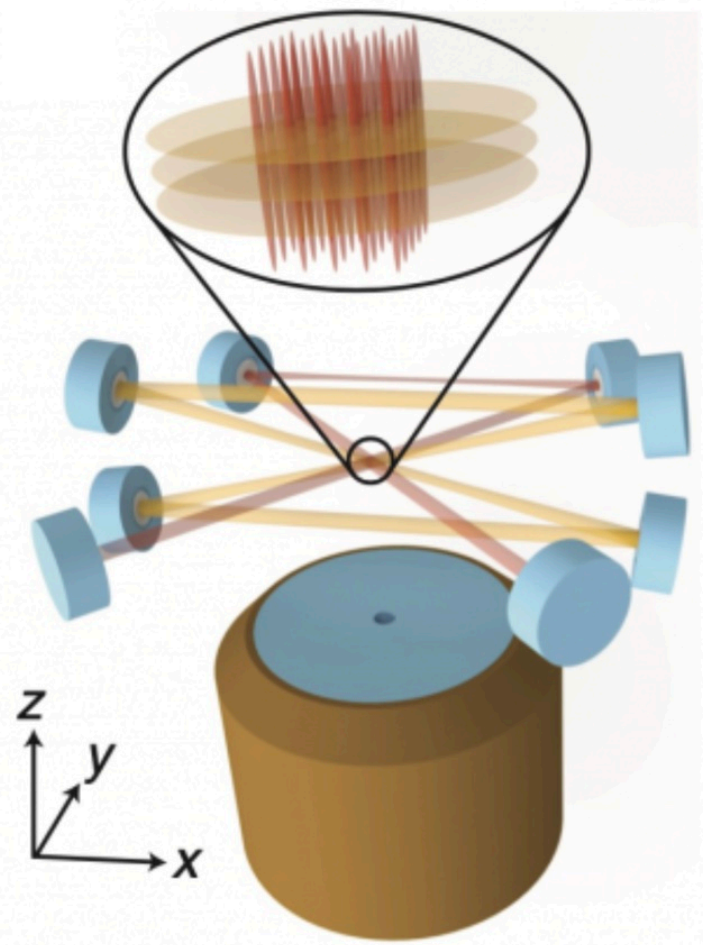
With quantum systems composed of 100+ qubits, researchers are beginning to explore algorithms and applications at scales beyond brute-force classical computation [using IBM Quantum systems](#).



IBM Quantum

- Evidence for the utility of quantum computing before fault tolerance**  
[127 qubits / 2880 CX gates](#)      Nature, 618, 500 (2023)
- Simulating large-size quantum spin chains on cloud-based superconducting quantum computers**  
[102 qubits / 3186 CX gates](#)      arXiv:2207.09994
- Uncovering Local Integrability in Quantum Many-Body Dynamics**  
[124 qubits / 2641 CX gates](#)      arXiv:2307.07552
- Realizing the Nishimori transition across the error threshold for constant-depth quantum circuits**  
[125 qubits / 429 gates + meas.](#)      arXiv:2309.02863
- Scalable Circuits for Preparing Ground States on Digital Quantum Computers: The Schwinger Model Vacuum on 100 Qubits**  
[100 qubits / 788 CX gates](#)      arXiv:2308.04481
- Efficient Long-Range Entanglement using Dynamic Circuits**  
[101 qubits / 504 gates + meas.](#)      arXiv:2308.13065
- Quantum reservoir computing with repeated measurements on superconducting devices**  
[120 qubits / 49470 gates + meas.](#)      arXiv:2310.06706

# Select Recent Advances in Quantum Computing



Cold-Atom arrays with Optical Tweezers



4 Logical Qubits  
32-qubit H2-1 trapped ions  
(Quantinuum-Microsoft)

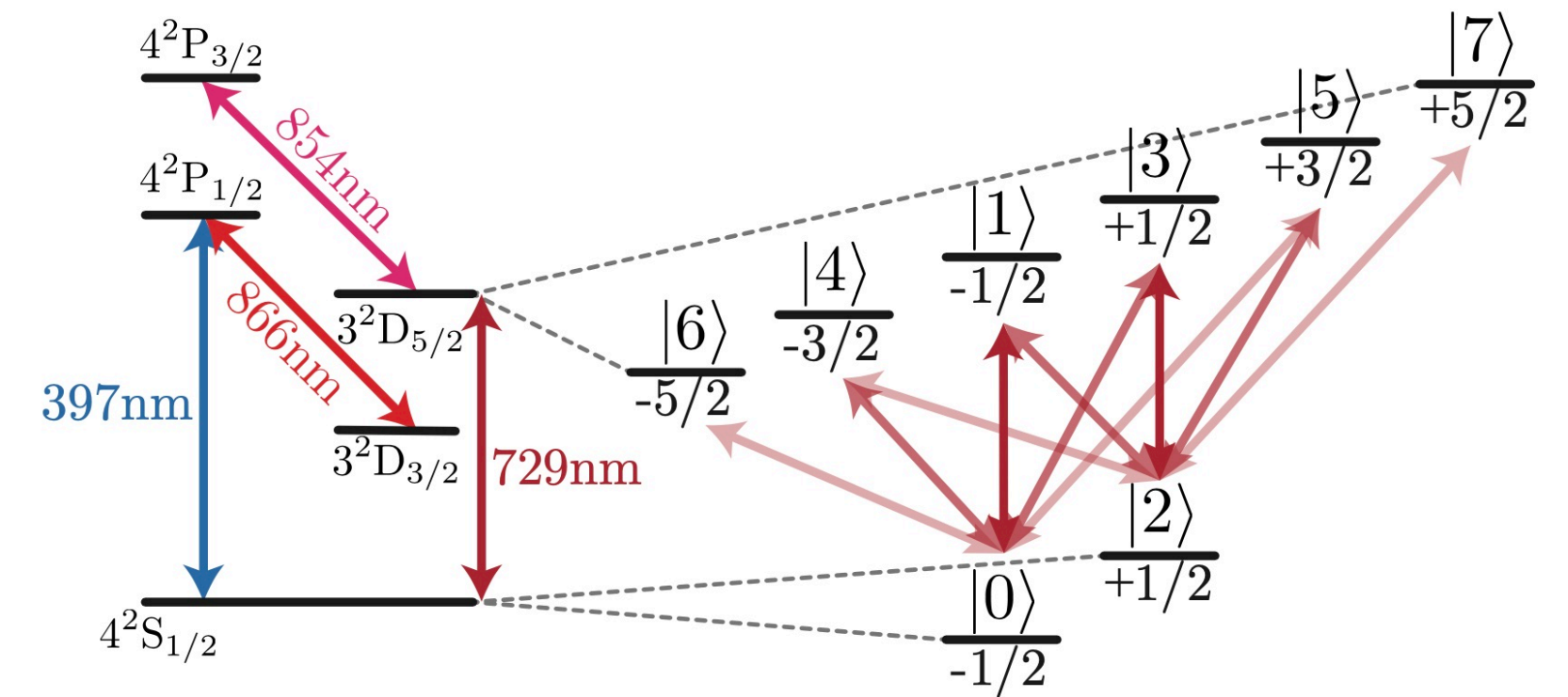
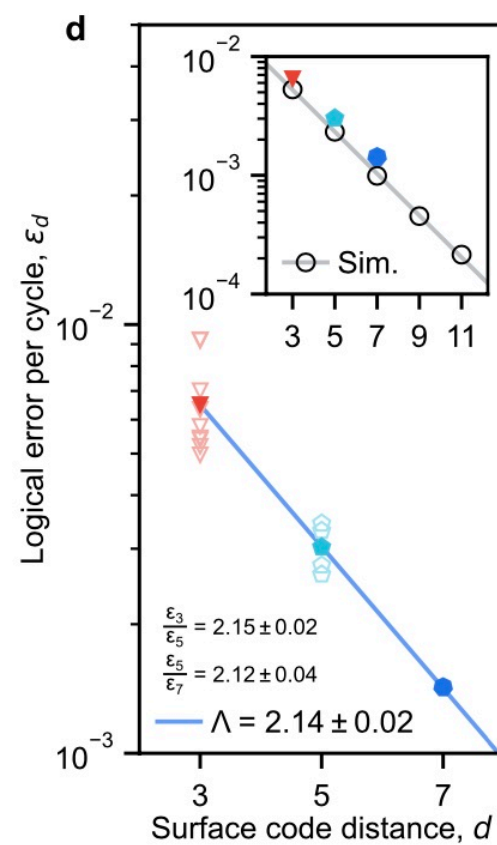
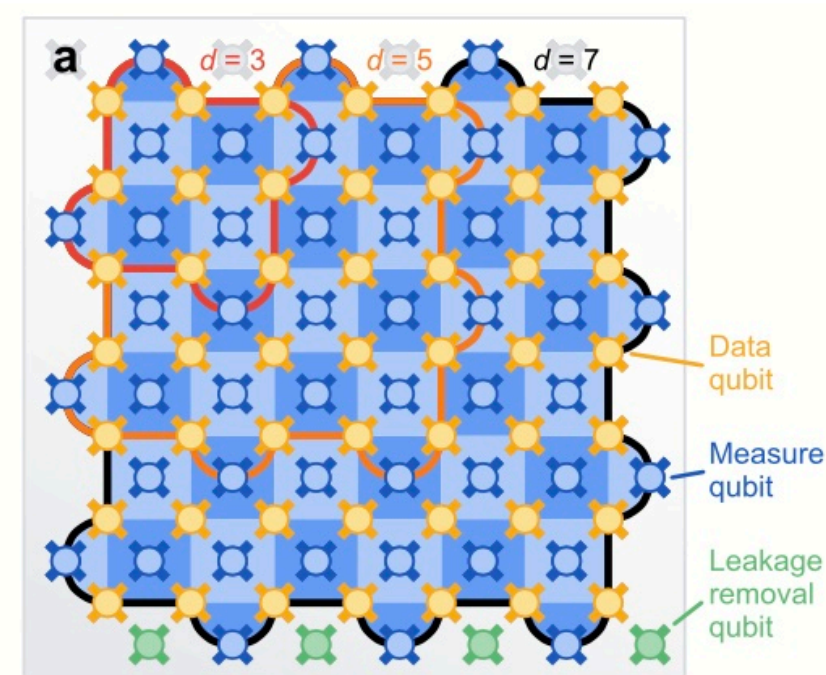
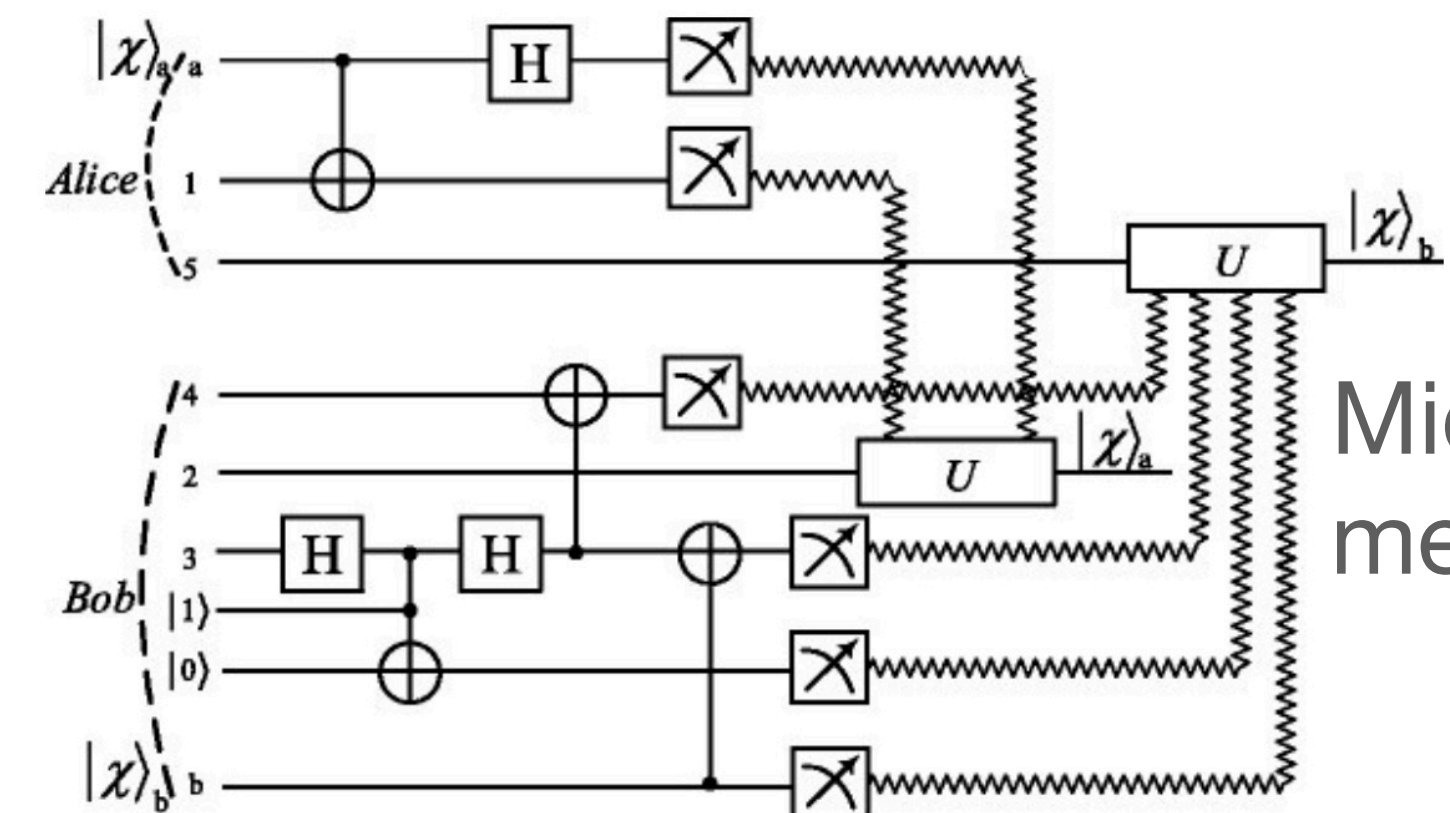


FIG. 1. Level scheme of the  $^{40}\text{Ca}^+$  ion.

Qudits with trapped ions

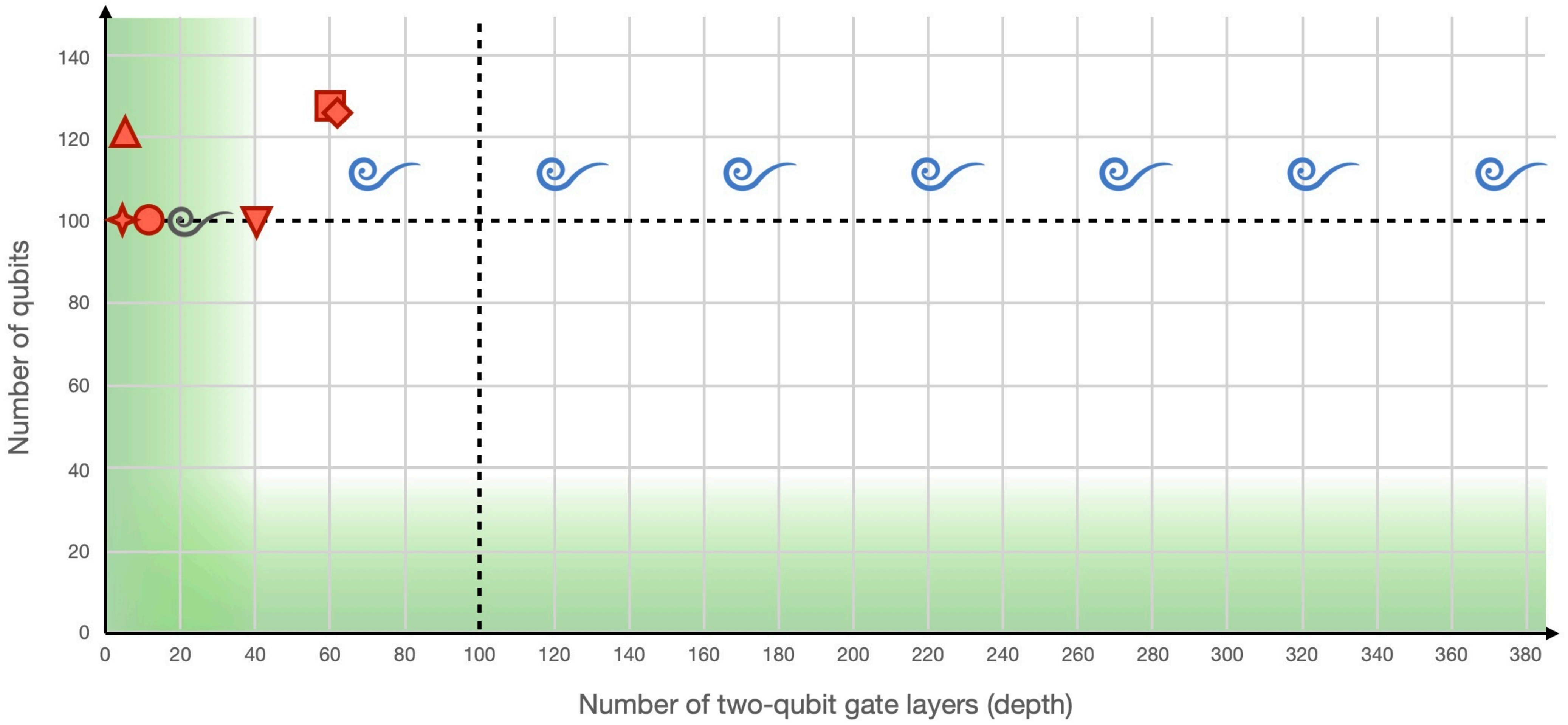


Surface code  
>100 superconducting qubits



Mid-circuit measurements

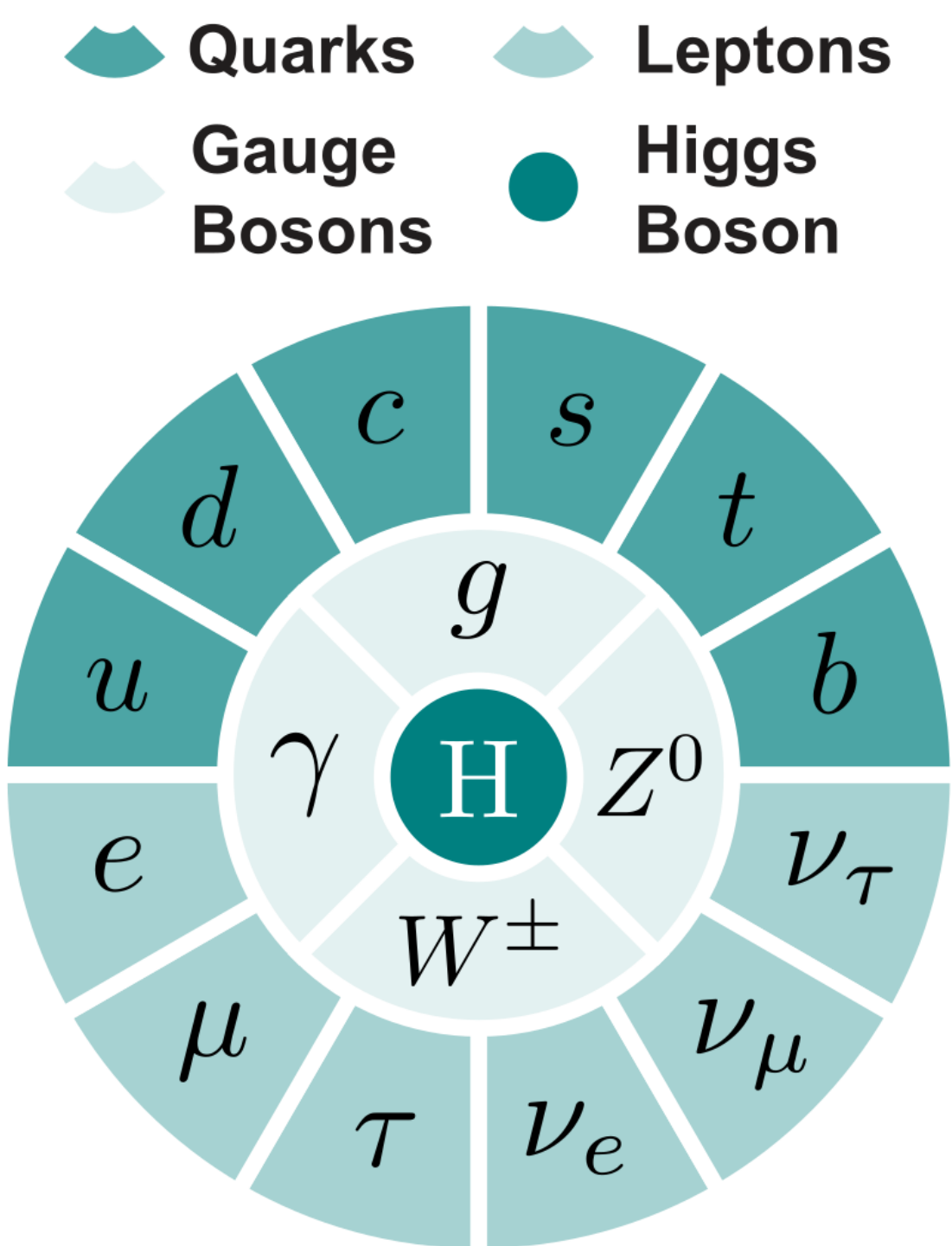
- Yu, Zhao, Wei, PRR 5 (2023)
- ◻ Kim et al., Nature (2023)
- ▲ Chen et al., arXiv:2309.02863 (2023)
- ◆ Shtanko, Wang, Zhang, Harle, Seif, Movassagh, Mineev, arXiv:2307.07552 (2023)
- ✦ Bäumer, Tripathi, Wang, Rall, Chen, Majumder, Seif, Mineev, arXiv:2308.13065 (2023)
- ▼ Liao, Wang, Sitdikov, Salcedo, Seif, Mineev, arXiv:2309.17368 (2023)
- 🌀 Farrell, Illa, Ciavarella, Savage, arXiv: 2308.04481 (2023)
- 🌀 Farrell, Illa, Ciavarella, Savage, arXiv:2401.08044 (2024)



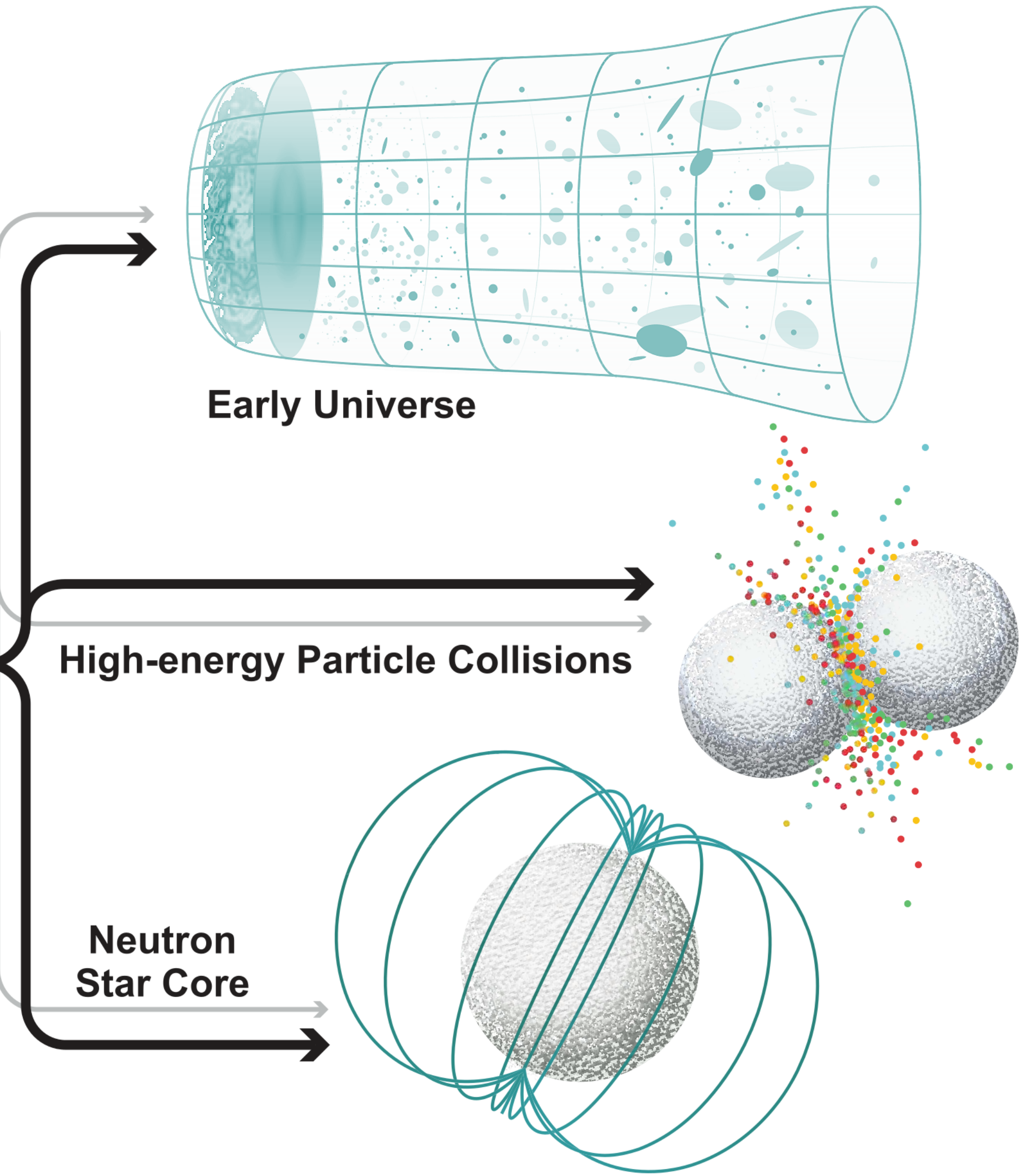
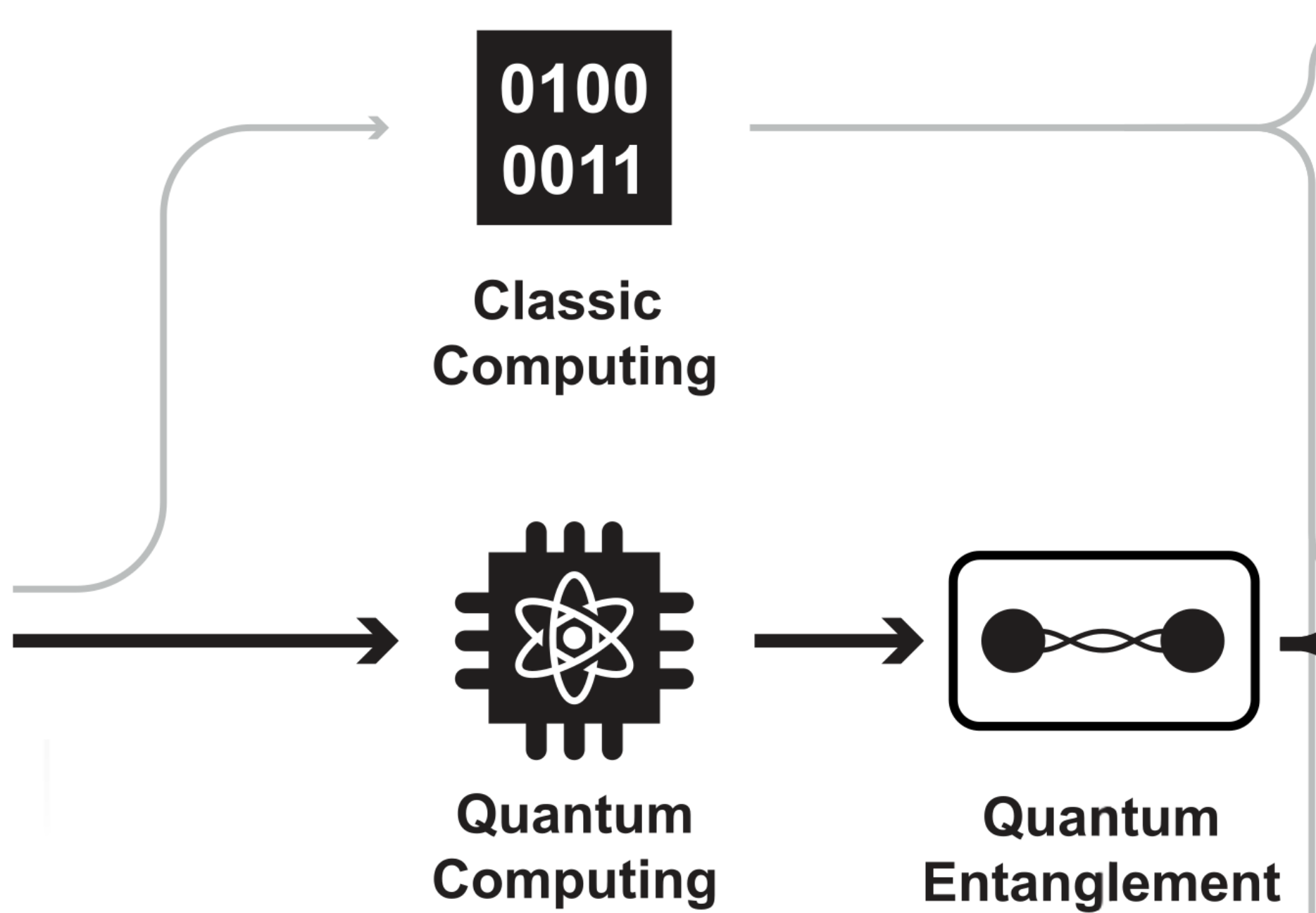
# Particles & Interactions

# Simulation

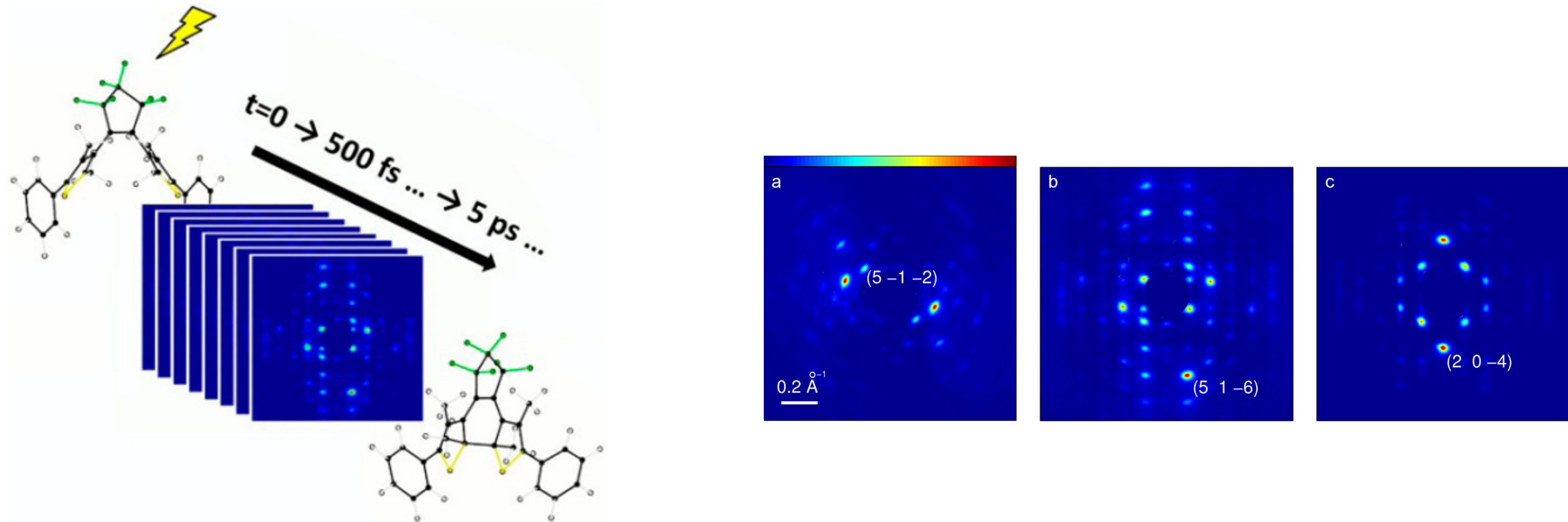
# Phases & Dynamics of Matter



- Quarks
- Leptons
- Gauge Bosons
- Higgs Boson



# Real-Time Dynamics and Reaction Pathways



*J. Phys. Chem. B* 2013, 117, 49, 15894-15902

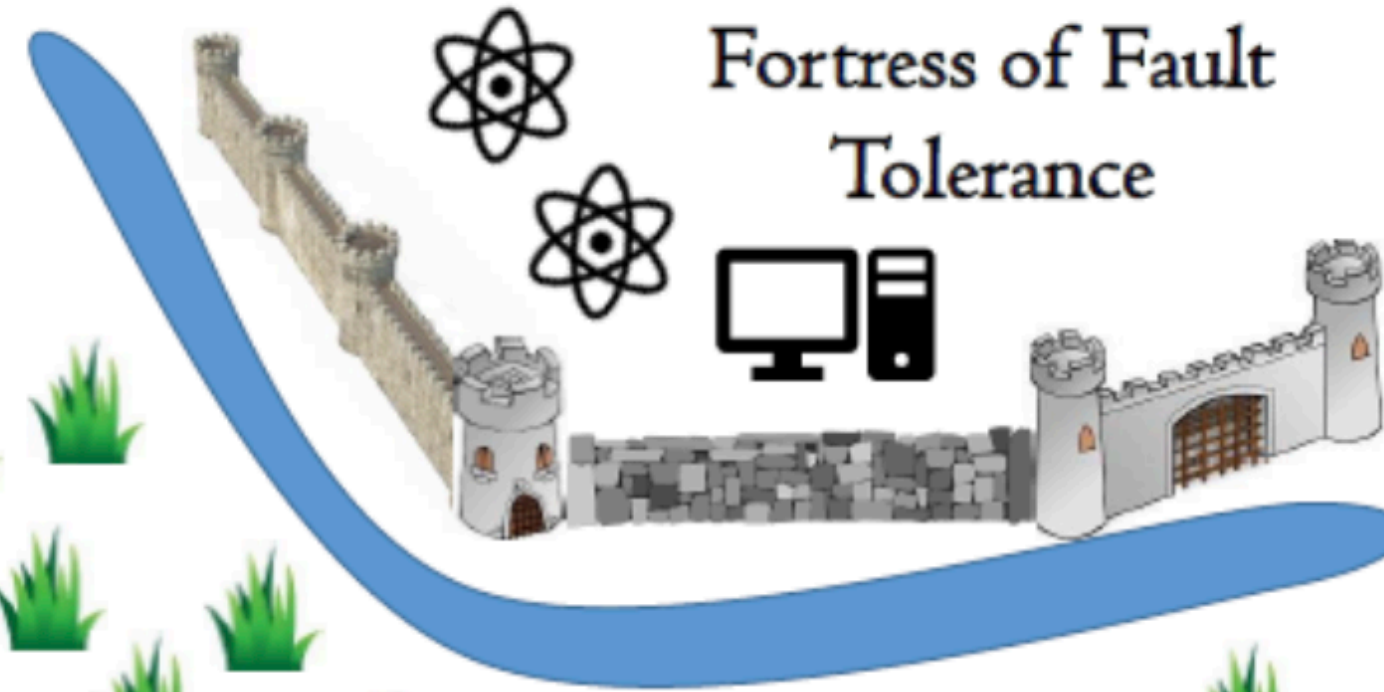
**Femto-second chemistry reveals reaction mechanisms**  
**Quantum simulations will reveal the reactions pathways of QCD**

# Quantum Simulation in the NISQ Era

Today: Error Mitigation and Dreaming of Correction



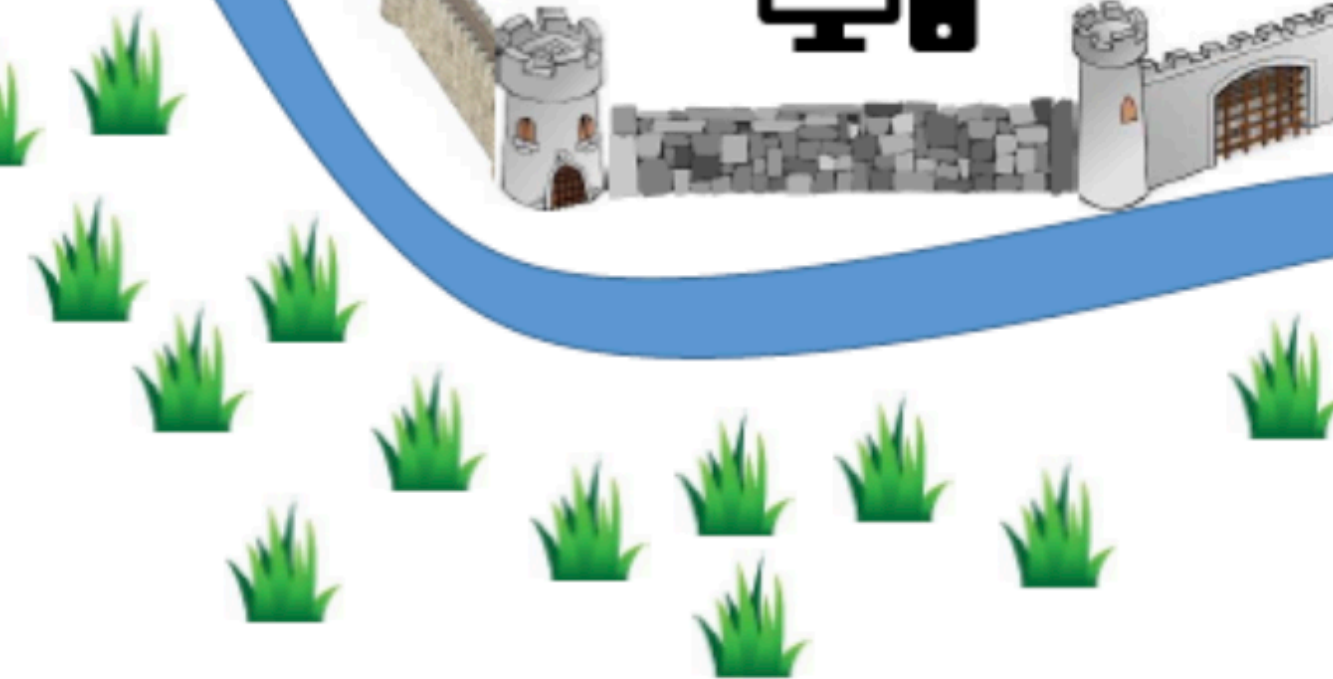
Magic Moat of Error Correction



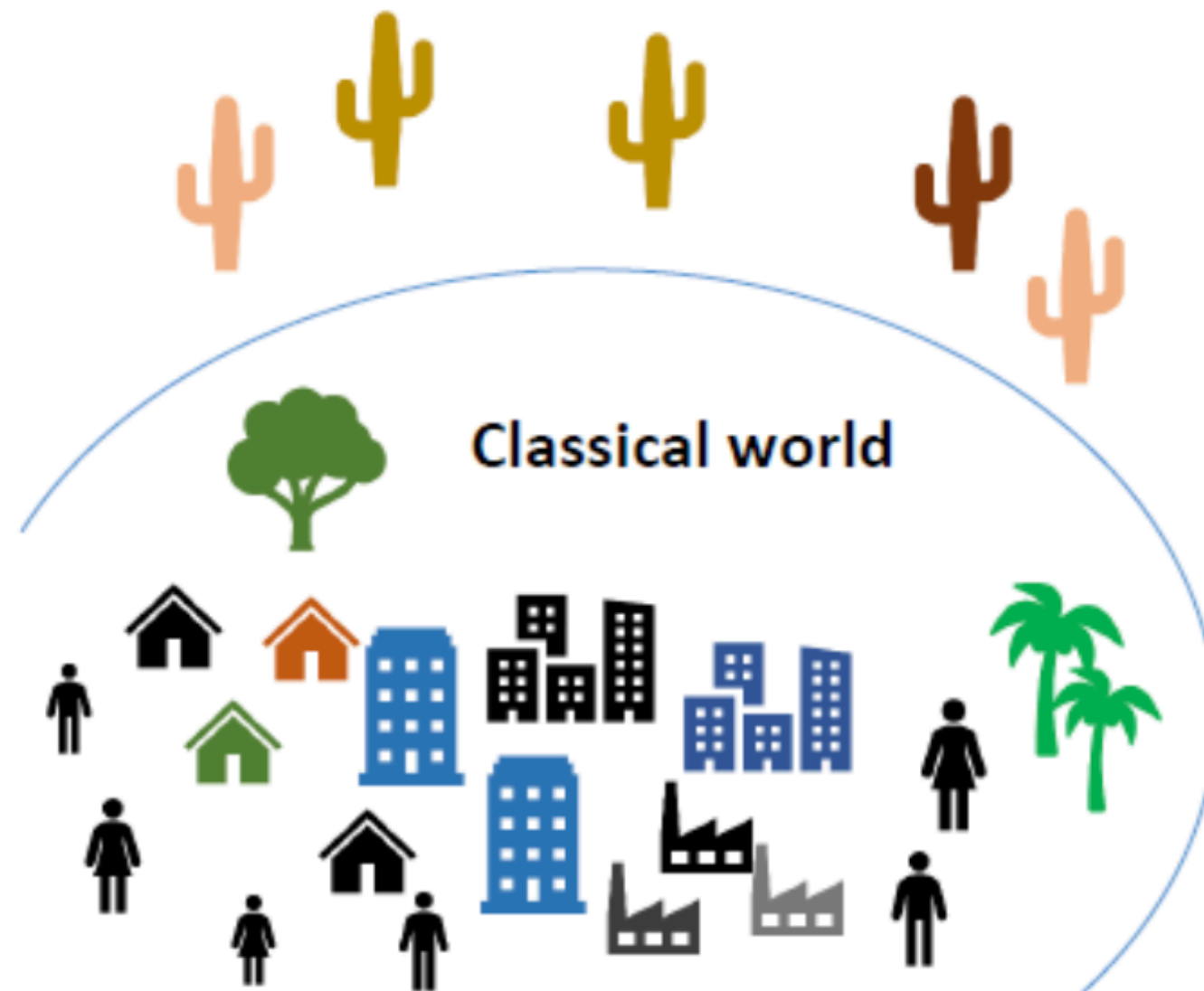
Fortress of Fault Tolerance

Precision simulations to compare with experiments and make reliable predictions

Verdant Plains of NISQ



Classical world



Desert of Deathly Decoherence



by [Ewan Munro](#), Co-Founder of [Entropica Labs](#).

Landscape of quantum computing from an error correction perspective. Inspired by a [figure](#) by Daniel

Gottesman.

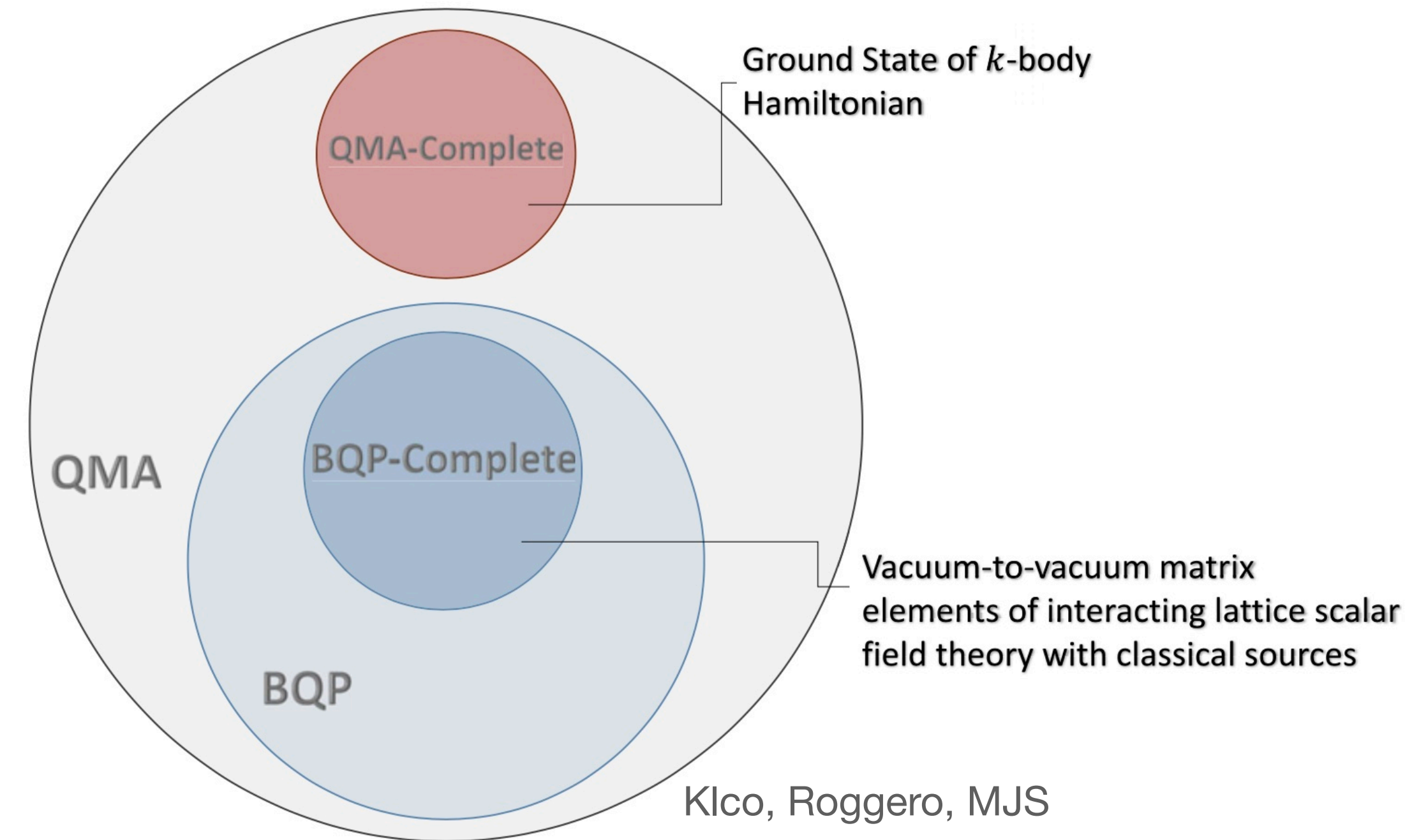
Insights, ideas, sub-parts, observables and algorithms

# Errors are a Defining Consideration in Simulations

Theory errors, mapping errors ,  
algorithm errors, workflow errors,  
device errors, analysis errors .....

Can find the source(s) of the largest errors  
and relax the others.

Exponential improvability is good!



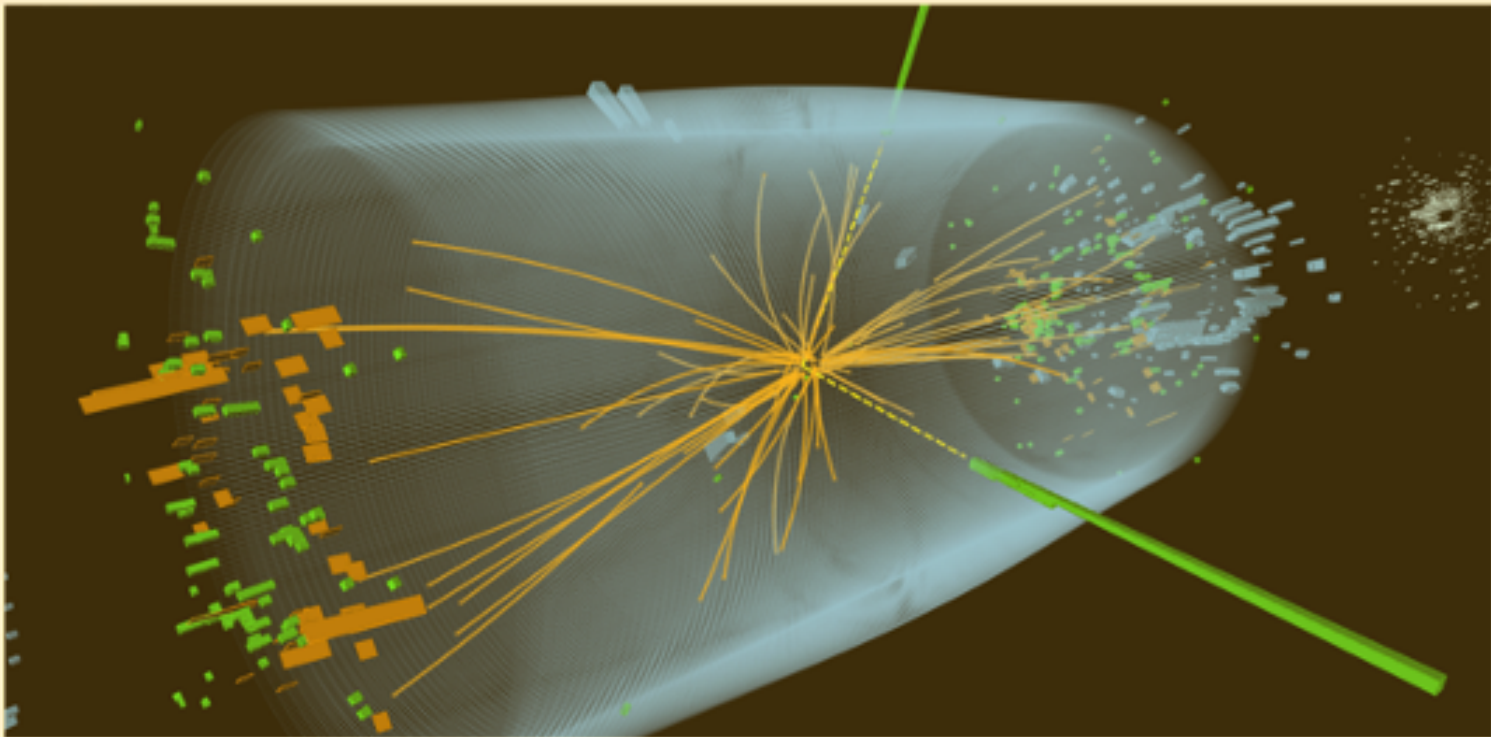
## Scaling

- system size
- precision



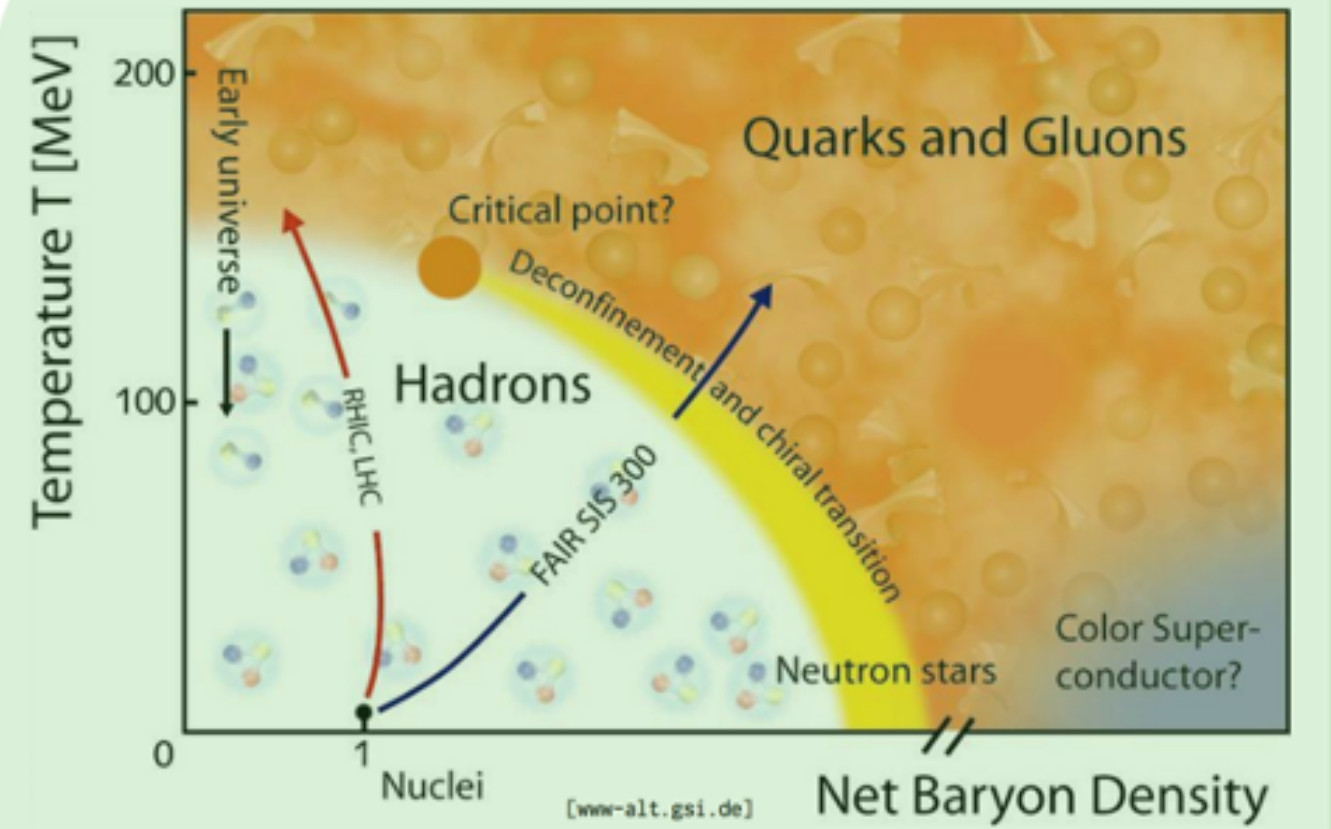
# Simulation Objectives for the Standard Model and Beyond

## Gauge Theories and Descendent Effective Field Theories and Models

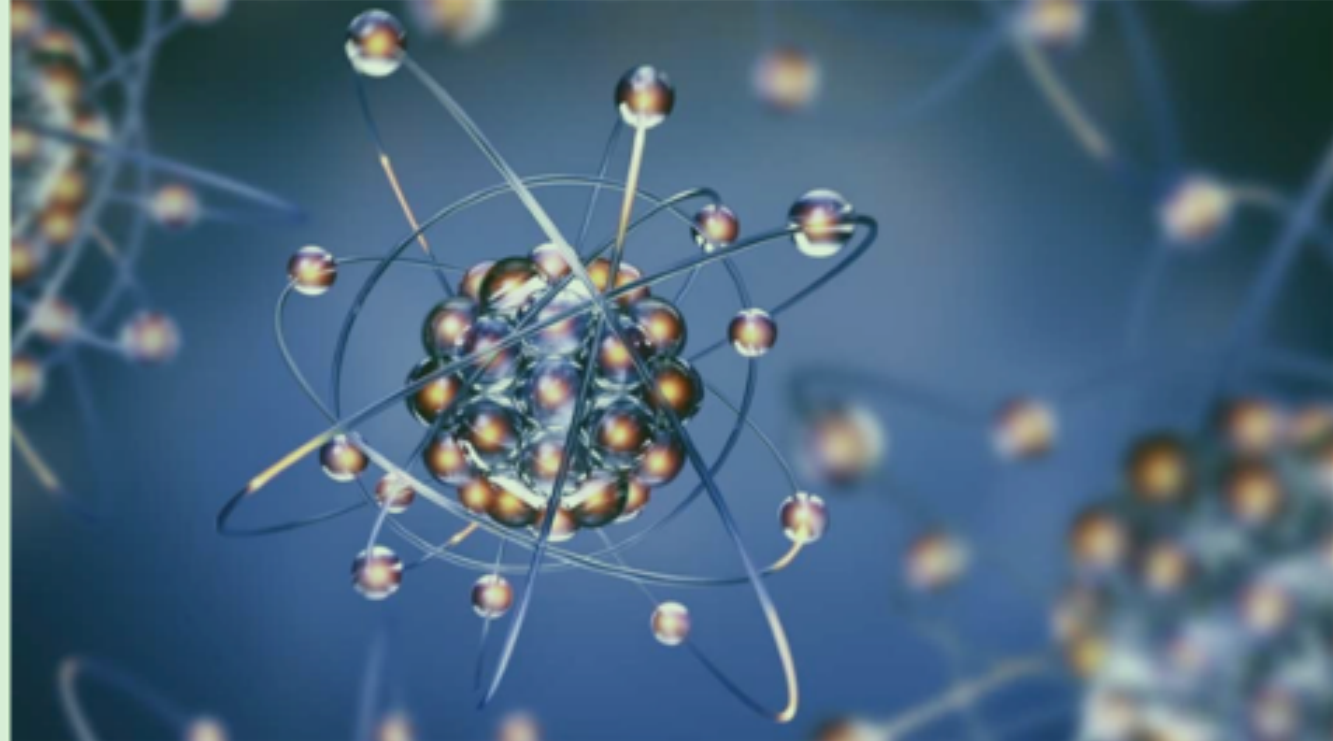


- Real-time dynamics
  - particle production, fragmentation
  - vacuum and in medium
- Low-energy reactions
- Electroweak processes (e.g.,  $\nu$ -A)
- Neutrino dynamics
- Matter-antimatter asymmetry

BQP

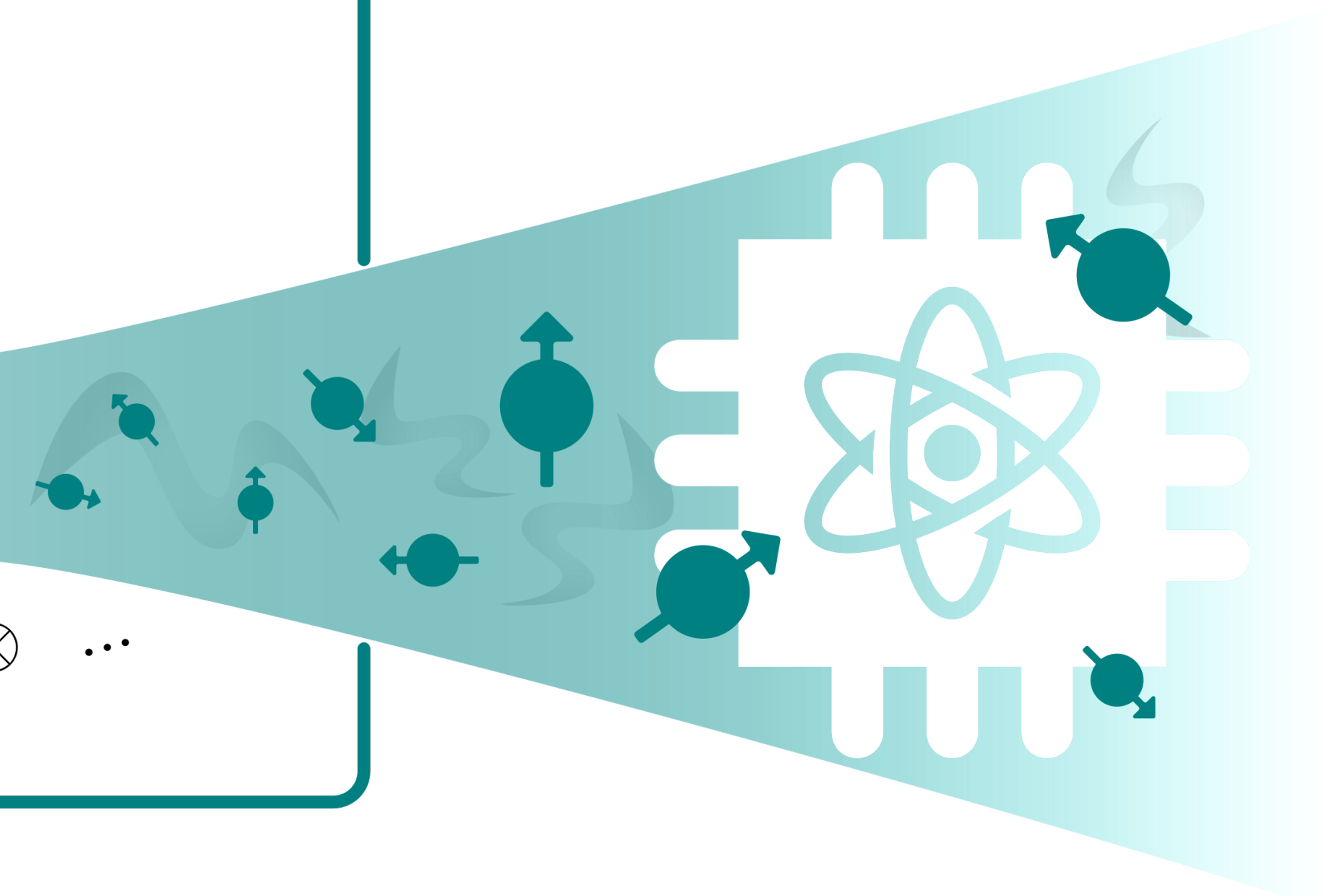
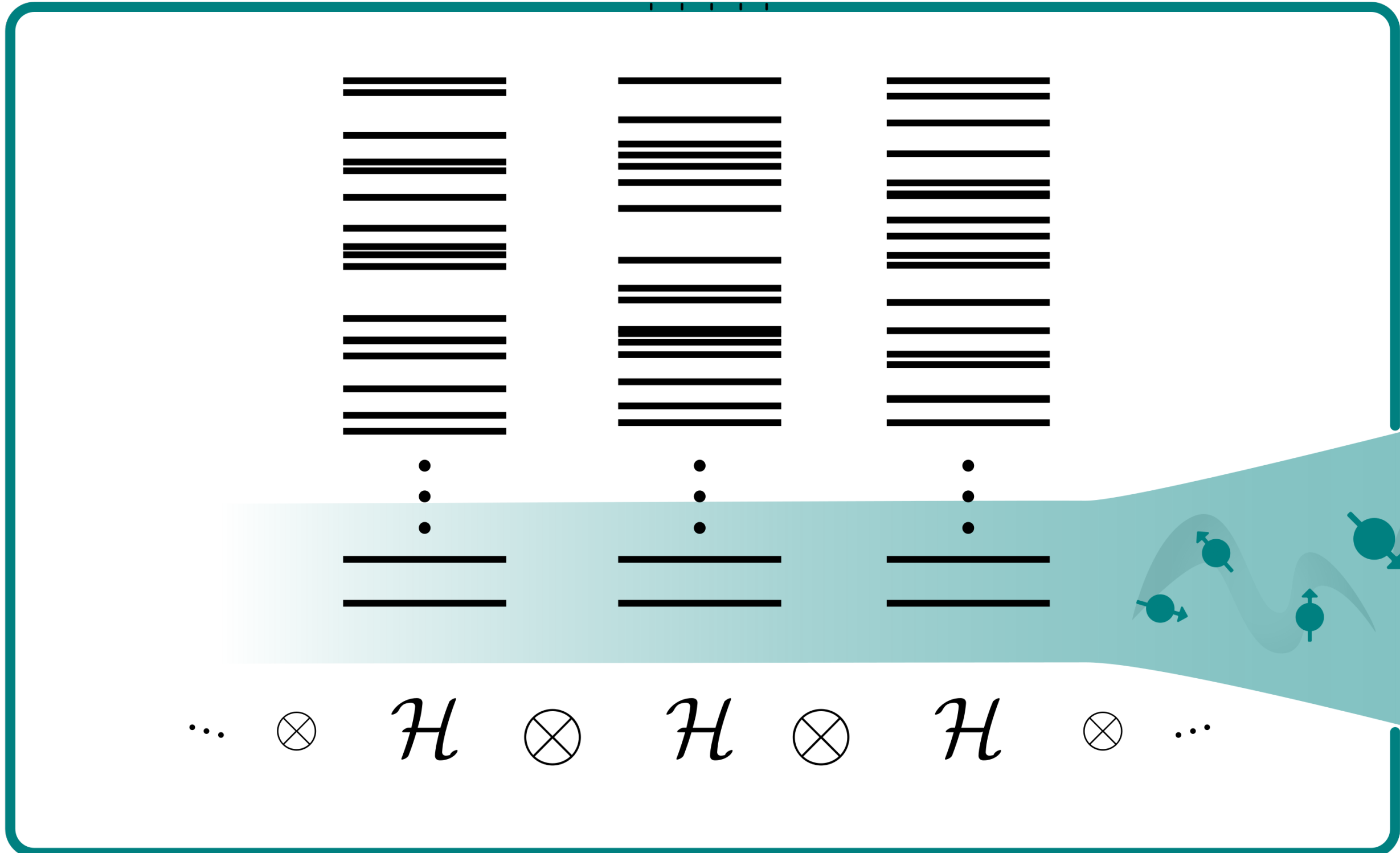
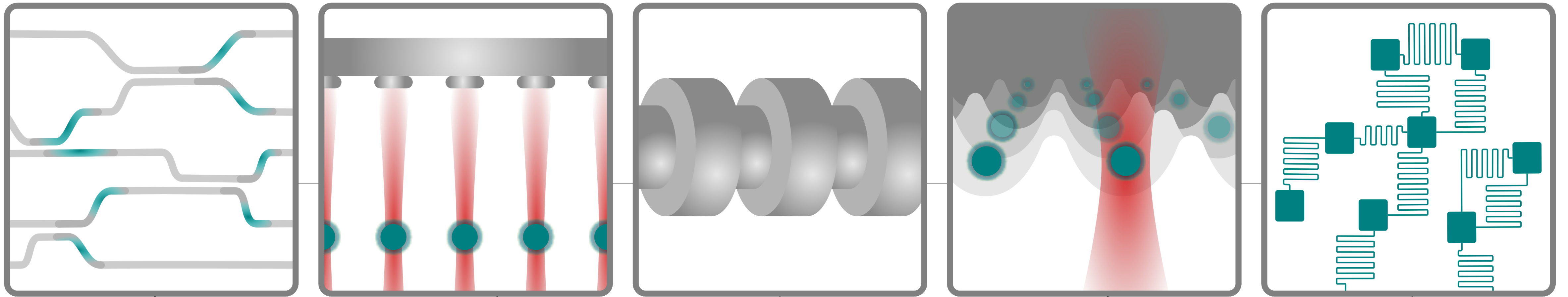


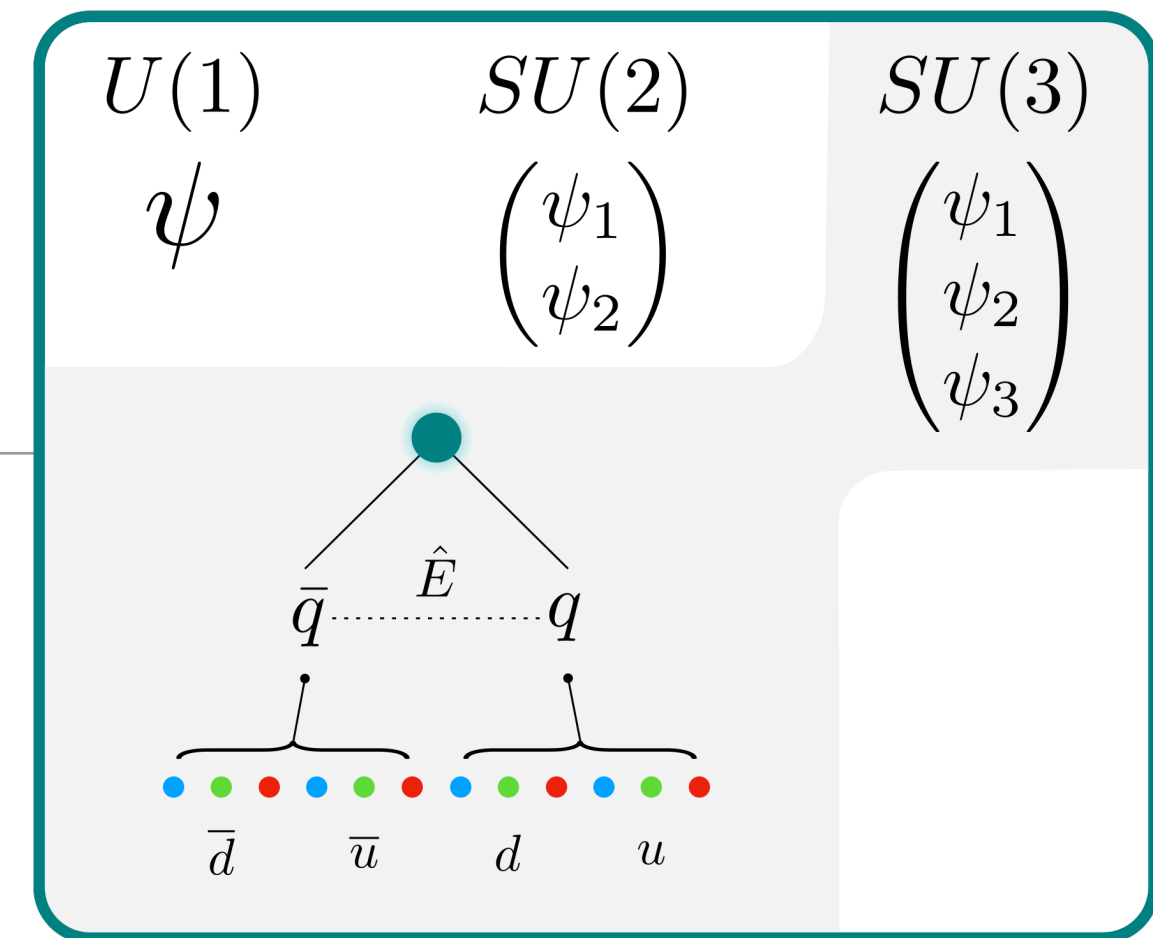
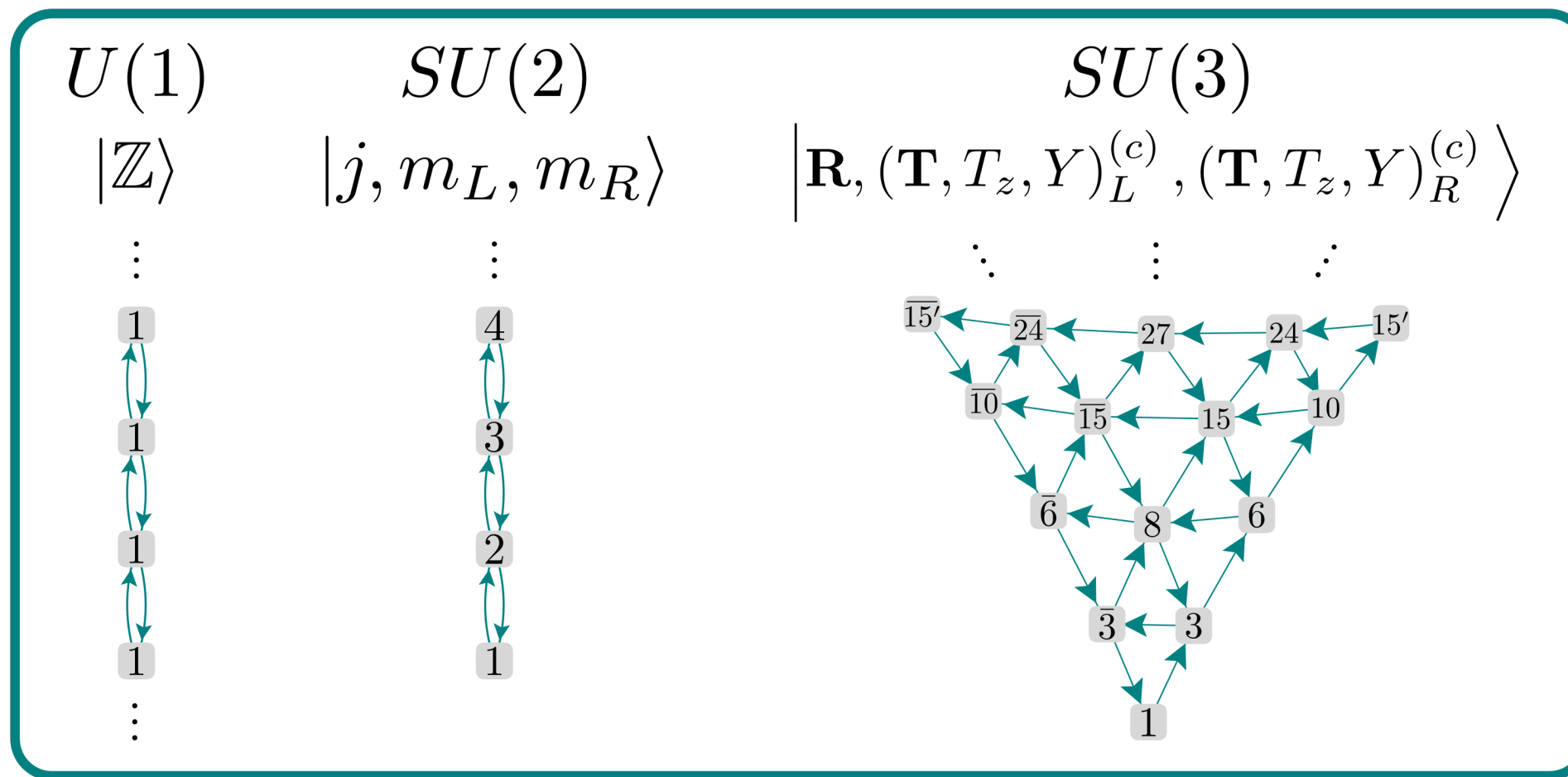
- Equation of state of dense hot matter and dynamics
  - viscosity, etc
- Conquering some "sign problems"
- The early universe
- Supernova/Neutron stars



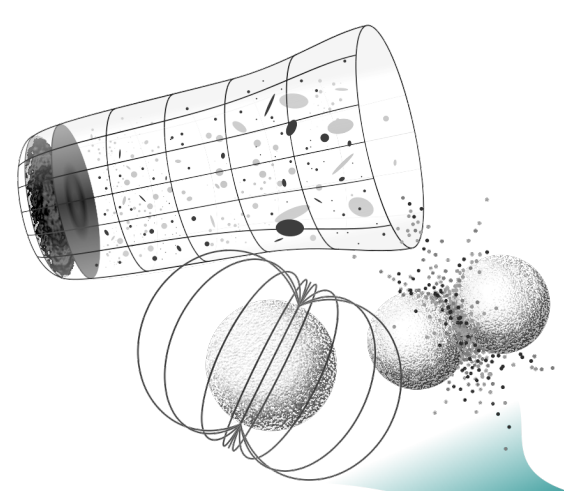
- Precision structure and interactions of nuclei
- Many-body systems
- Rare processes, double-beta decay

QMA  
 - symmetries

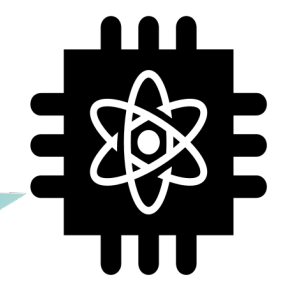




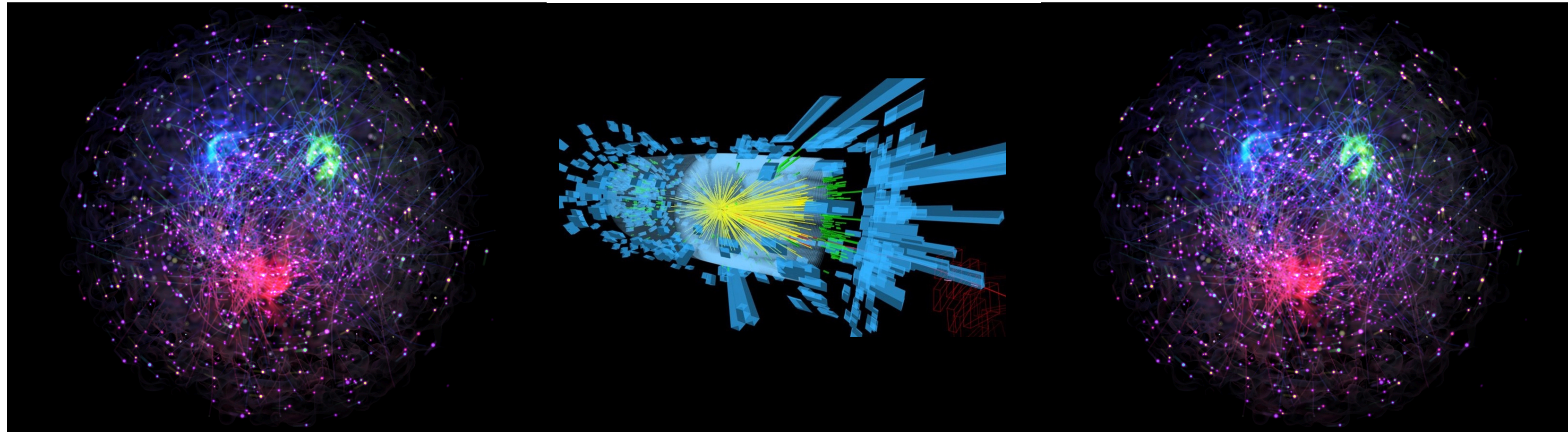
$$\hat{\mathcal{H}} \sim g^2 |\hat{E}(\mathbf{x})|^2 - \frac{1}{g^2} \text{Tr} \left[ \hat{U}_1 \hat{U}_2 \hat{U}_3^\dagger \hat{U}_4^\dagger + \text{h.c.} \right] + \hat{\mathcal{H}}_\psi$$



$$\hat{G}^a(\mathbf{x}) |\Phi\rangle_{\text{phys}} = 0$$



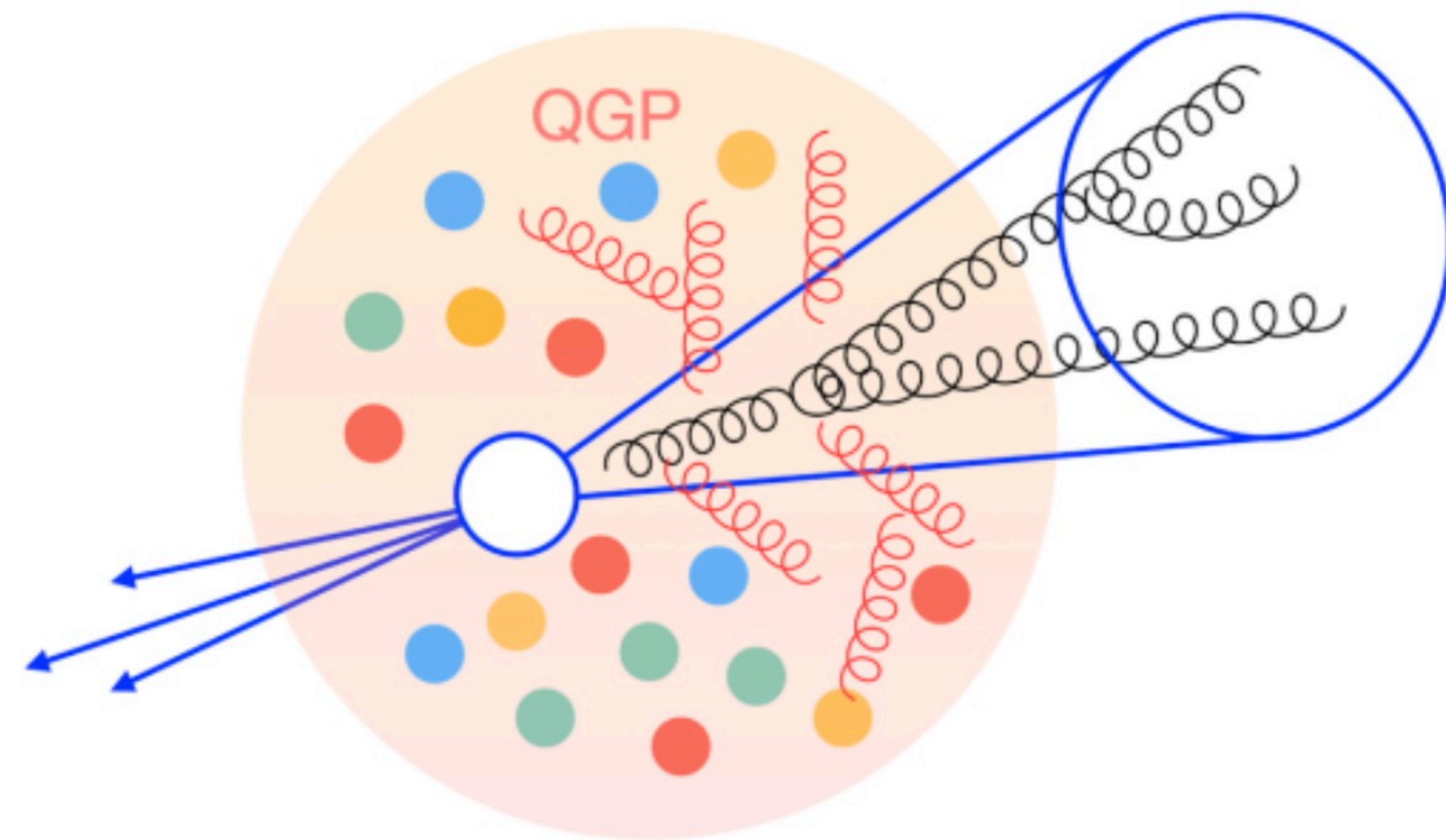
# Hadronization and Fragmentation



For example, jet production, energy-loss, hadronization

3+1D, quantum chromodynamics, quarks+gluons

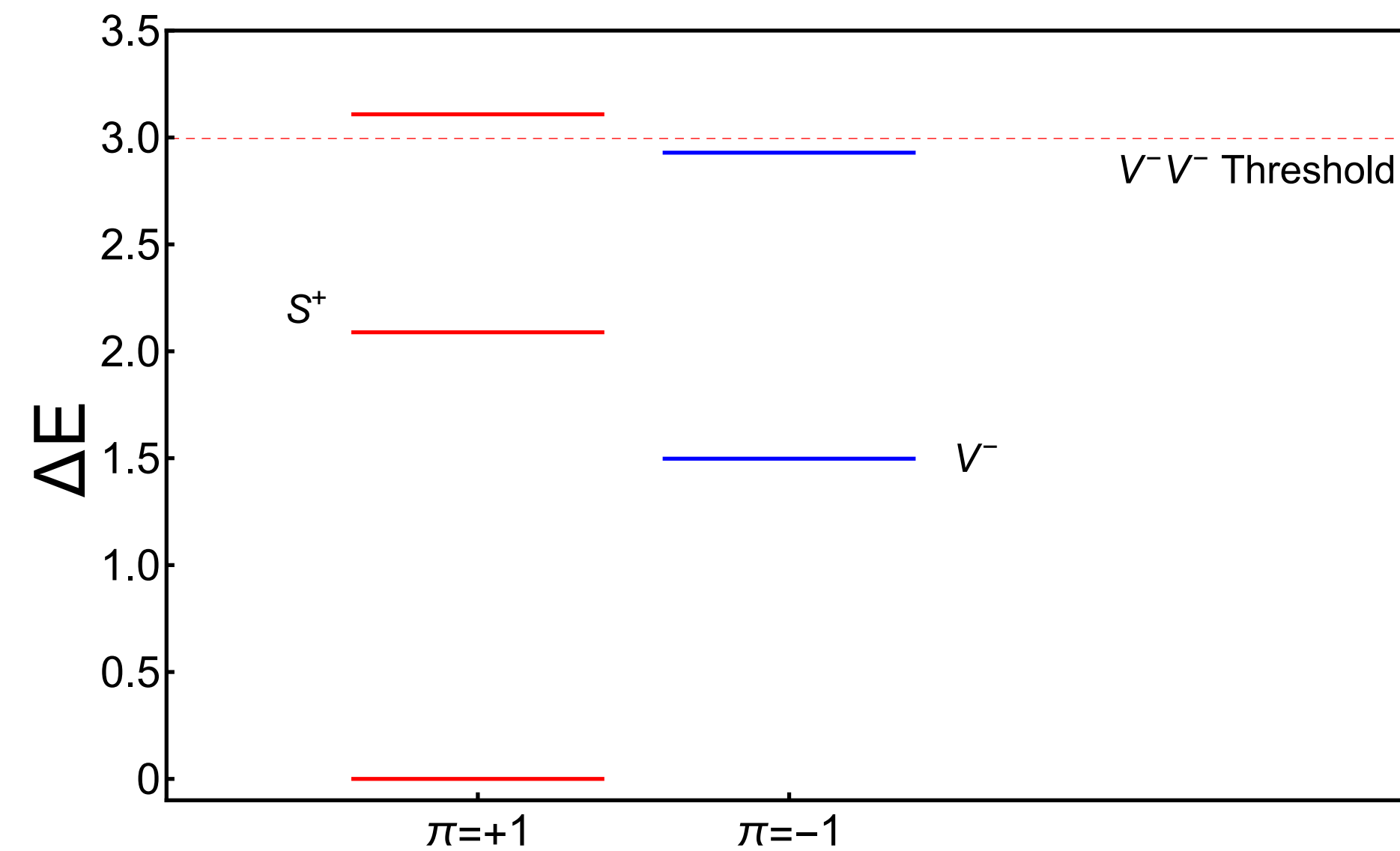
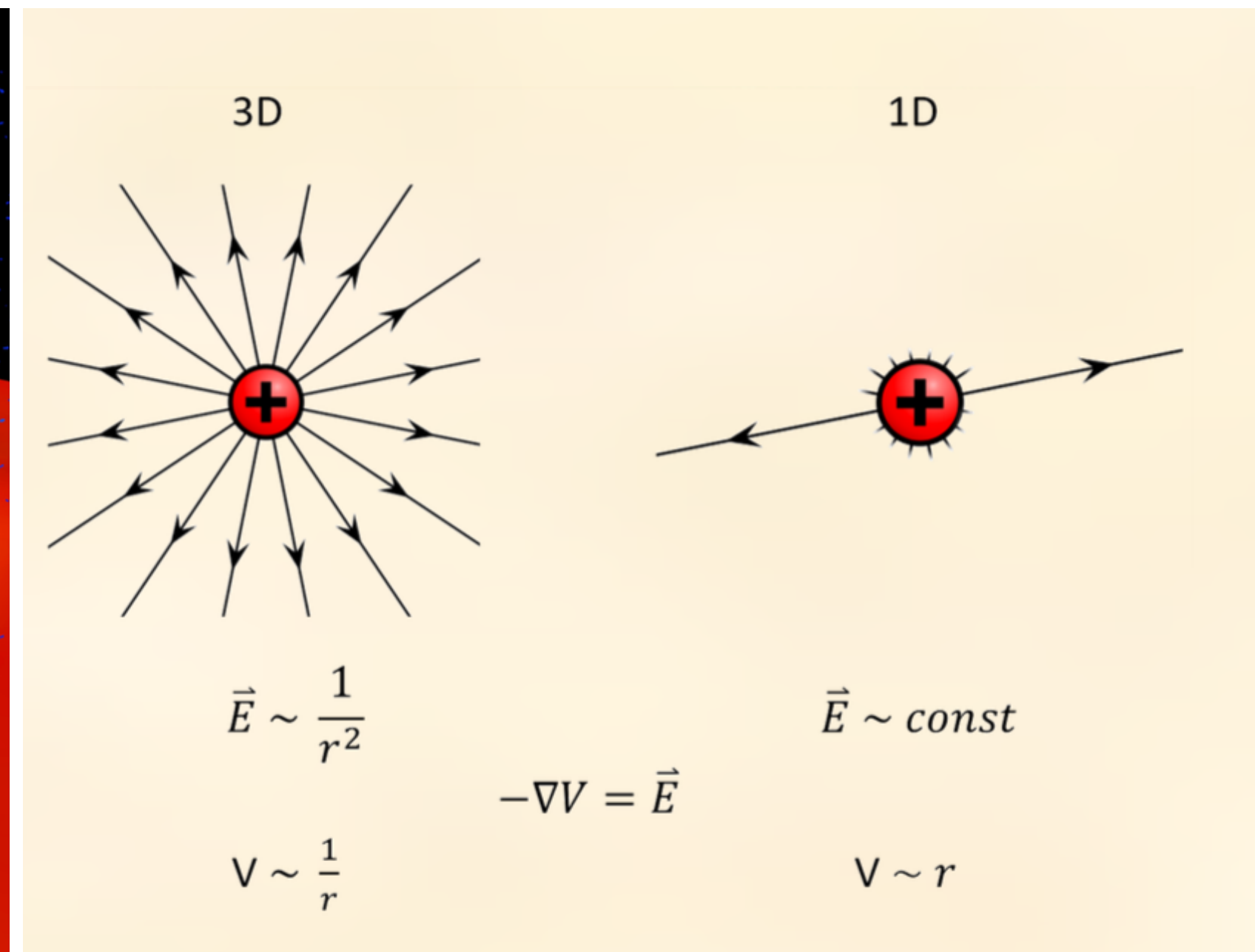
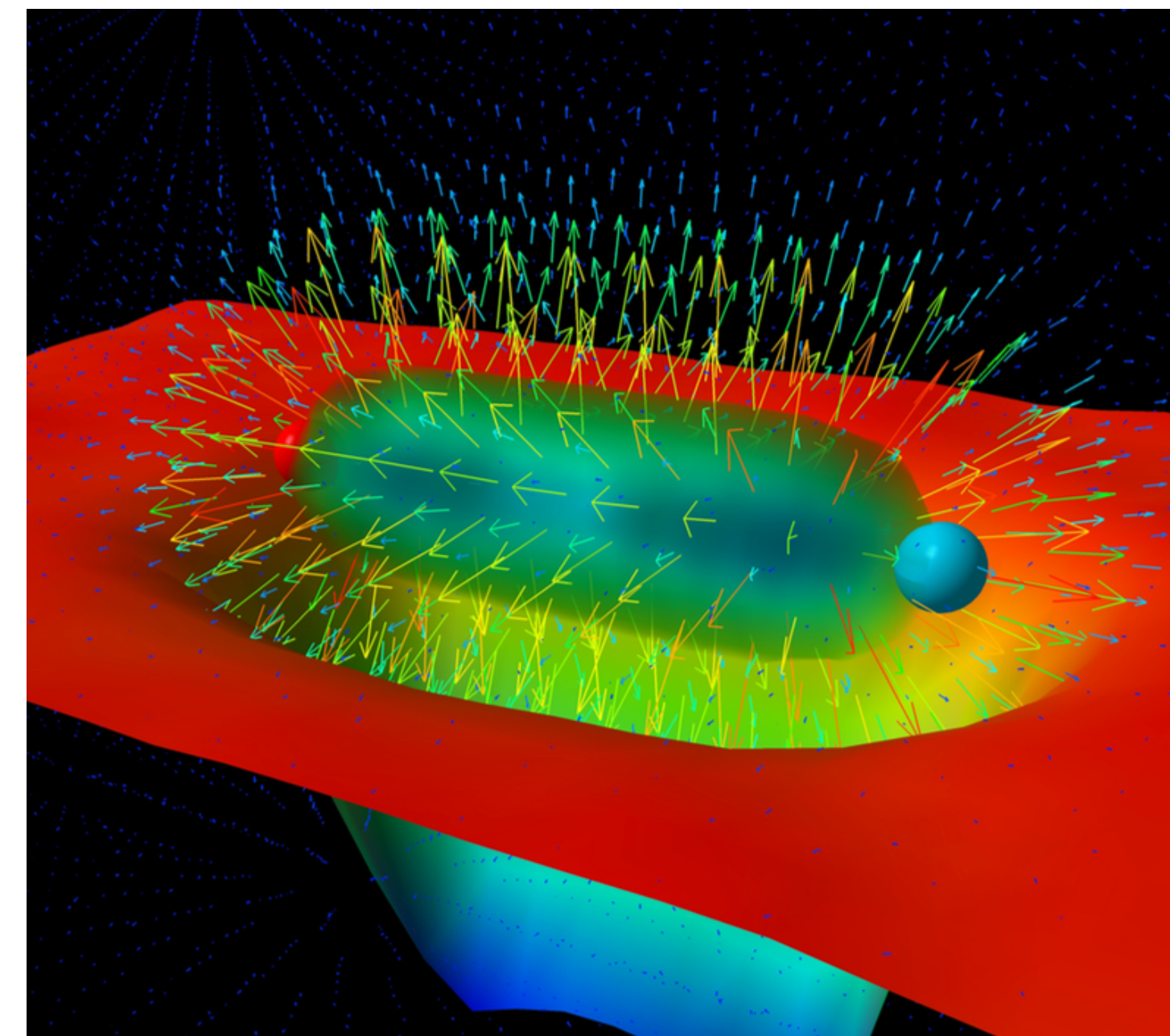
Event generators constrained by decades of precise data,  
Asymptotic freedom, effective field theory relations,  
Lacks entanglement and quantum coherence.  
Major classical computing resource requirement.



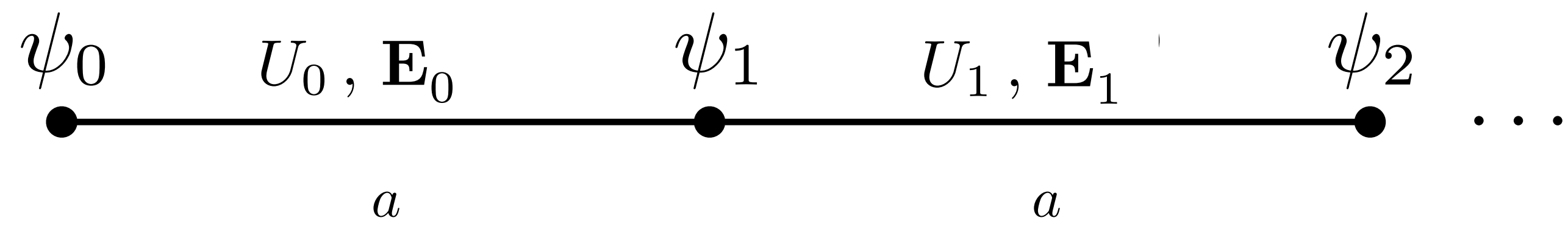
# Quantum Electrodynamics in 1+1 Dimensions

$$\mathcal{L} = \bar{\psi} (i\not{D} - m) \psi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

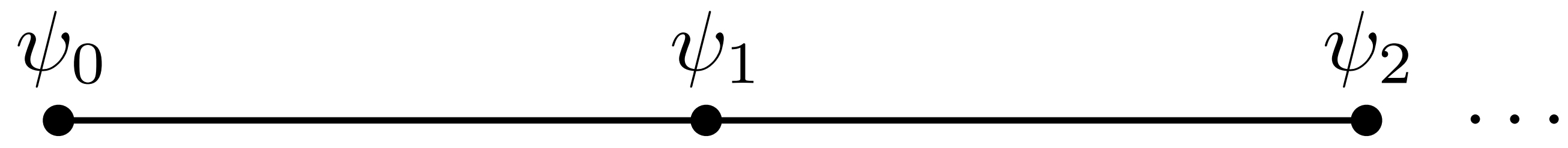
- Charge screening, confinement
- Fermion condensate
- Gap
- Translationally invariant vacuum



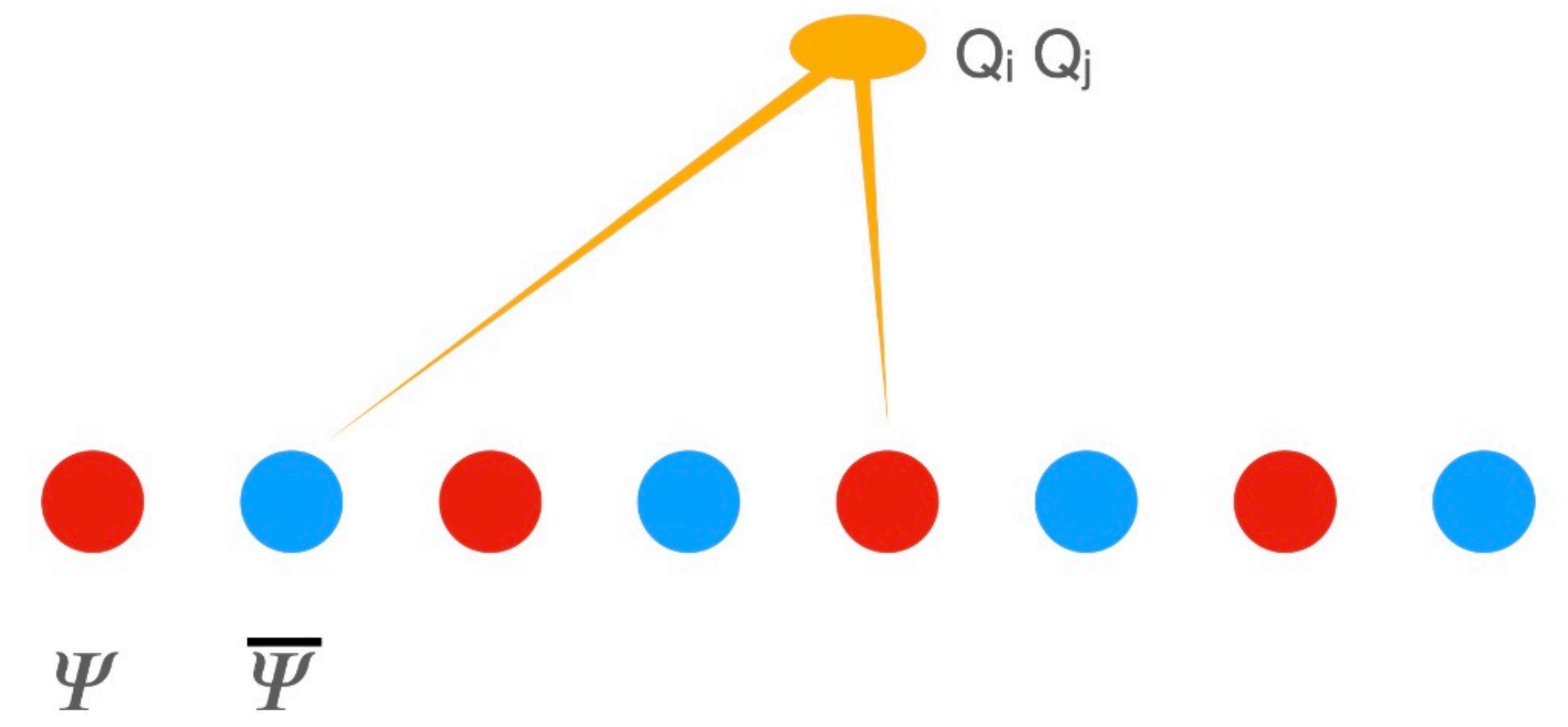
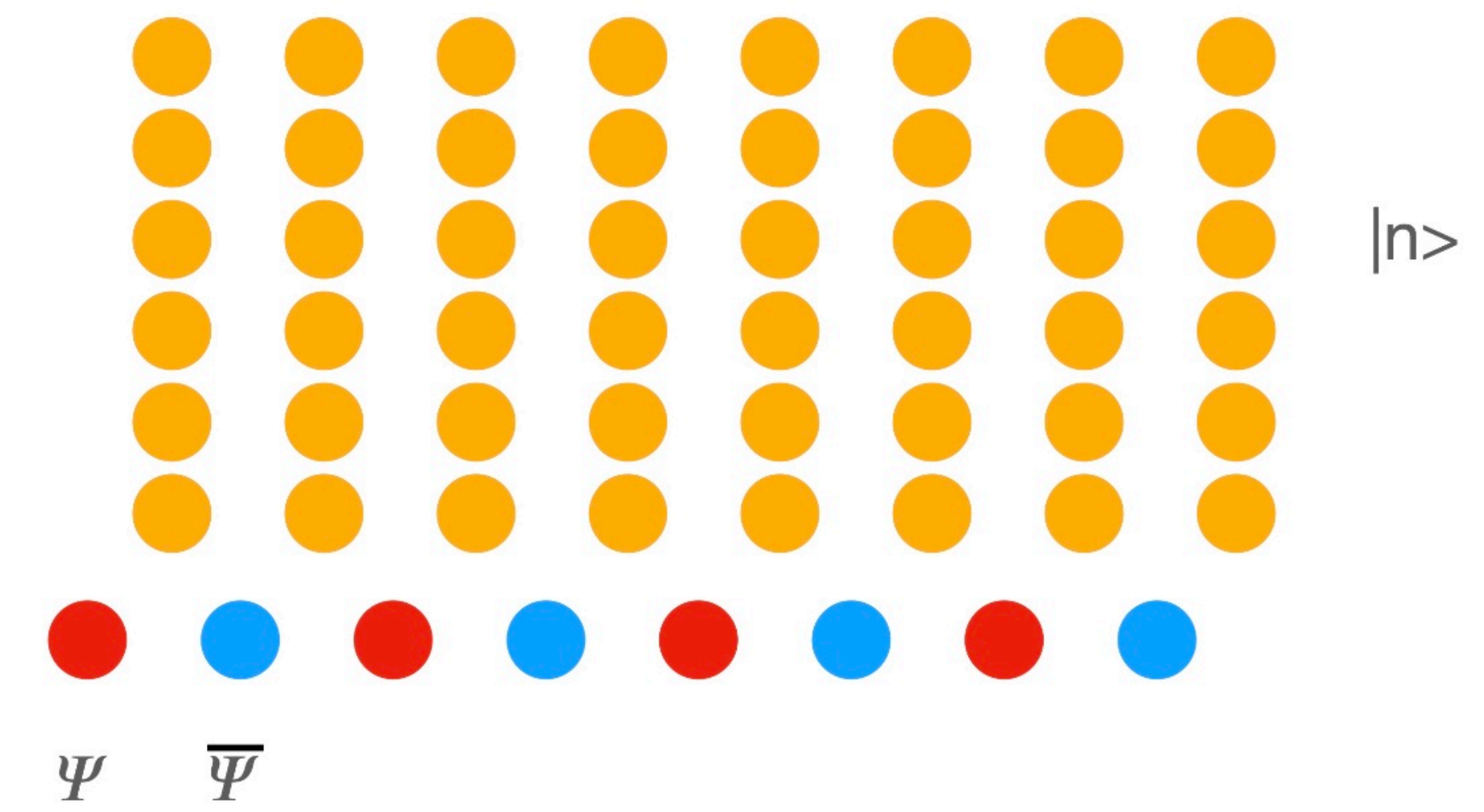
# Lattice Hamiltonian in 1+1D - Which Gauge to Choose?



**Weyl gauge**



**Axial gauge**



# Jordan-Wigner Mapping with OBCs

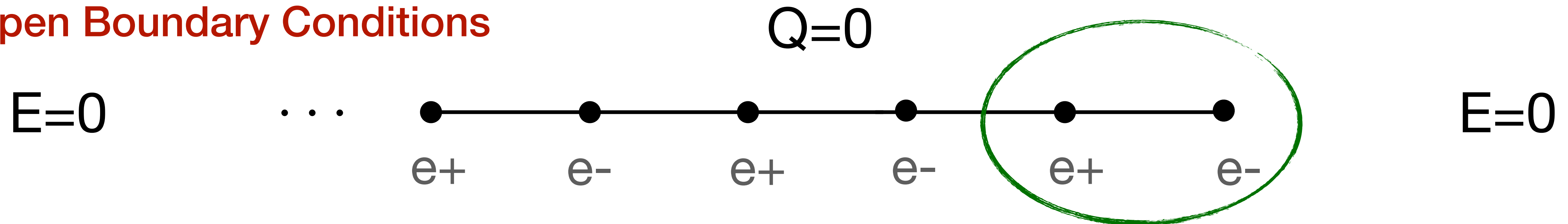
$$\hat{H} = \hat{H}_m + \hat{H}_{kin} + \hat{H}_{el} = \frac{m}{2} \sum_{j=0}^{2L-1} \left[ (-1)^j \hat{Z}_j + \hat{I} \right] + \frac{1}{2} \sum_{j=0}^{2L-2} (\hat{\sigma}_j^+ \hat{\sigma}_{j+1}^- + \text{h.c.}) + \frac{g^2}{2} \sum_{j=0}^{2L-2} \left( \sum_{k \leq j} \hat{Q}_k \right)^2$$

Local
Nearest Neighbor
Non-local

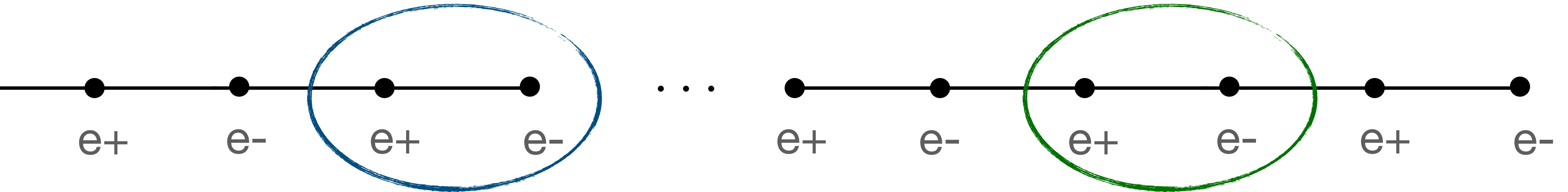
$$\hat{Q}_k = -\frac{1}{2} \left[ \hat{Z}_k + (-1)^k \hat{I} \right] \quad \chi = \frac{1}{2L} \sum_{j=0}^{2L-1} \left\langle (-1)^j \hat{Z}_j + \hat{I} \right\rangle \equiv \frac{1}{2L} \sum_{j=0}^{2L-1} \chi_j$$

Local
Local

Open Boundary Conditions



# Confinement Means .....



$$\langle Q_i Q_j \rangle$$

Vanishes exponentially with increasing separation  
— with a length scale set by the gap

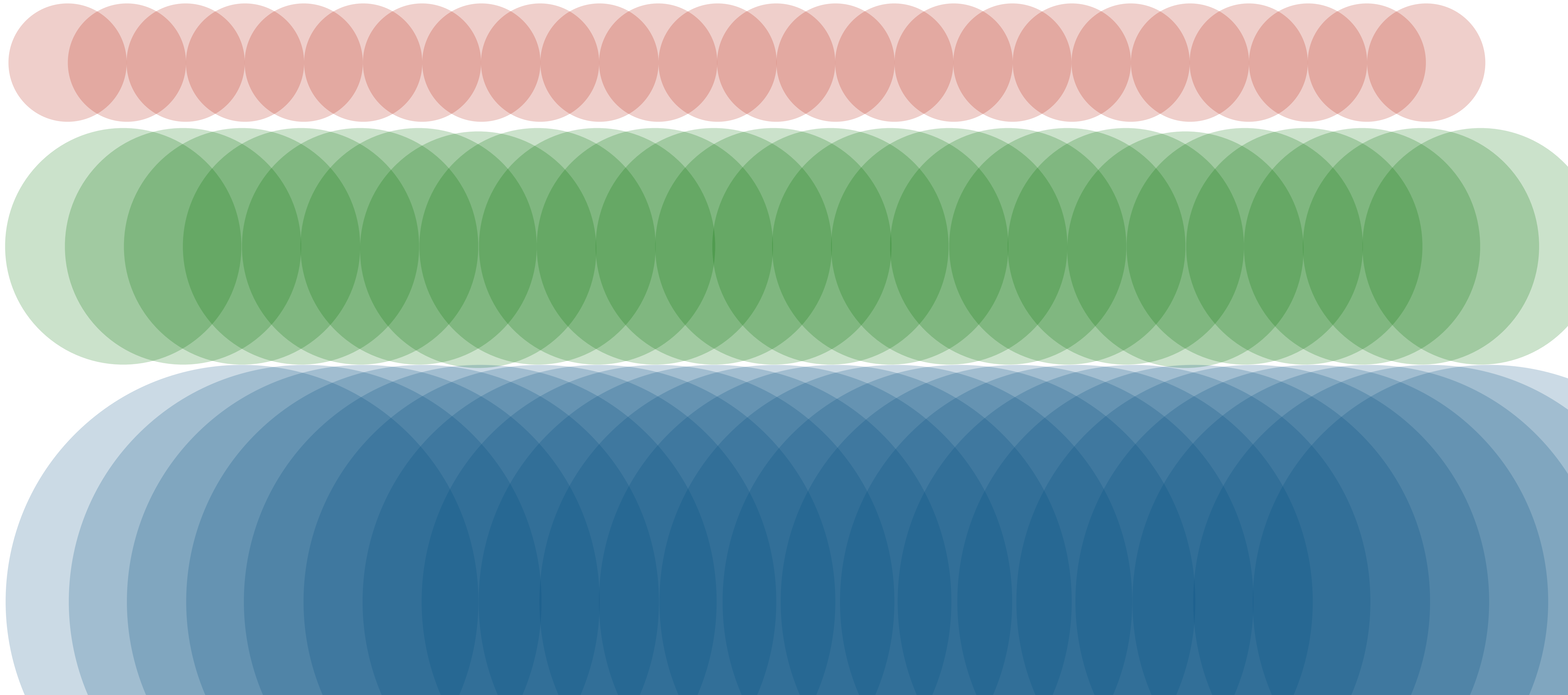
Truncation of non-local term(s) in the Hamiltonian will converge rapidly



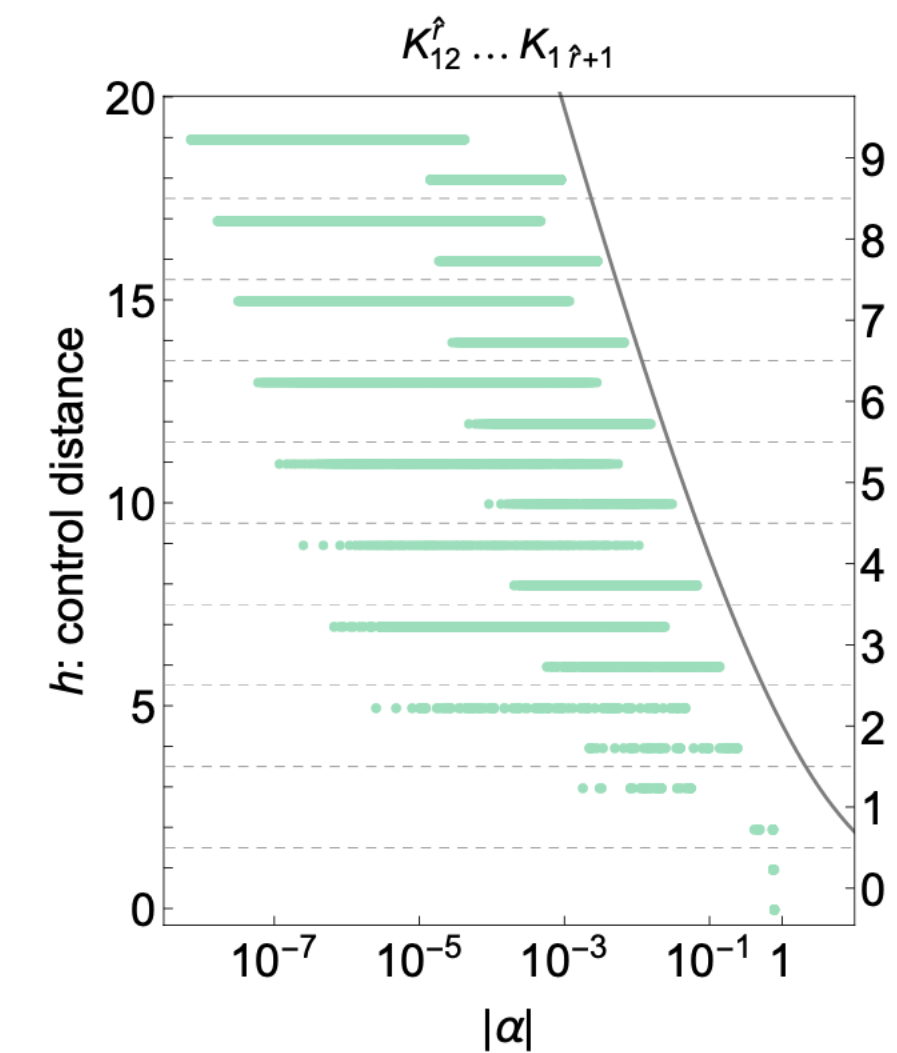
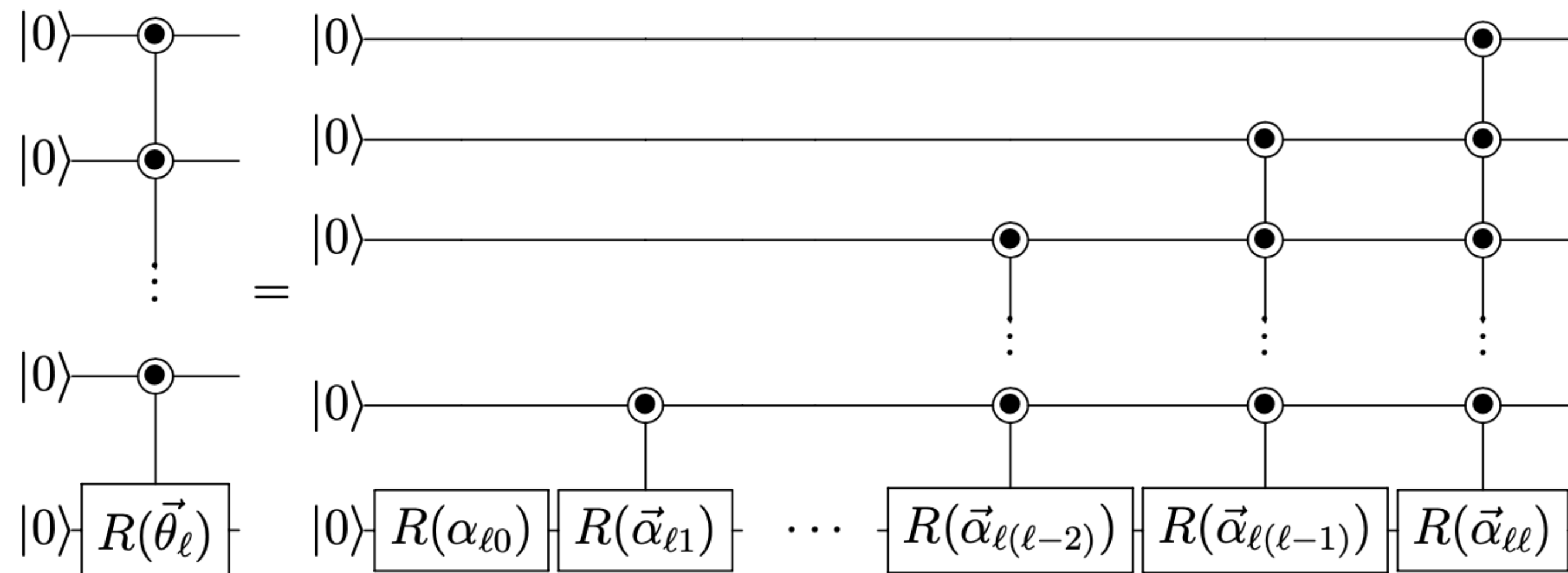
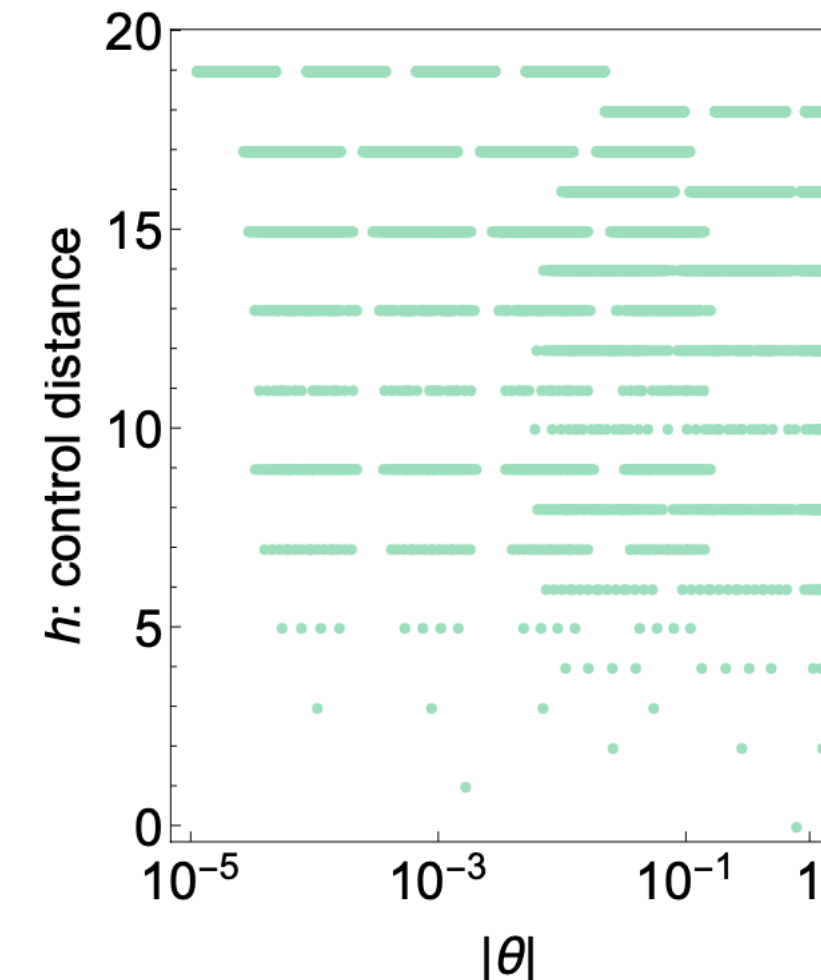
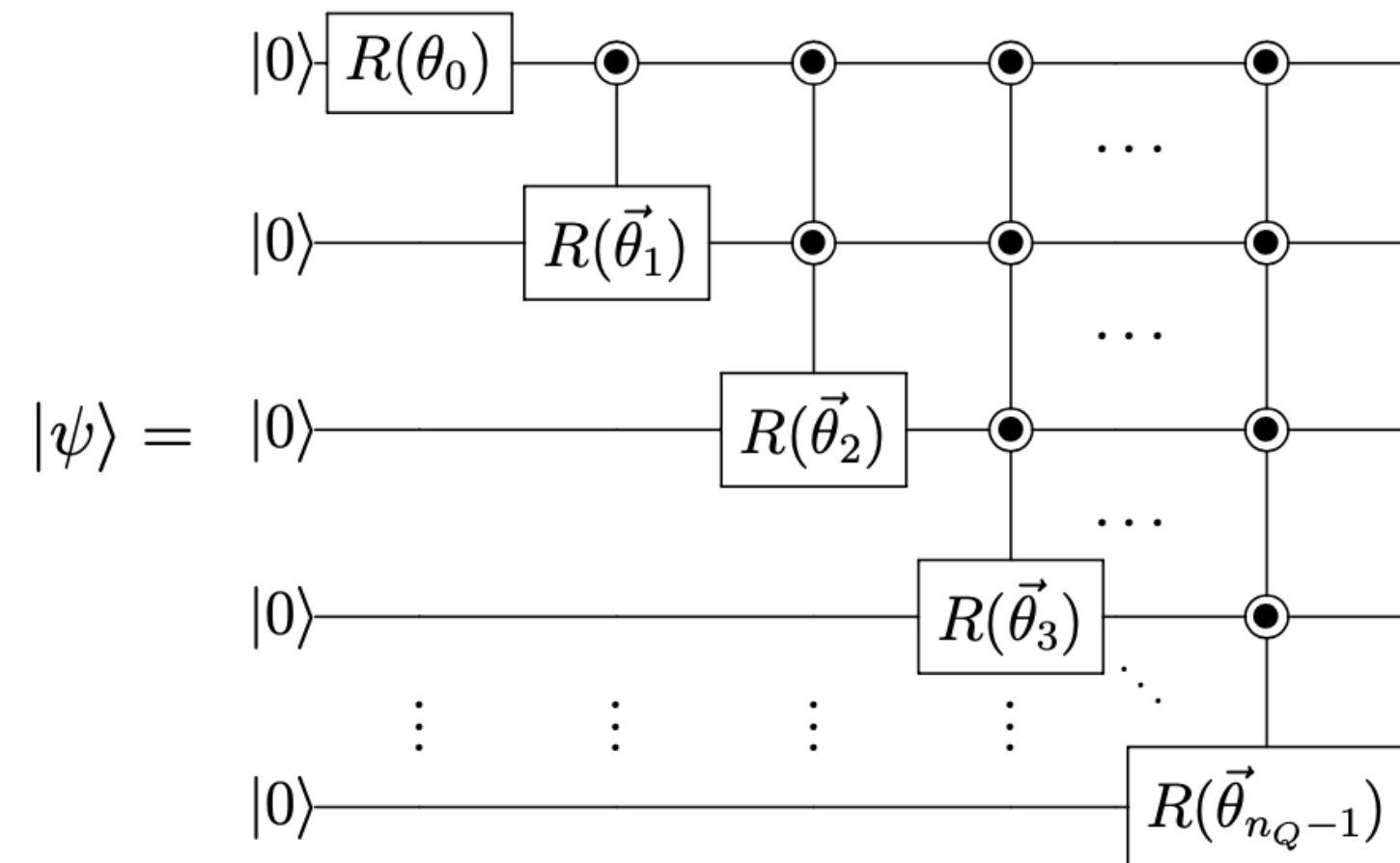
# Building in Correlations

**Bounded in the IR and UV - Confinement Scale**

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# Physics-Aware Mapping and State Preparation



Correlation length allows for fixed-point angles to be determined exponentially well with small-scale simulations

Systematically Localizable Operators for Quantum Simulations of Quantum Field Theories

Natalie Klco (Washington U., Seattle), Martin J. Savage (Dec 7, 2019)

Published in: *Phys.Rev.A* 102 (2020) 1, 012619 • e-Print: 1912.03577 [quant-ph]

Fixed-point quantum circuits for quantum field theories

Natalie Klco (Washington U., Seattle), Martin J. Savage (Washington U., Seattle) (Feb 5, 2020)

Published in: *Phys.Rev.A* 102 (2020) 5, 052422 • e-Print: 2002.02018 [quant-ph]

# Preparing the Vacuum: Outline of Strategy

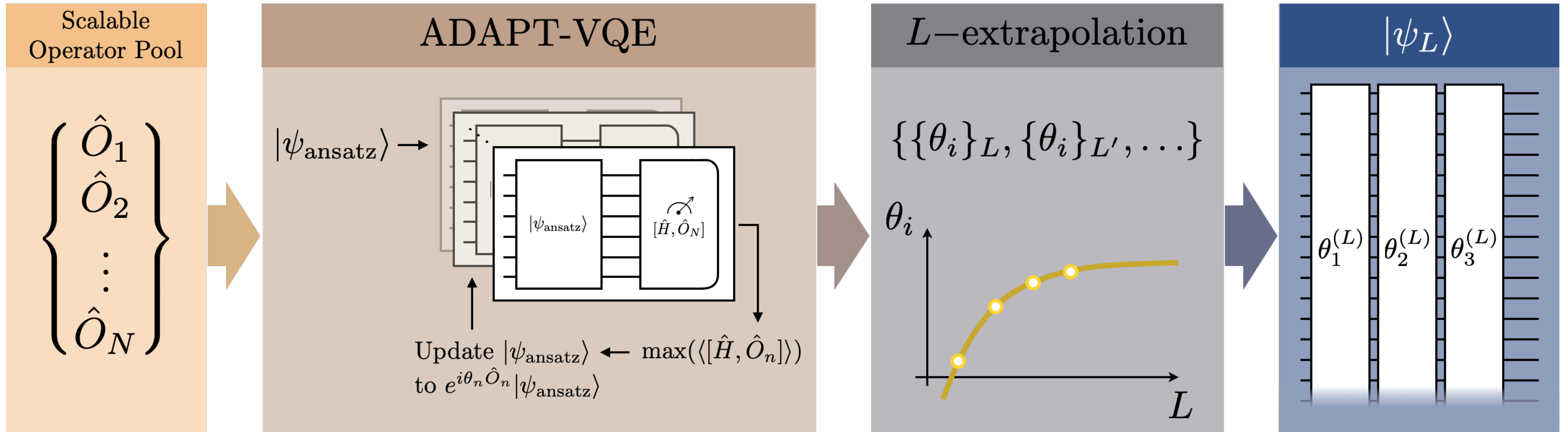
## Introducing ... SC-ADAPT-VQE

### Symmetries and Confinement

**Classical** Optimization

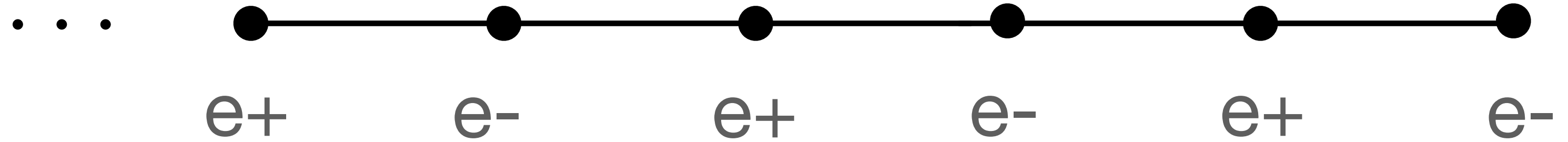
**Classical** Extrapolations

**Quantum** Implementation



Adaptive Derivative-Assembled Pseudo-Trotter ansatz Variational Quantum Eigensolver (ADAPT-VQE)

# Scalable Operators: Volume and Surface



$$\hat{\Theta}_m^V = \frac{1}{2} \sum_{n=0}^{2L-1} (-1)^n \hat{Z}_n ,$$

$$\hat{\Theta}_h^V(d) = \frac{1}{4} \sum_{n=0}^{2L-1-d} \left( \hat{X}_n \hat{Z}^{d-1} \hat{X}_{n+d} + \hat{Y}_n \hat{Z}^{d-1} \hat{Y}_{n+d} \right) ,$$

$$\hat{\Theta}_m^S(d) = (-1)^d \frac{1}{2} \left( \hat{Z}_d - \hat{Z}_{2L-1-d} \right) ,$$

$$\hat{\Theta}_h^S(d) = \frac{1}{4} \left( \hat{X}_1 \hat{Z}^{d-1} \hat{X}_{d+1} + \hat{Y}_1 \hat{Z}^{d-1} \hat{Y}_{d+1} + \hat{X}_{2L-2-d} \hat{Z}^{d-1} \hat{X}_{2L-2} + \hat{Y}_{2L-2-d} \hat{Z}^{d-1} \hat{Y}_{2L-2} \right)$$

Real wavefunction from real initial wavefunction : (all) symmetries in operators

# Scalable Operators: Volume and Surface

$$\{\hat{O}\} = \left\{ \hat{O}_{mh}^V(d), \hat{O}_{mh}^S(0, d), \hat{O}_{mh}^S(1, d) \right\},$$

$$\hat{O}_{mh}^V(d) \equiv i \left[ \hat{\Theta}_m^V, \hat{\Theta}_h^V(d) \right] = \frac{1}{2} \sum_{n=0}^{2L-1-d} (-1)^n \left( \hat{X}_n \hat{Z}^{d-1} \hat{Y}_{n+d} - \hat{Y}_n \hat{Z}^{d-1} \hat{X}_{n+d} \right),$$

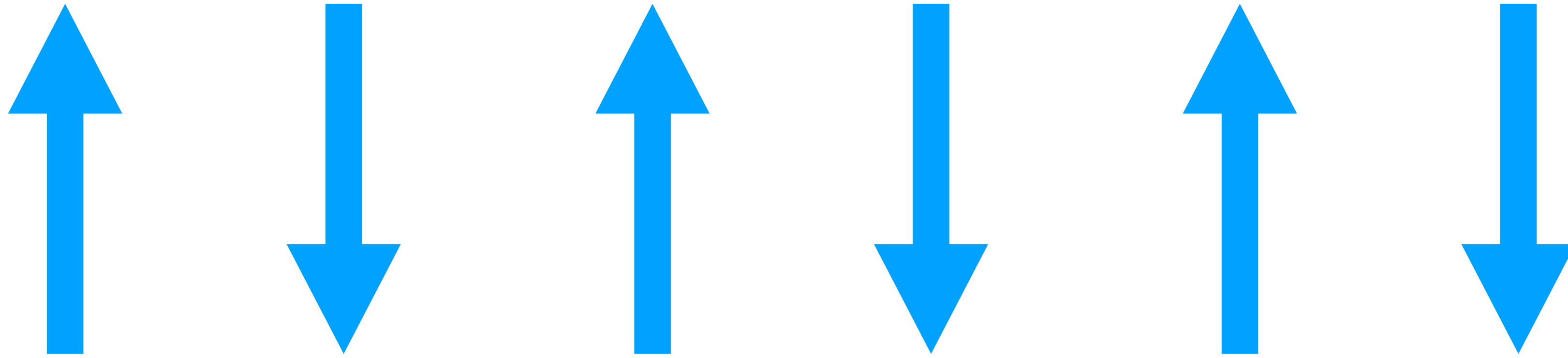
$$\hat{O}_{mh}^S(0, d) \equiv i \left[ \hat{\Theta}_m^S(0), \hat{\Theta}_h^V(d) \right] = \frac{1}{4} \left( \hat{X}_0 \hat{Z}^{d-1} \hat{Y}_d - \hat{Y}_0 \hat{Z}^{d-1} \hat{X}_d - \hat{Y}_{2L-1-d} \hat{Z}^{d-1} \hat{X}_{2L-1} + \hat{X}_{2L-1-d} \hat{Z}^{d-1} \hat{Y}_{2L-1} \right),$$

$$\hat{O}_{mh}^S(1, d) \equiv i \left[ \hat{\Theta}_m^S(1), \hat{\Theta}_h^S(d) \right] = \frac{1}{4} \left( \hat{Y}_1 \hat{Z}^{d-1} \hat{X}_{d+1} - \hat{X}_1 \hat{Z}^{d-1} \hat{Y}_{d+1} + \hat{Y}_{2L-2-d} \hat{Z}^{d-1} \hat{X}_{2L-2} - \hat{X}_{2L-2-d} \hat{Z}^{d-1} \hat{Y}_{2L-2} \right)$$

**Trotterized to minimize circuit depth for a given level of precision.**

**Confinement means finite correlation length : Max d operators are limited**

# Strong Coupling Vacuum – Why?



Build on top of strong-coupling vacuum where long-distance physics is correct  
- limit “workload” to correlated regions.

$g = \text{infinity}$  or  $\text{Hopping} = 0$  – same wavefunction

# Scalable Operators: Circuits

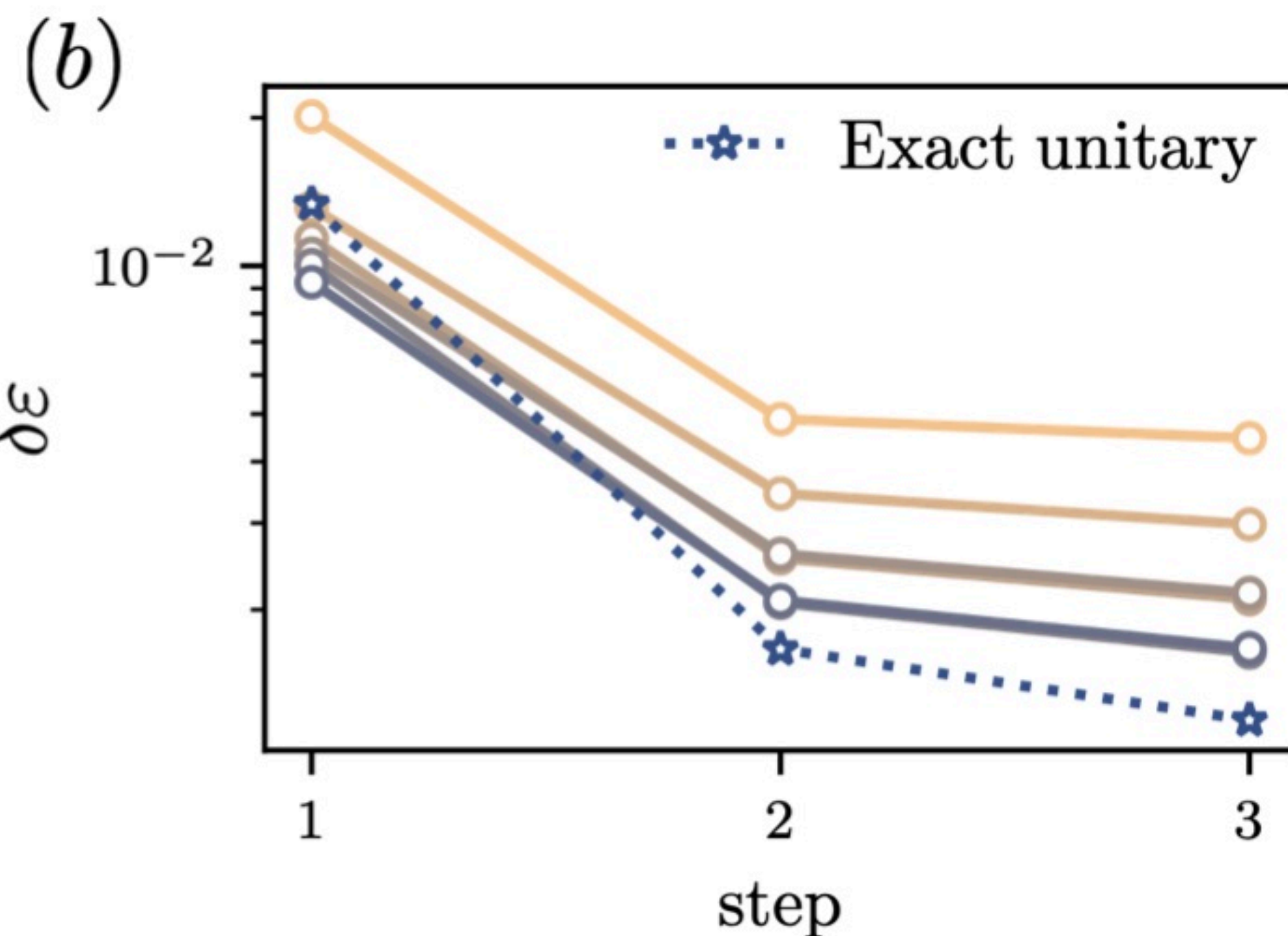
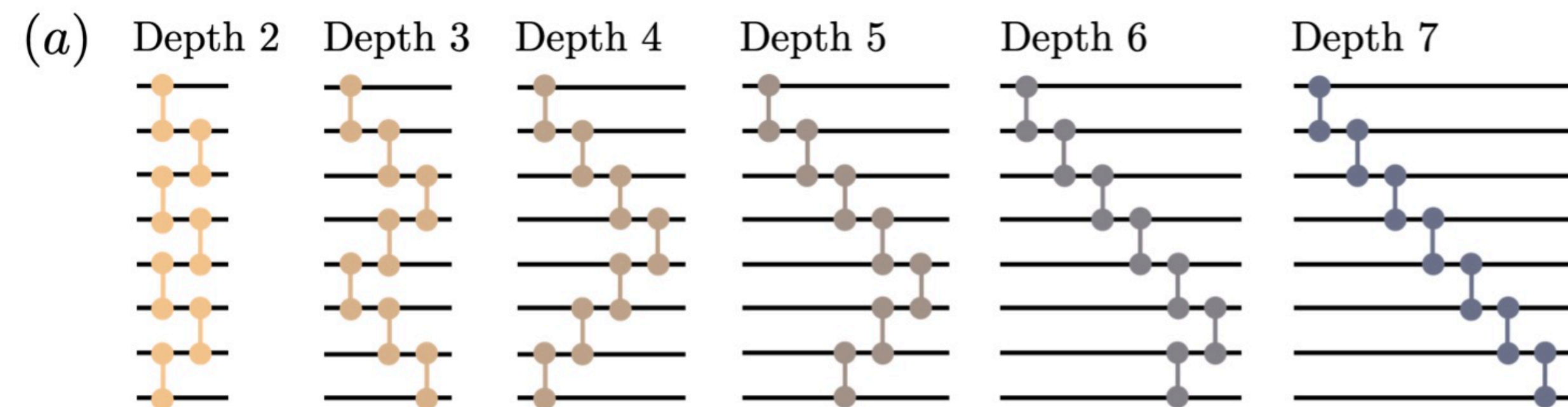
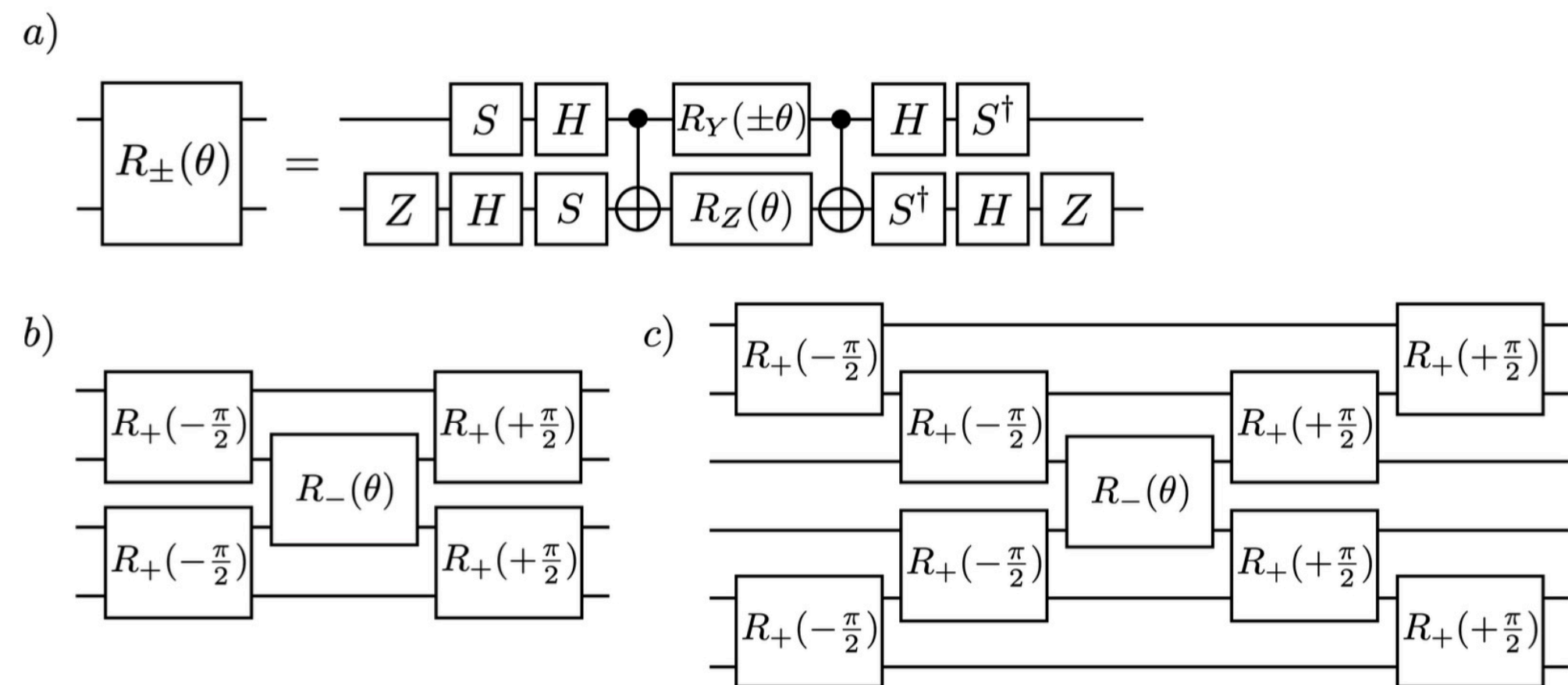


FIG. 3. (a) The definition of the  $R_{\pm}(\theta)$  gate, which implements  $\exp[i\theta/2(\hat{X}\hat{Y} \pm \hat{Y}\hat{X})]$ . The  $R_{\pm}(\theta)$  gate is used to implement (b)  $\exp[-i\theta/2(\hat{X}\hat{Z}^2\hat{Y} - \hat{Y}\hat{Z}^2\hat{X})]$  and (c)  $\exp[i\theta/2(\hat{X}\hat{Z}^4\hat{Y} - \hat{Y}\hat{Z}^4\hat{X})]$  (note the change in sign).

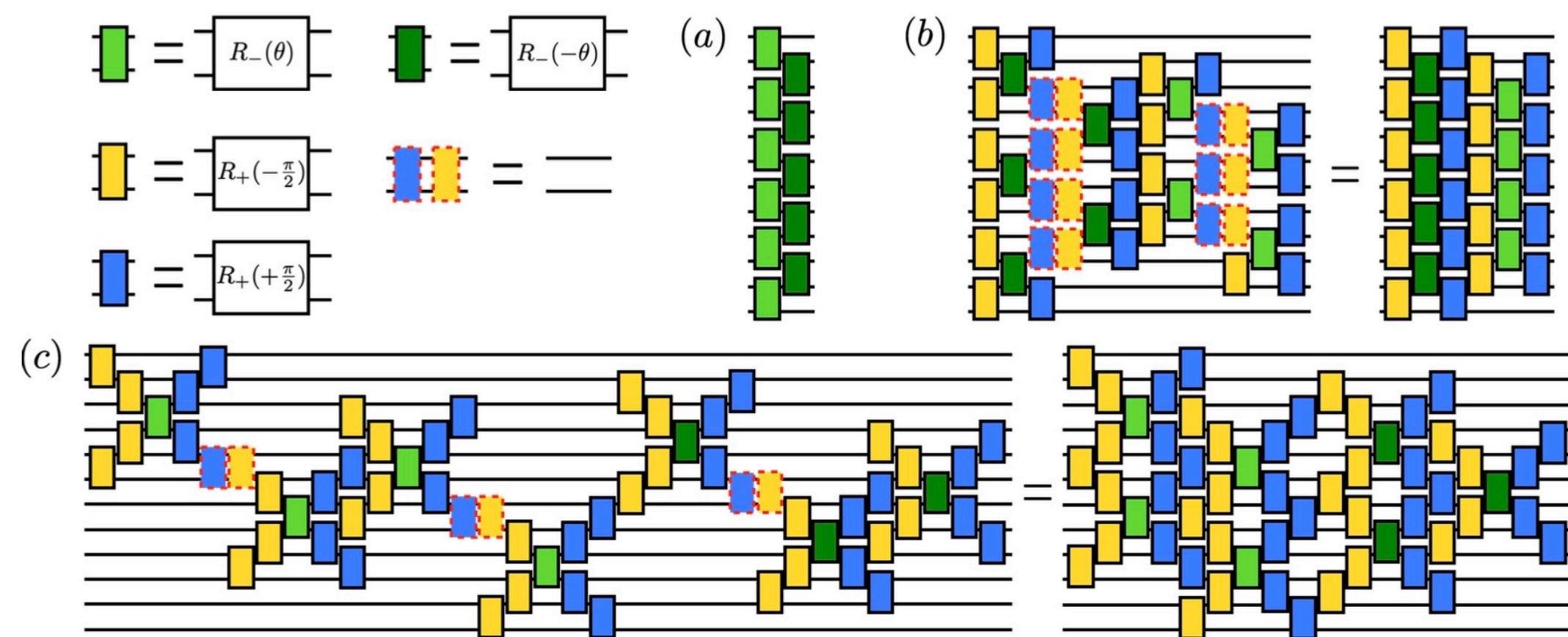
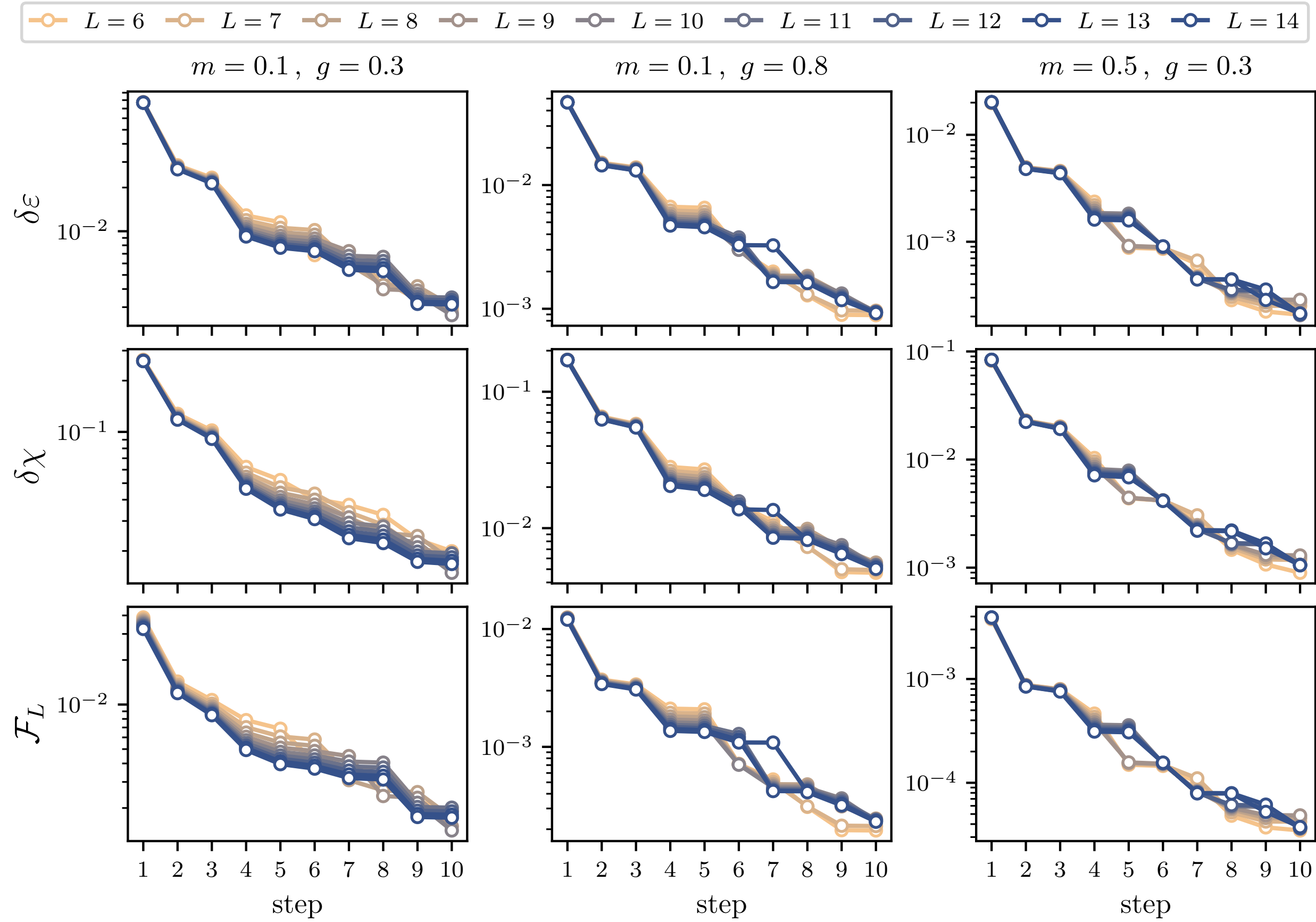


FIG. 4. Simplifications of quantum circuits for the Trotterized unitaries corresponding to (a)  $\hat{O}_{mh}^V(1)$ , (b)  $\hat{O}_{mh}^V(3)$ , and (c)  $\hat{O}_{mh}^V(5)$  for  $L = 6$ , as explained in the main text. Cancellations between  $R_+(\pm\pi/2)$  are highlighted with red-dashed-outlined boxes.

# Scalable Operators: Convergence of Layers

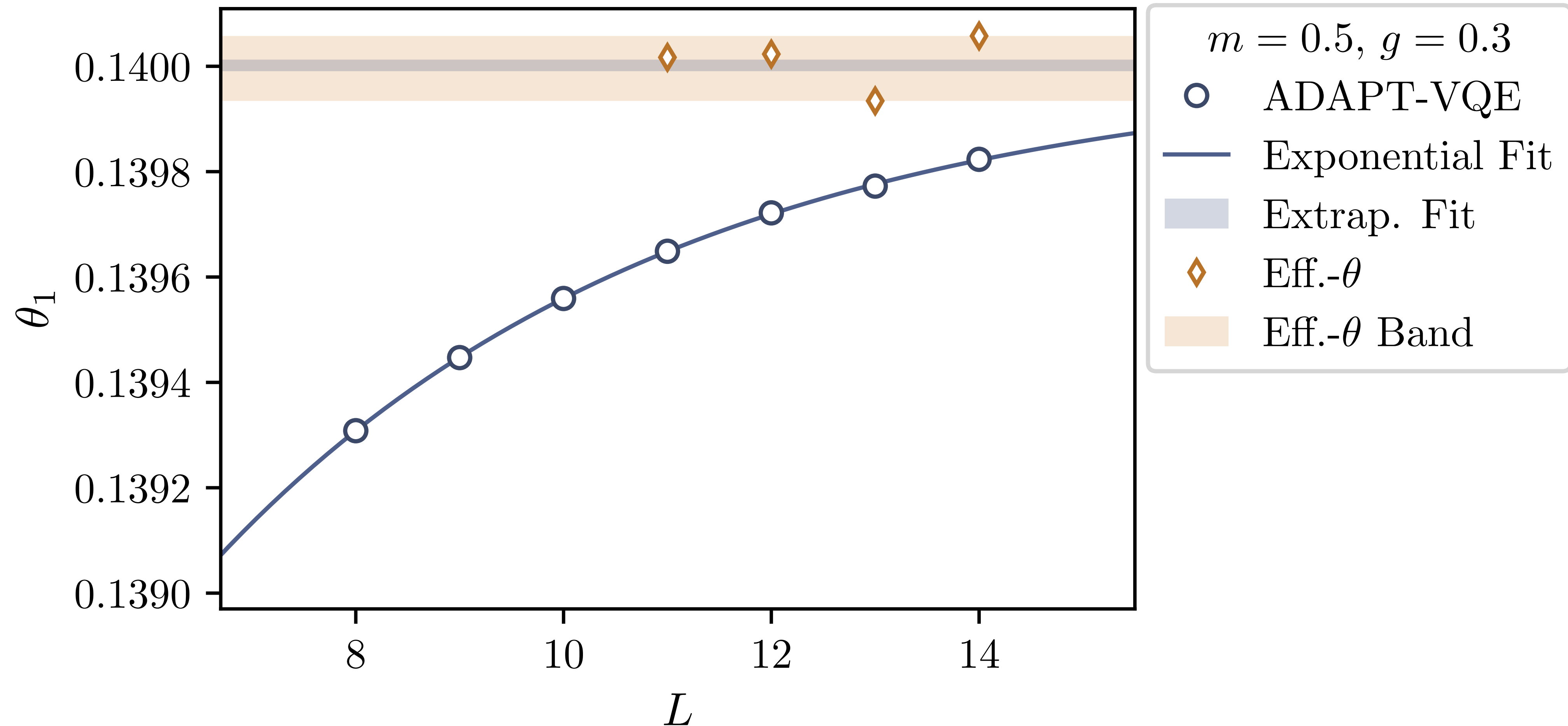


$L \setminus \theta_i$	$\hat{O}_{mh}^V(1)$	$\hat{O}_{mh}^V(3)$	$\hat{O}_{mh}^V(5)$	$\hat{O}_{mh}^V(1)$	$\hat{O}_{mh}^V(7)$	$\hat{O}_{mh}^S(0,1)$	$\hat{O}_{mh}^V(7)$
6	0.18426	-0.03540	0.00731	0.11866	–	0.06895	-0.00182
7	0.18440	-0.03574	0.00729	0.11864	–	0.06867	-0.00177
8	0.13931	-0.03727	0.00760	0.08870	–	0.06925	-0.00183
9	0.13945	-0.03714	0.00755	0.08849	–	0.06904	-0.00180
10	0.13956	-0.03703	0.00752	0.08832	-0.00178	0.06888	–
11	0.13965	-0.03695	0.00749	0.08819	-0.00177	0.06875	–
12	0.13972	-0.03688	0.00747	0.08808	-0.00176	0.06865	–
13	0.13977	-0.03683	0.00745	0.08800	-0.00175	0.06856	–
14	0.13982	-0.03678	0.00744	0.08793	-0.00174	0.06849	–
$\infty$	0.1400	-0.0366	0.0074	0.0877	-0.0017	0.0682	–

Global Optimization of parameters at each step



# Scalable Operators: Convergence of Parameters



# Decoherence Renormalization

## Mitigating Depolarizing Noise on Quantum Computers with Noise-Estimation Circuits

Miroslav Urbanek, Benjamin Nachman, Vincent R. Pascuzzi, Andre He, Christian W. Bauer, and Wibe A. de Jong  
Phys. Rev. Lett. **127**, 270502 – Published 27 December 2021

## Self-mitigating Trotter circuits for SU(2) lattice gauge theory on a quantum computer

Sarmed A Rahman, Randy Lewis, Emanuele Mendicelli, and Sarah Powell  
*Department of Physics and Astronomy, York University,  
Toronto, Ontario, Canada, M3J 1P3*

(Dated: May 2022. Updated: October 2022.)

Works well today .....

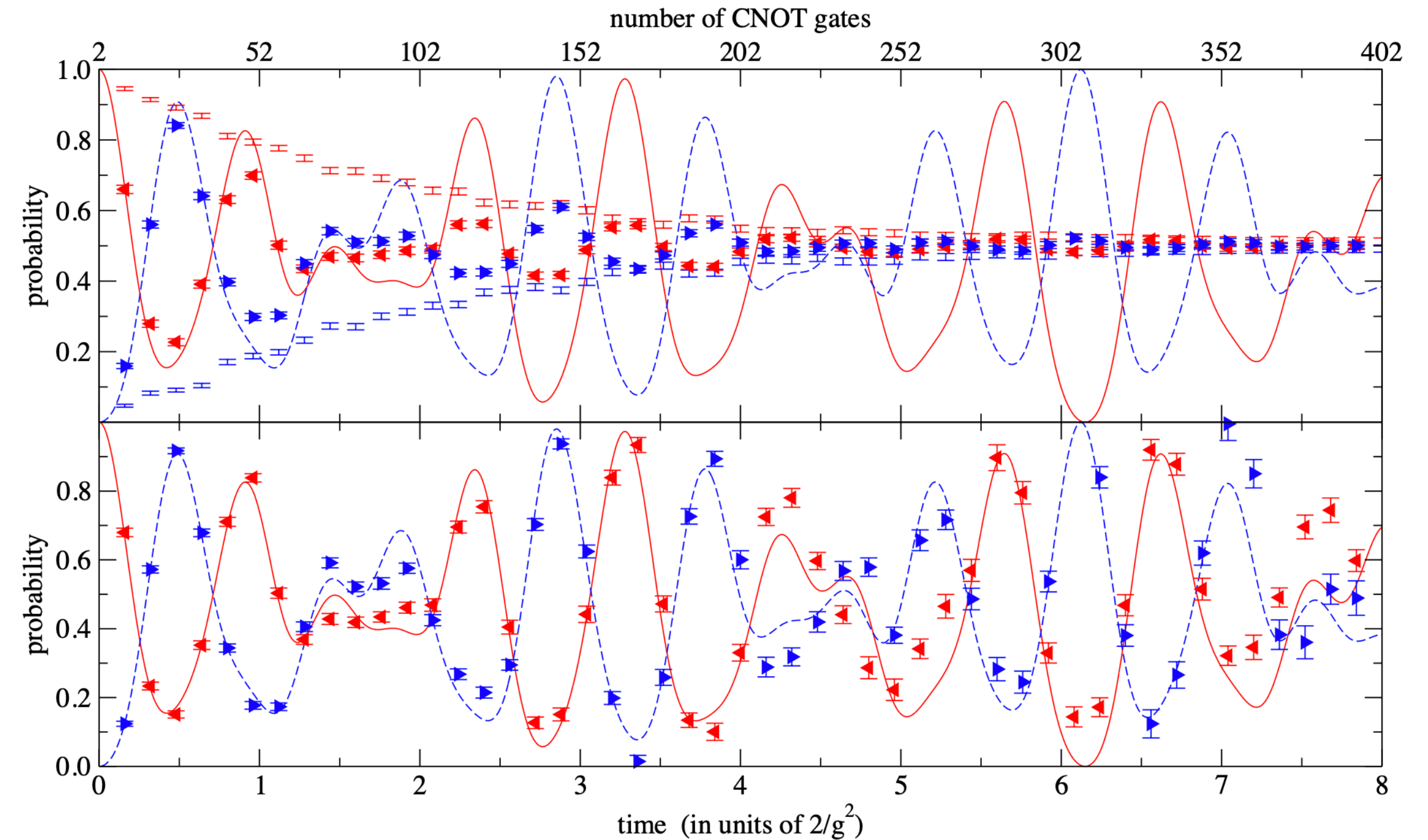
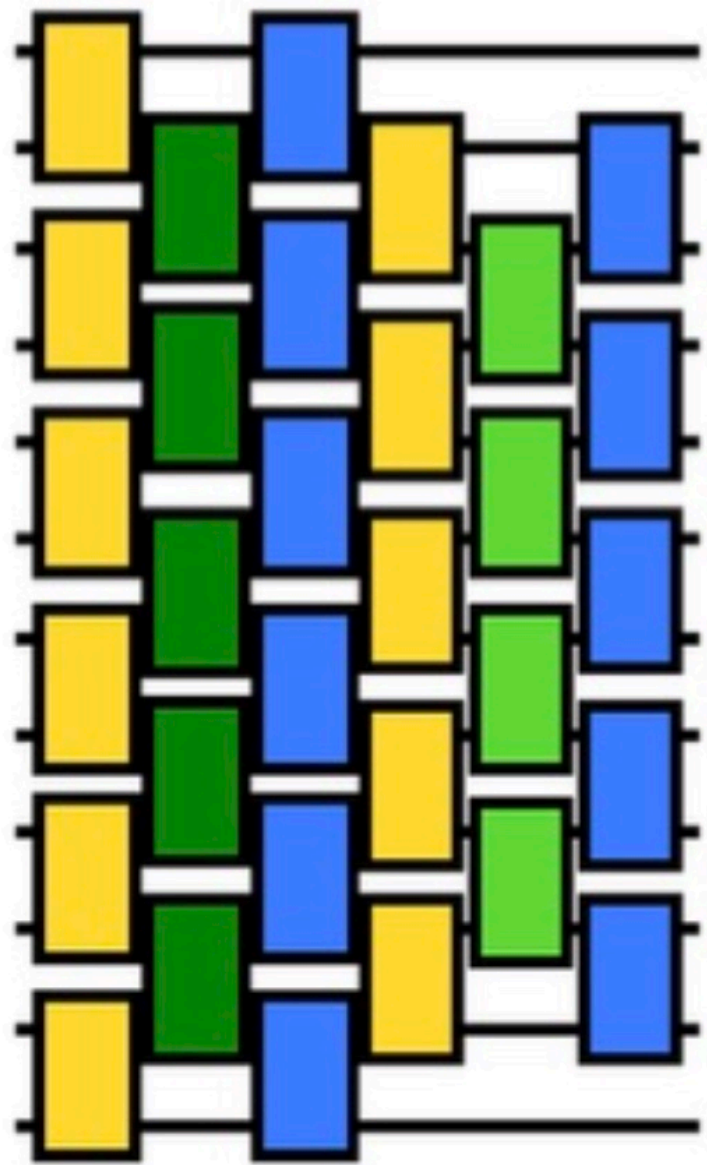


FIG. 3. Time evolution by self-mitigation on a two-plaquette lattice from the initial state of Fig. 1 with gauge coupling  $x = 2.0$  and time step  $dt = 0.08$ . In both panels, the red solid (blue dashed) curve is the exact probability of the left (right) plaquette being measured to have  $j = \frac{1}{2}$ . **Upper panel:** The red left-pointing (blue right-pointing) triangles are the physics data computed from the `ibm_lagos` quantum processor. The red (blue) error bars without symbols are the mitigation data computed on `ibm_lagos` from the same circuit but with half the steps forward in time and then half backward in time. **Lower panel:** The triangles are the physics results obtained by applying Eq. (8) to the data from the upper panel.

# Operator Decoherence Renormalization

## Localized Error Mitigation for Localized Observables

Errors in New York should not impact simulations in Seattle, i.e. errors are in the laboratory  
 ..... use local mitigation strategies



Angles from ADAPT-VQE  
 Vacuum of 1+1 QED

Physics wavefunction

Angles = 0 [Clifford]

Mitigation wavefunction

Strong-coupling vacuum

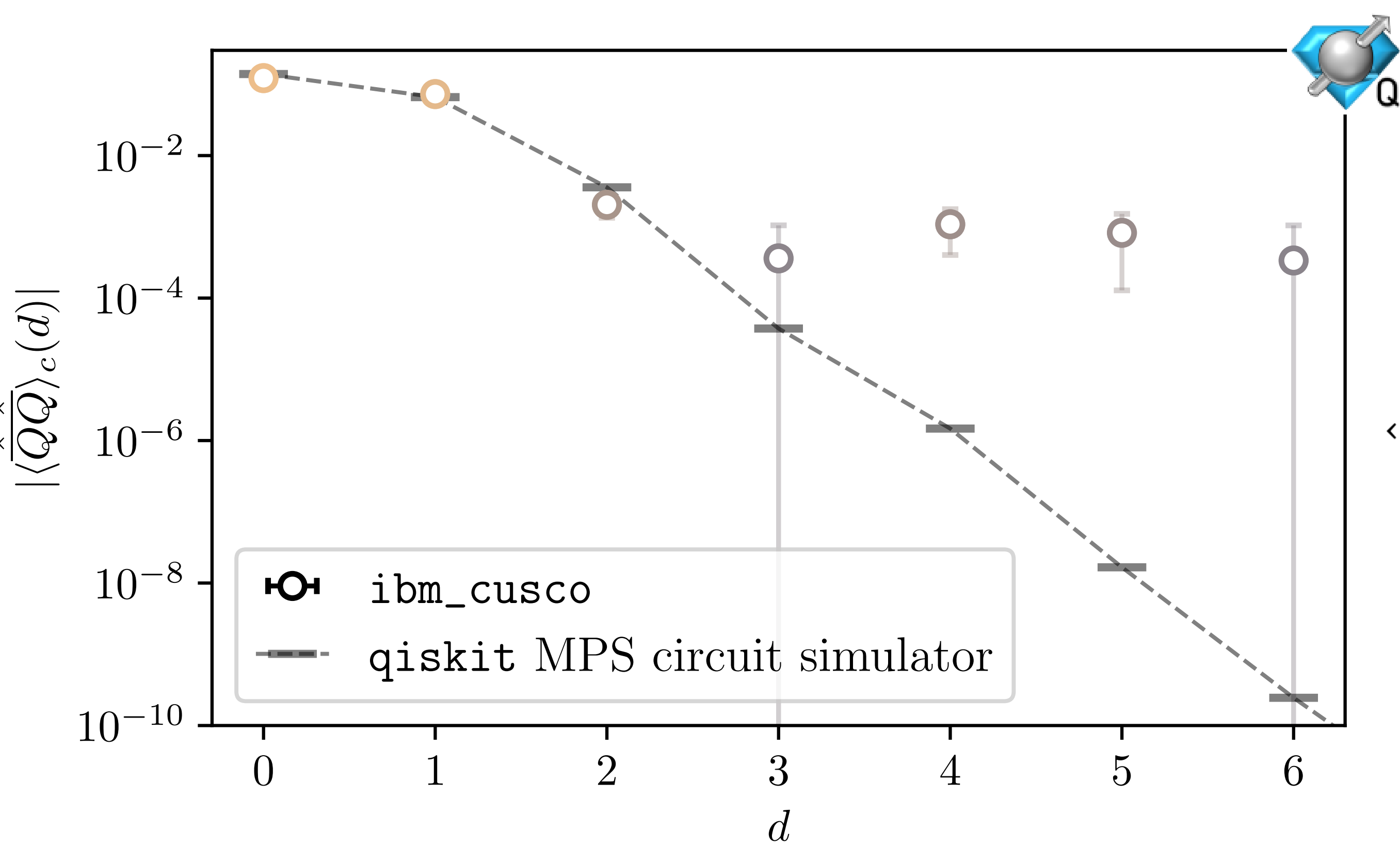
Known values for observables  
 of interest

$$\rho \rightarrow \sum_{i=1}^{4^N} \eta_i \hat{P}_i \rho \hat{P}_i \quad \langle \hat{O} \rangle_{\text{meas}} = \sum_{i=1}^{4^N} \eta_i \text{Tr} \left( \hat{P}_i \hat{O} \hat{P}_i \rho \right) \quad \langle \hat{O} \rangle_{\text{meas}} = (1 - \eta_O) \langle \hat{O} \rangle_{\text{pred}}$$

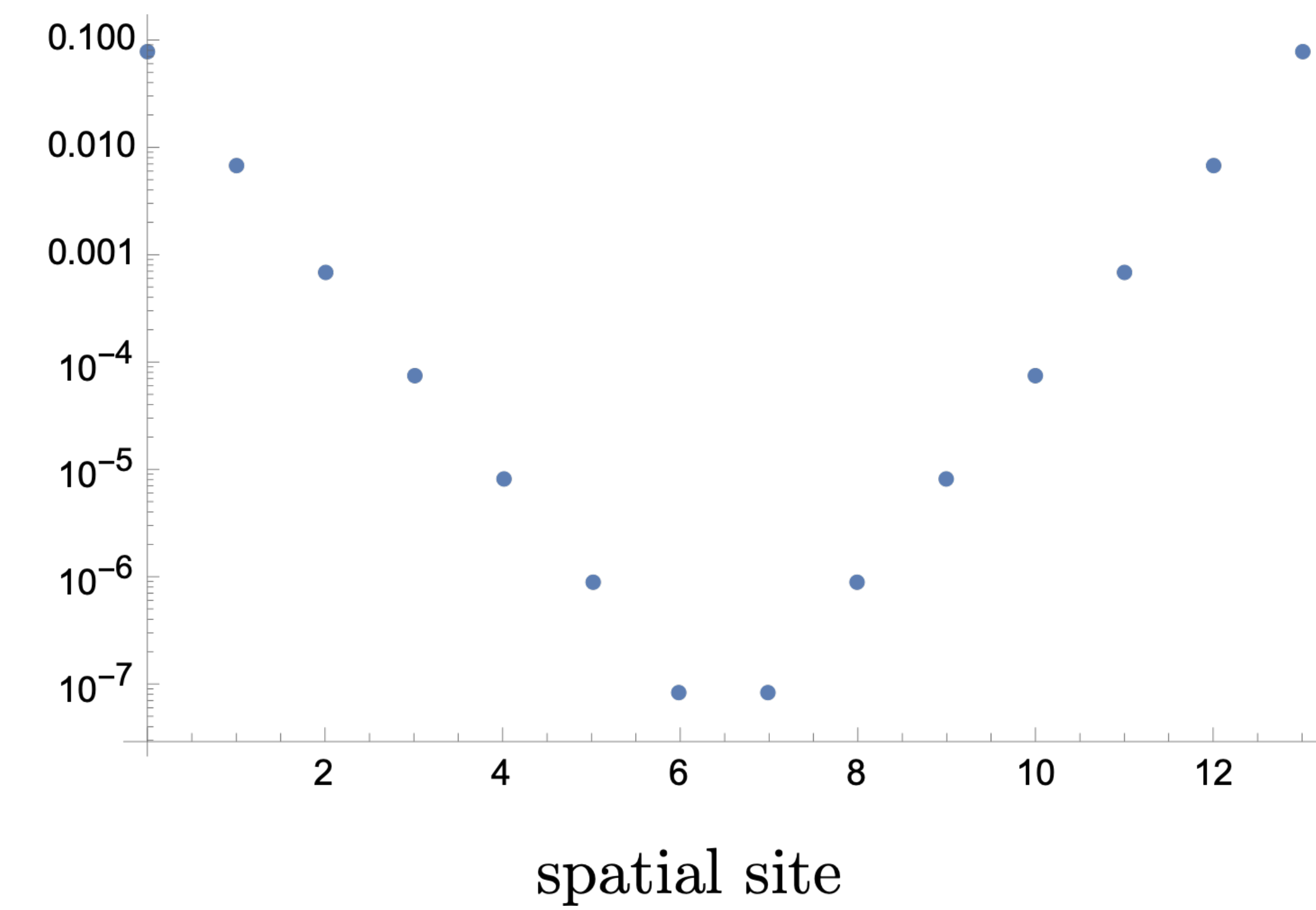
For each different Pauli-string operator forming observable, e.g., ZZ

# Charge-Charge Correlations

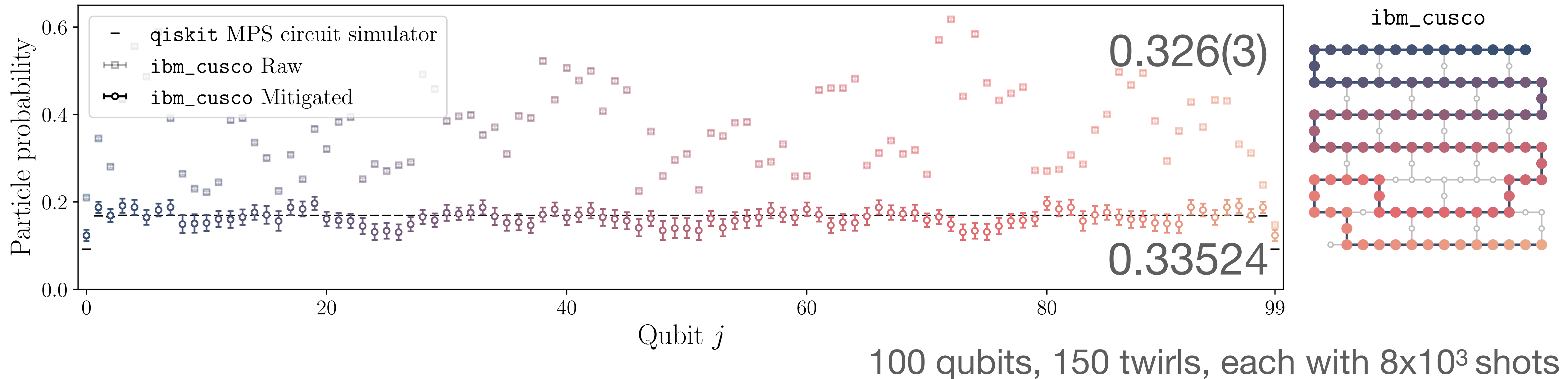
Twirls and statistics limited



$m = 0.5, g = 0.3, L = 14$



# Production on IBM's 127-Qubit Eagles



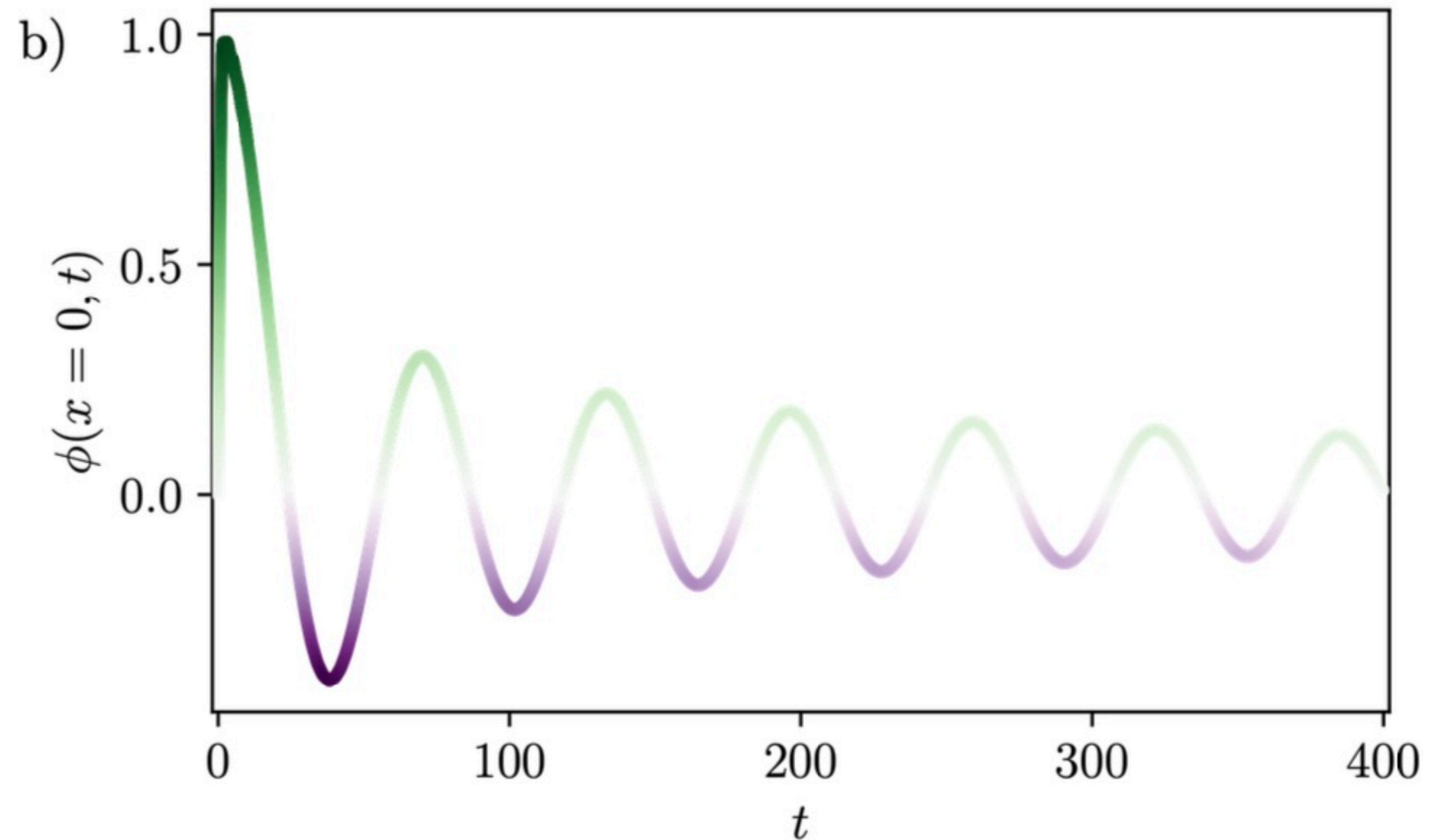
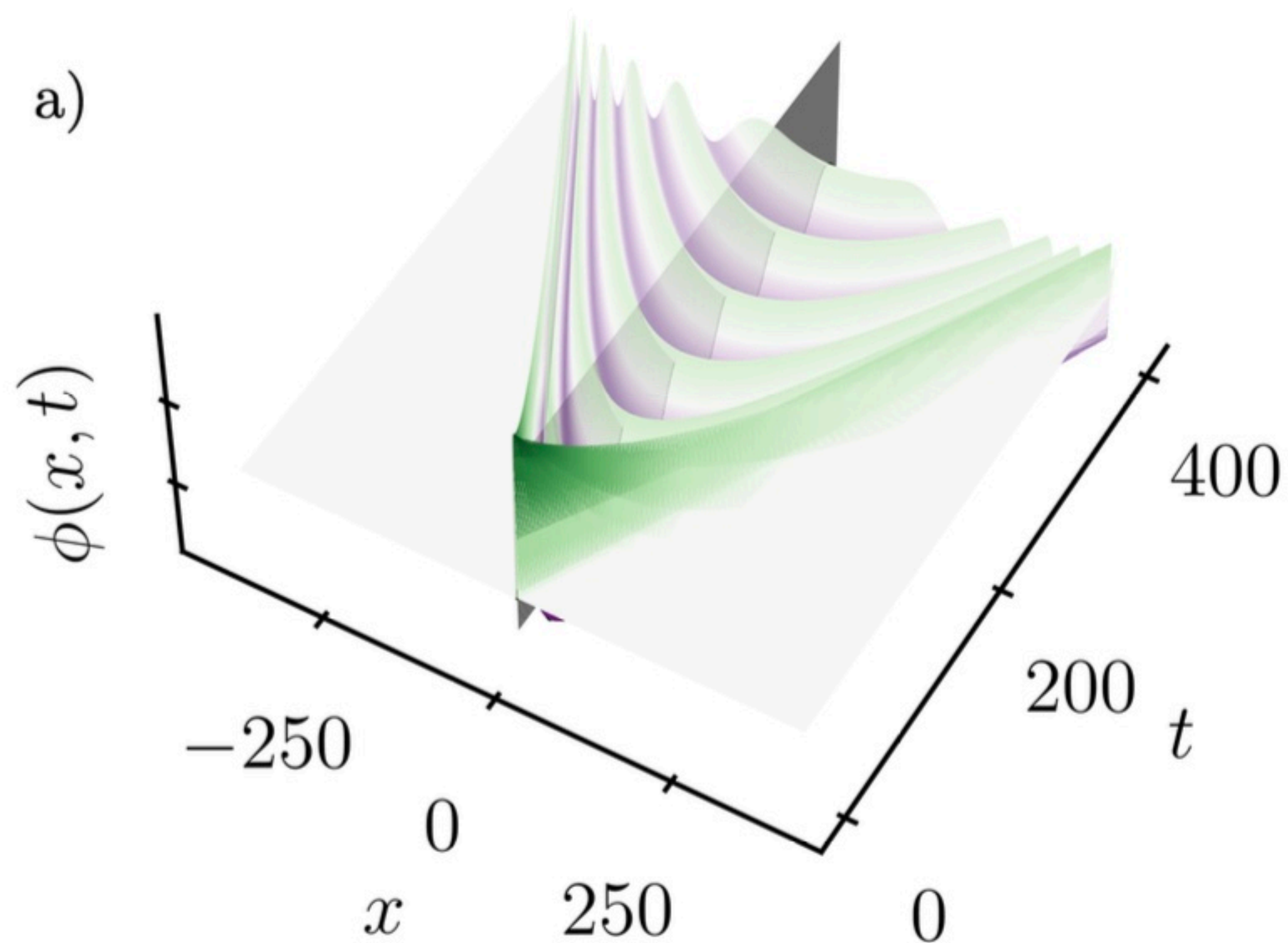
- **SC-ADAPT-VQE**
  - 2-layers, expect systematic errors at  $\sim 1\%$ ,  $\sim 700$  CNOTS
  - 3-layers explored  $\sim 1300$  CNOTS
- Operator decoherence renormalization (ODR)
  - With and without readout error mitigation
- Run on MPS for classical comparison for  $L \leq 100$
- Modest number of twirls as circuit elements repeat -  $\sim 150$

# Wavepacket Preparation

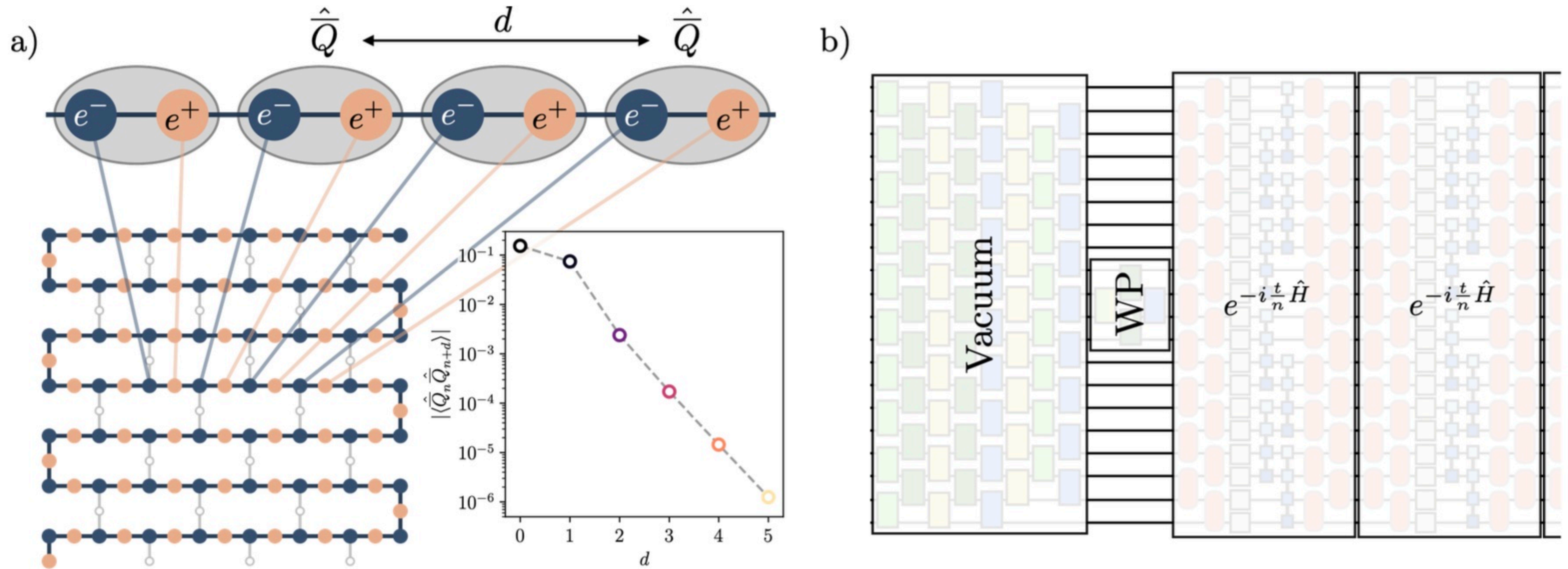
## Naive Expectations

Preparing beams of "protons"

- we don't know their wavefunction from first principles
- Let the system do it for us!



# The Protocol

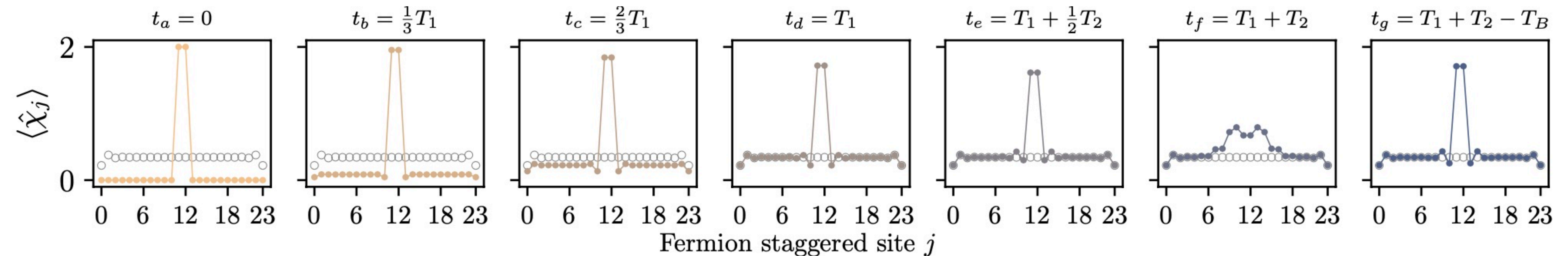


# Wavepacket Preparation

## Modest-sized Wave Packet to “Match” to

$$|\psi_{\text{WP}}\rangle_{\text{init}} = \hat{X}_{L-1} \hat{X}_L |\Omega_0\rangle$$

$$\hat{H}_{\text{ad}}(t) = \begin{cases} \hat{H}_m + \hat{H}_{el} + \frac{t}{T_1} \left[ \hat{H}_{kin} - \frac{1}{2} (\sigma_{L-2}^+ \sigma_{L-1}^- + \sigma_L^+ \sigma_{L+1}^- + \text{h.c.}) \right] & 0 < t \leq T_1, \\ \hat{H}_m + \hat{H}_{el} + \hat{H}_{kin} - \left( 1 - \frac{t-T_1}{T_2} \right) \frac{1}{2} (\sigma_{L-2}^+ \sigma_{L-1}^- + \sigma_L^+ \sigma_{L+1}^- + \text{h.c.}) & T_1 < t \leq T_1 + T_2. \end{cases}$$



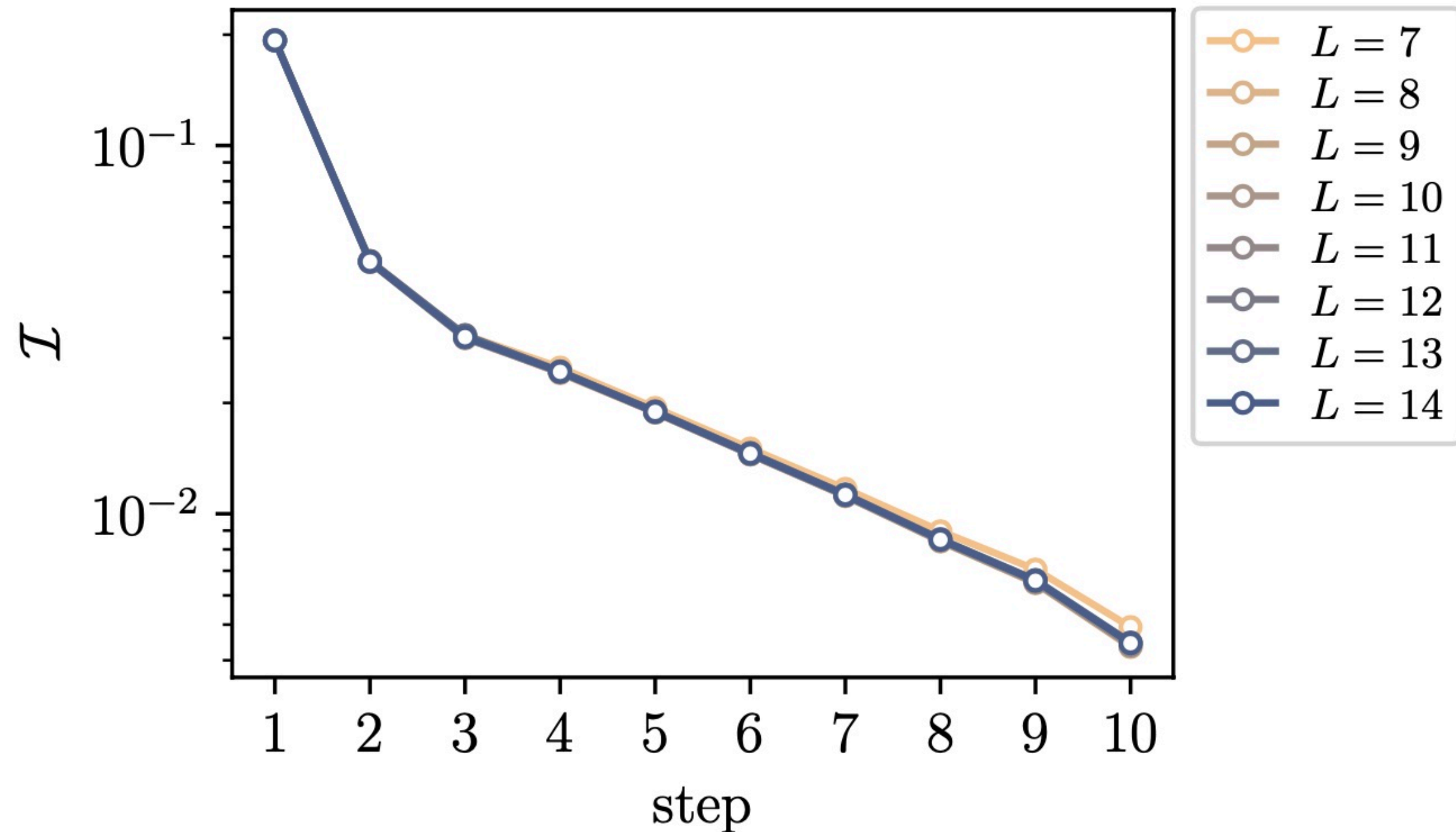
# Classical Simulations



# Wavepacket Preparation on the Vacuum

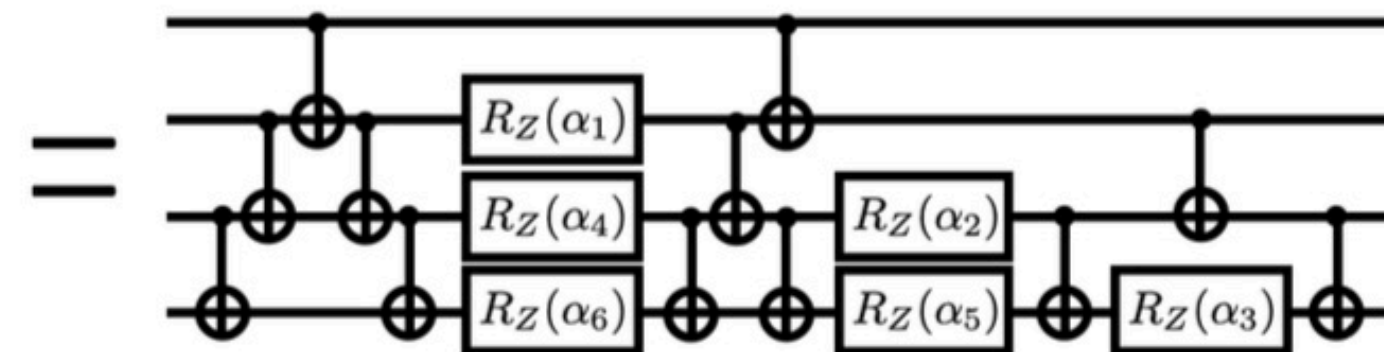
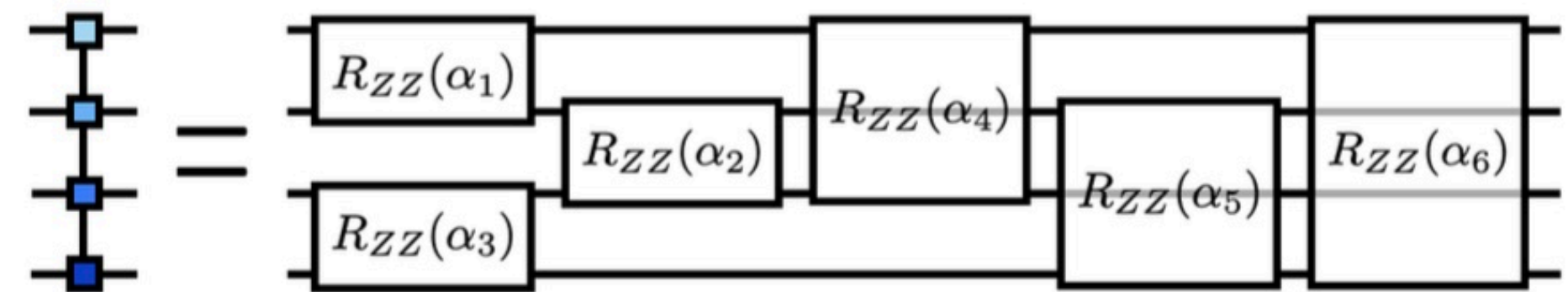
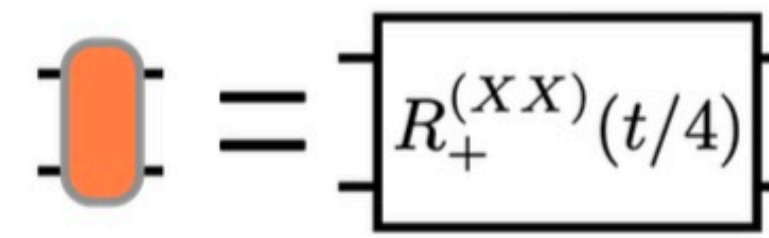
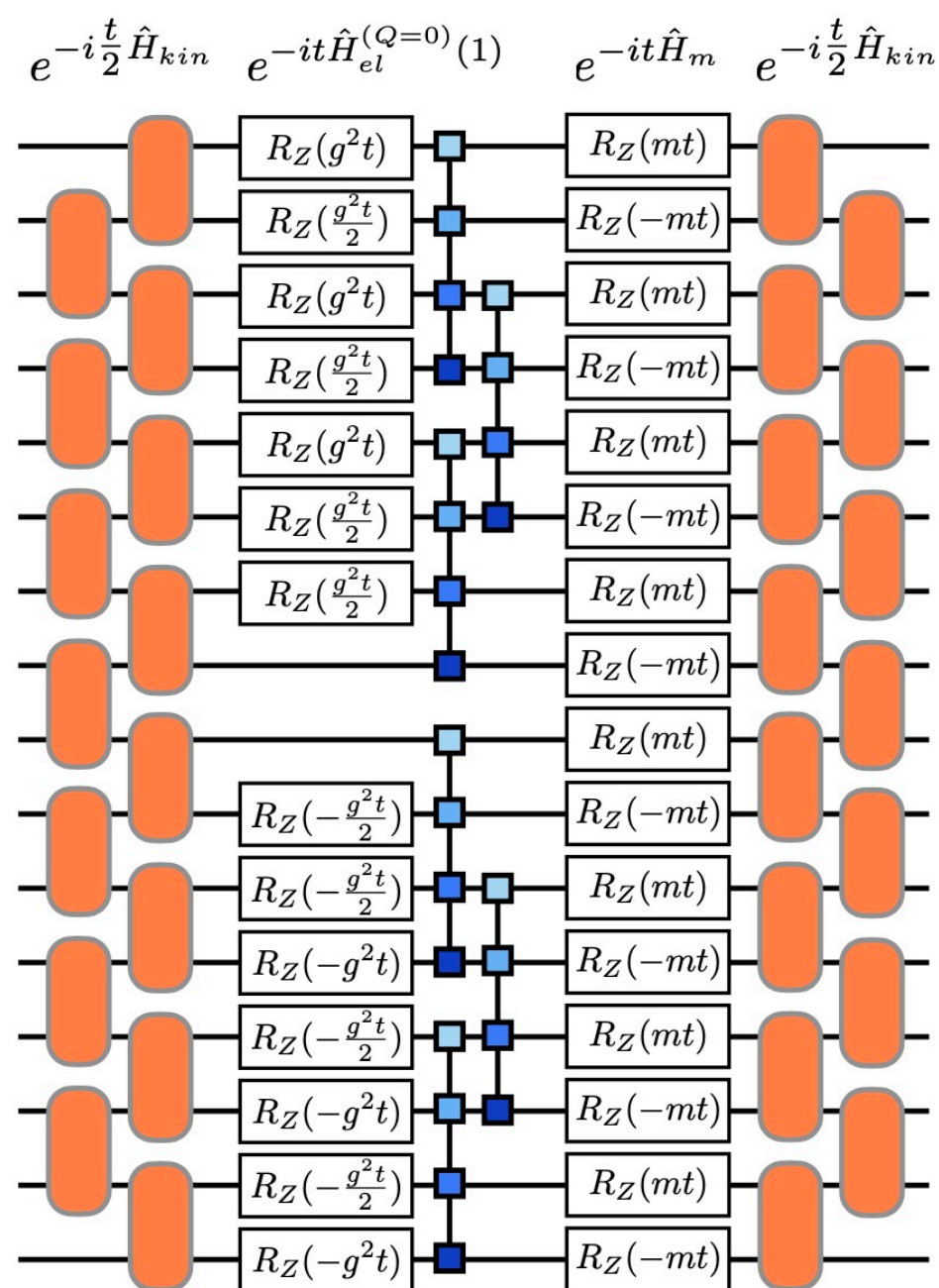
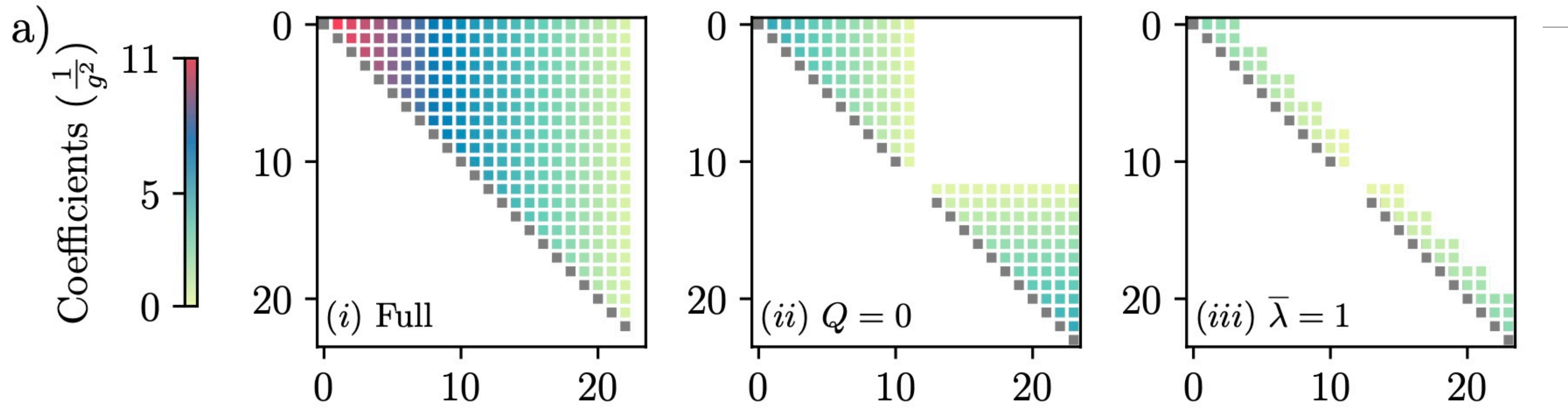
## Matching to Quantum Circuits

$$\begin{aligned} \{\hat{O}\}_{\text{WP}} &= \{\hat{O}_{mh}(n, d), \hat{O}_h(n, d), \hat{O}_m(n)\}, \\ \hat{O}_{mh}(n, d) &= \frac{1}{2} \left[ \hat{X}_{L-n} \hat{Z}^{d-1} \hat{Y}_{L-n+d} - \hat{Y}_{L-n} \hat{Z}^{d-1} \hat{X}_{L-n+d} + (-1)^{d+1} (1 - \delta_{L-n, \gamma}) \left( \hat{X}_{\gamma} \hat{Z}^{d-1} \hat{Y}_{\gamma+d} - \hat{Y}_{\gamma} \hat{Z}^{d-1} \hat{X}_{\gamma+d} \right) \right], \\ \hat{O}_h(n, d) &= \frac{1}{2} \left[ \hat{X}_{L-n} \hat{Z}^{d-1} \hat{X}_{L-n+d} + \hat{Y}_{L-n} \hat{Z}^{d-1} \hat{Y}_{L-n+d} + (-1)^{d+1} (1 - \delta_{L-n, \gamma}) \left( \hat{X}_{\gamma} \hat{Z}^{d-1} \hat{X}_{\gamma+d} + \hat{Y}_{\gamma} \hat{Z}^{d-1} \hat{Y}_{\gamma+d} \right) \right], \end{aligned} \quad (12)$$

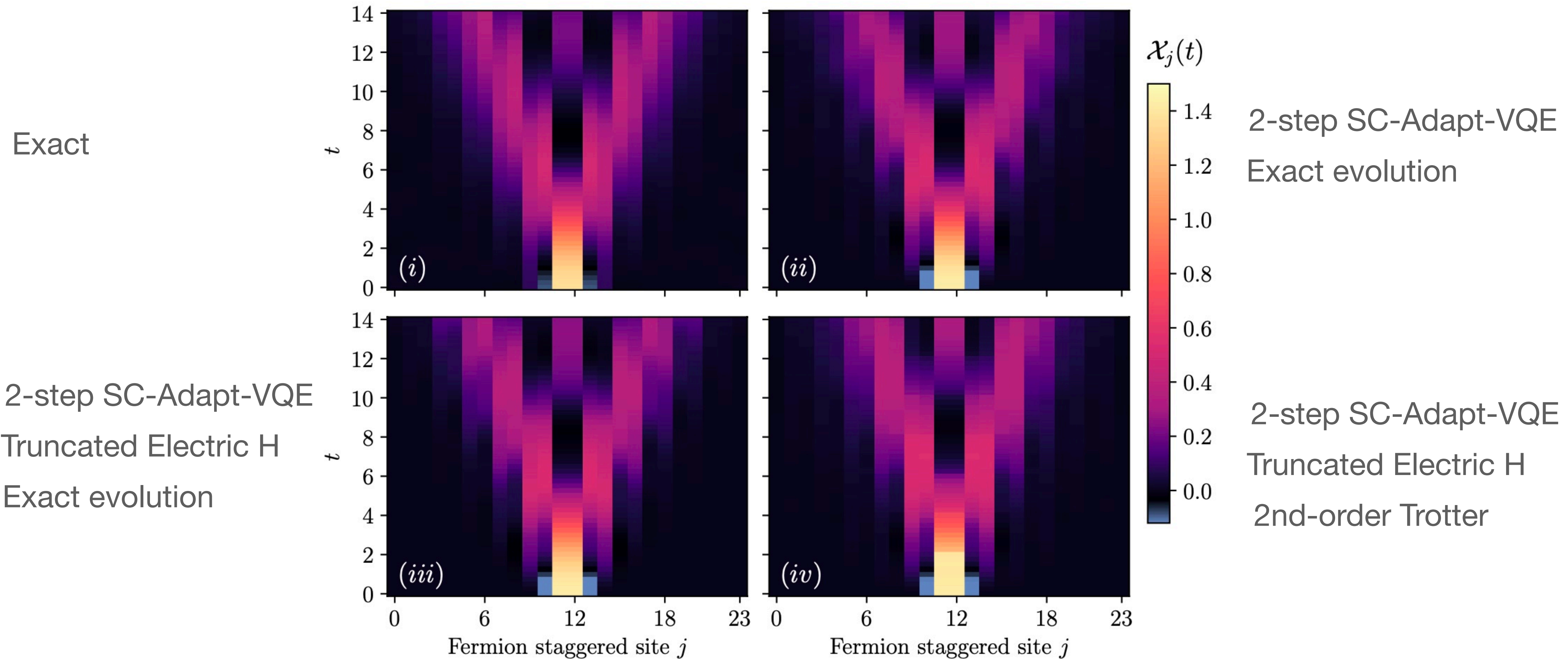


$$\mathcal{I} = 1 - |\langle \psi_{\text{WP}} | \psi_{\text{ansatz}} \rangle|^2$$

# Truncations in Electric Interactions Confinement



# Verifying Systematic Approximations (Classical)



# Production Details using IBM's Torino

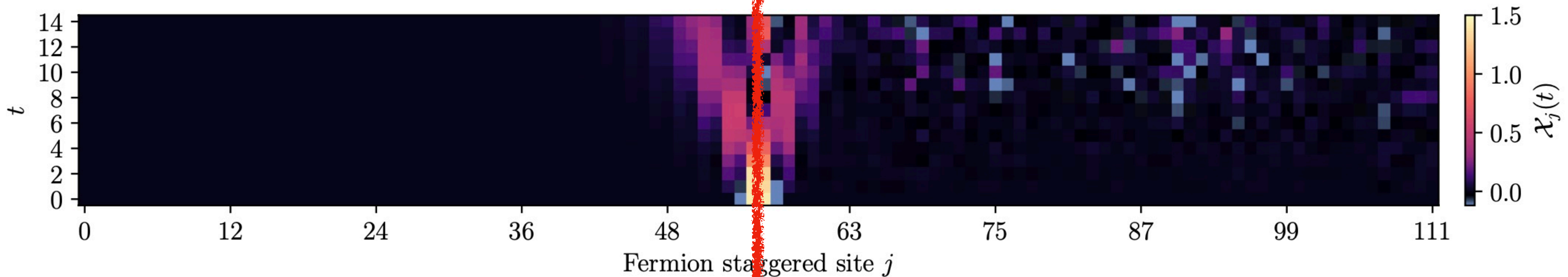
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$t$	$N_T$	# of CNOTs (per $t$ )	CNOT depth (per $t$ )	# of distinct circuits (per $t$ )	# of twirls (per circuit)	# of shots (per twirl)	Executed CNOTs ( $\times 10^9$ )	Total # of shots ( $\times 10^6$ )
1 & 2	2	2,746	70	4	480	8,000	$4 \times 2 \times 10.5$	$4 \times 2 \times 3.8$
3 & 4	4	4,598	120	4	480	8,000	$4 \times 2 \times 17.7$	$4 \times 2 \times 3.8$
5 & 6	6	6,450	170	4	480	8,000	$4 \times 2 \times 24.8$	$4 \times 2 \times 3.8$
7 & 8	8	8,302	220	4	480	8,000	$4 \times 2 \times 31.9$	$4 \times 2 \times 3.8$
9 & 10	10	10,154	270	4	160	8,000	$4 \times 2 \times 13.0$	$4 \times 2 \times 1.3$
11 & 12	12	12,006	320	4	160	8,000	$4 \times 2 \times 15.4$	$4 \times 2 \times 1.3$
13 & 14	14	13,858	370	4	160	8,000	$4 \times 2 \times 17.7$	$4 \times 2 \times 1.3$
<b>Totals</b>							$1.05 \times 10^{12}$	$1.54 \times 10^8$

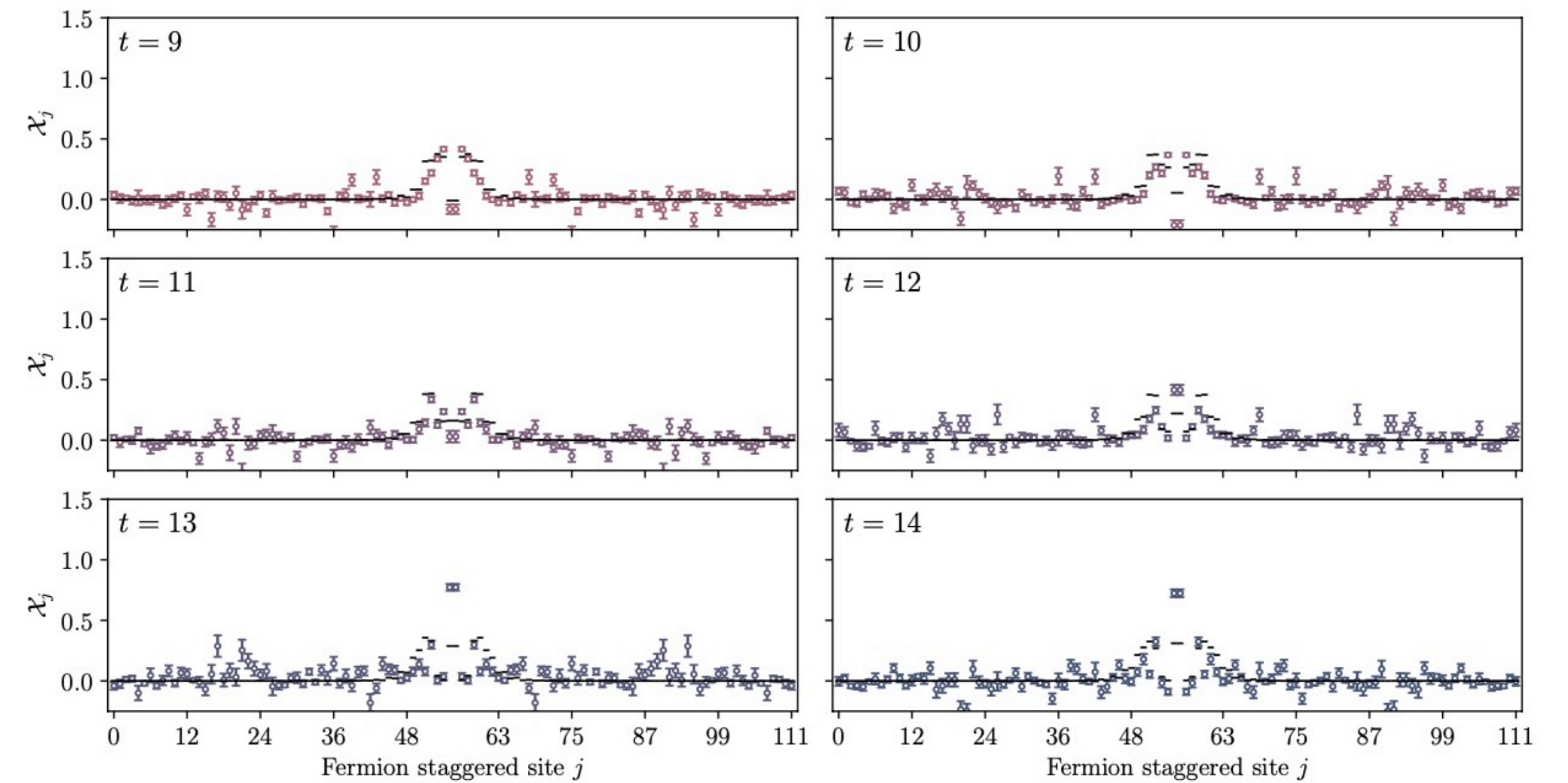
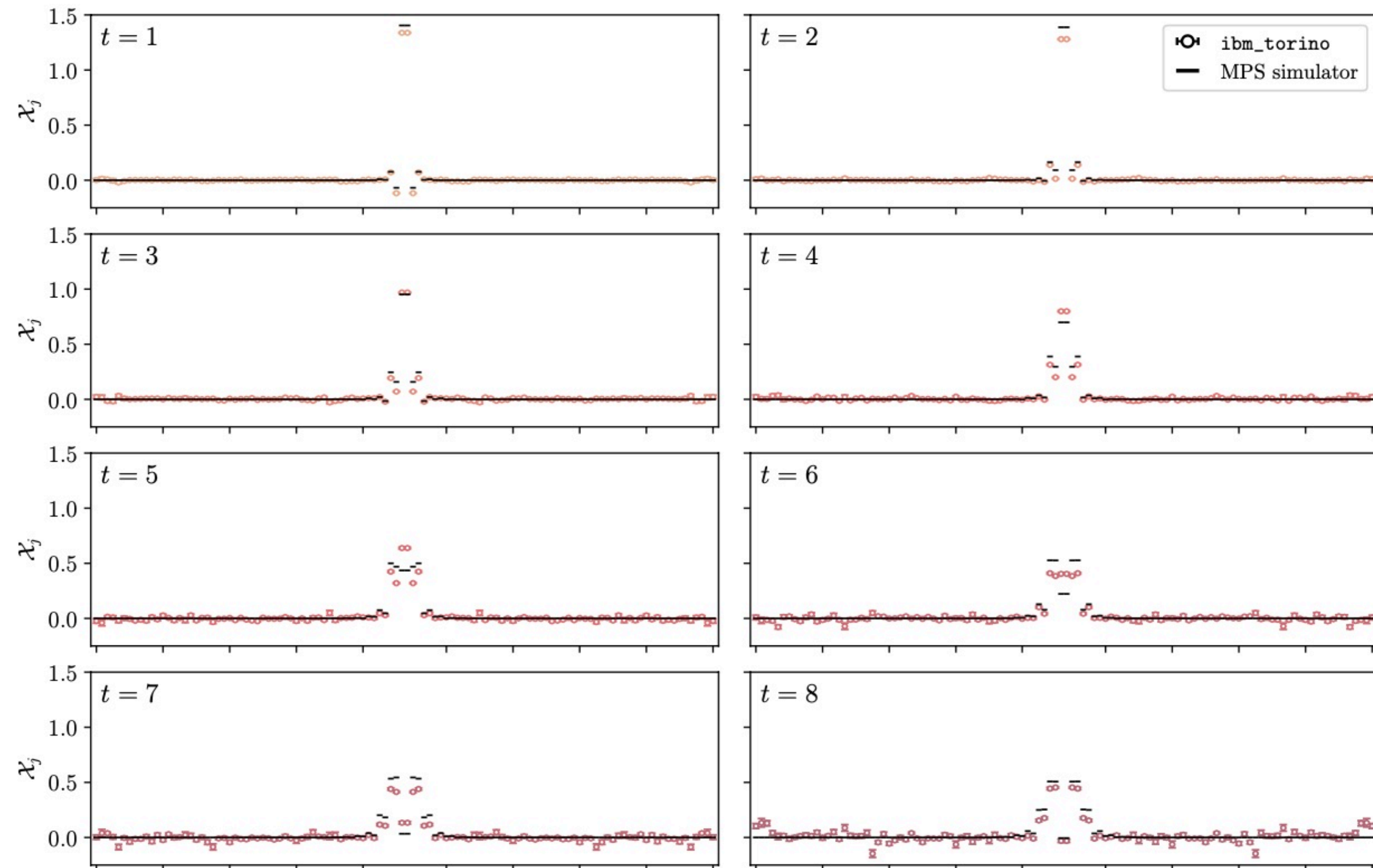
# Results on 112 Qubits with up to 14 Trotter Steps

Classical Expectation

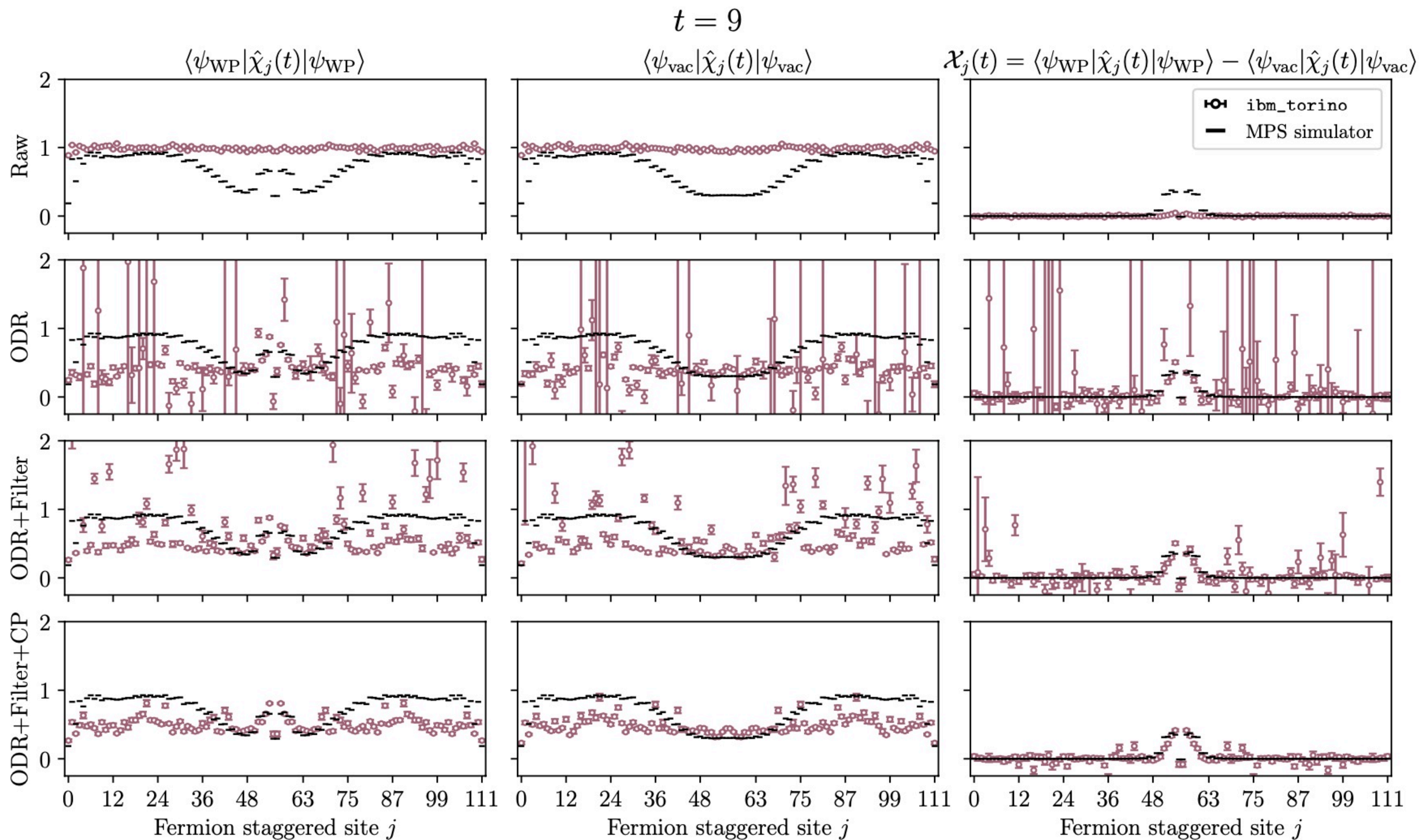
IBM's Quantum Computer - Torino  
Computed



# “Side-By-Side” Comparison



# The Key Role of Error Mitigation



# 1+1D QCD (2022)



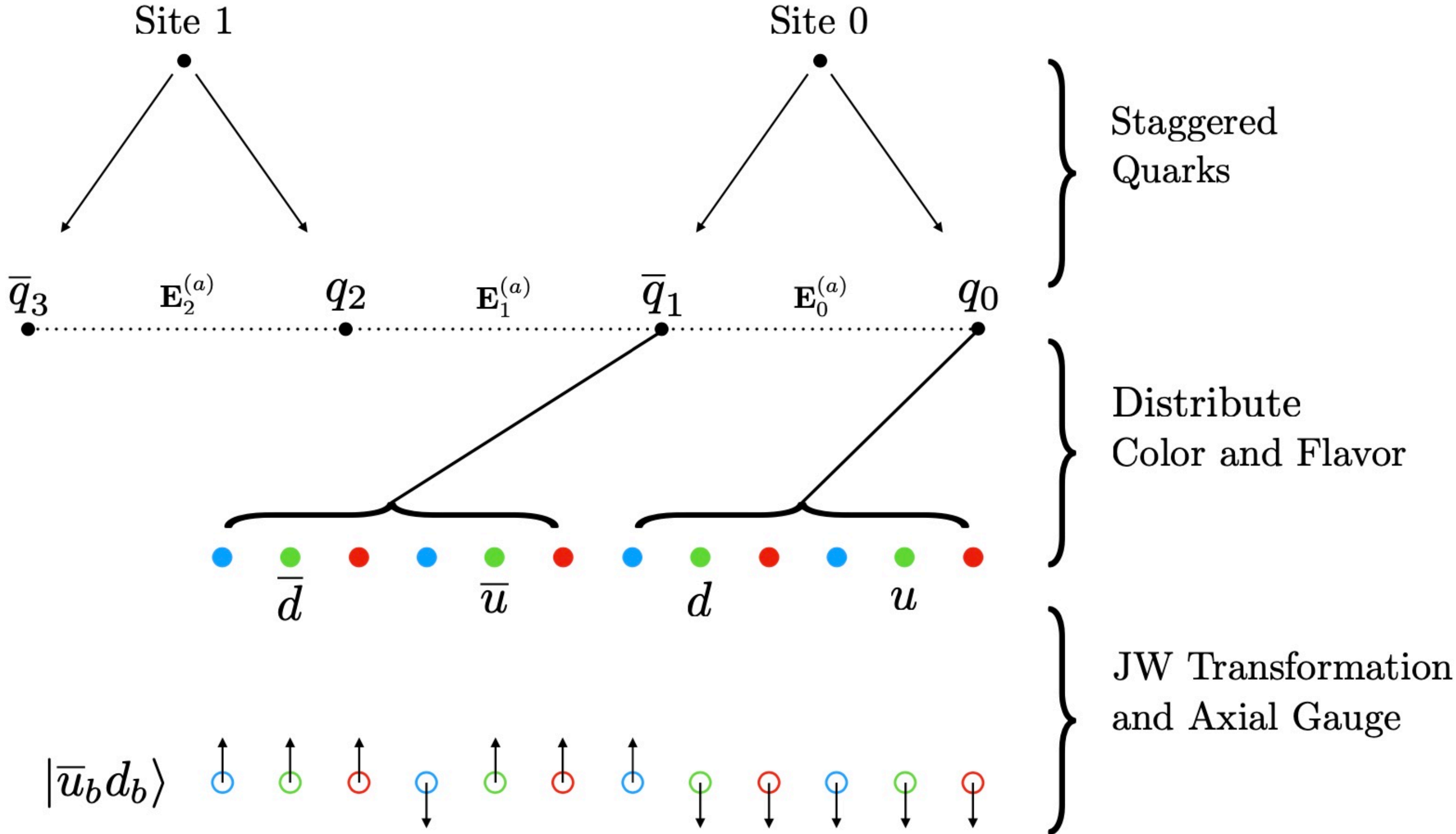
Building on the works of others, Banuls, Dirac, Jansen, Muschik, Lewis, ....

Preparations for quantum simulations of quantum chromodynamics in 1 + 1 dimensions. I. Axial gauge

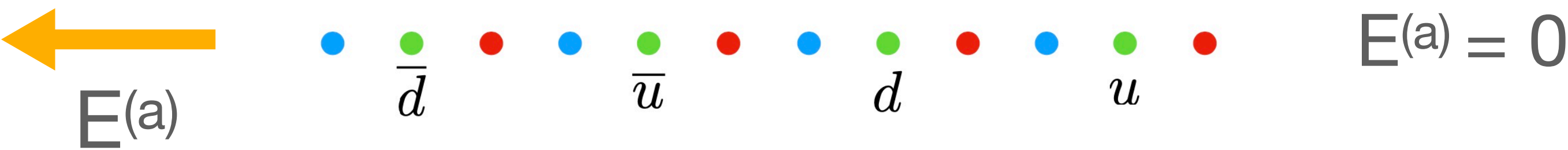
Roland C. Farrell, Ivan A. Chernyshev, Sarah J. M. Powell, Nikita A. Zemlevskiy, Marc Illa, and Martin J. Savage  
 Phys. Rev. D **107**, 054512 – Published 30 March 2023

Preparations for quantum simulations of quantum chromodynamics in 1 + 1 dimensions. II. Single-baryon  $\beta$ -decay in real time

Roland C. Farrell, Ivan A. Chernyshev, Sarah J. M. Powell, Nikita A. Zemlevskiy, Marc Illa, and Martin J. Savage  
 Phys. Rev. D **107**, 054513 – Published 30 March 2023



Color edge states

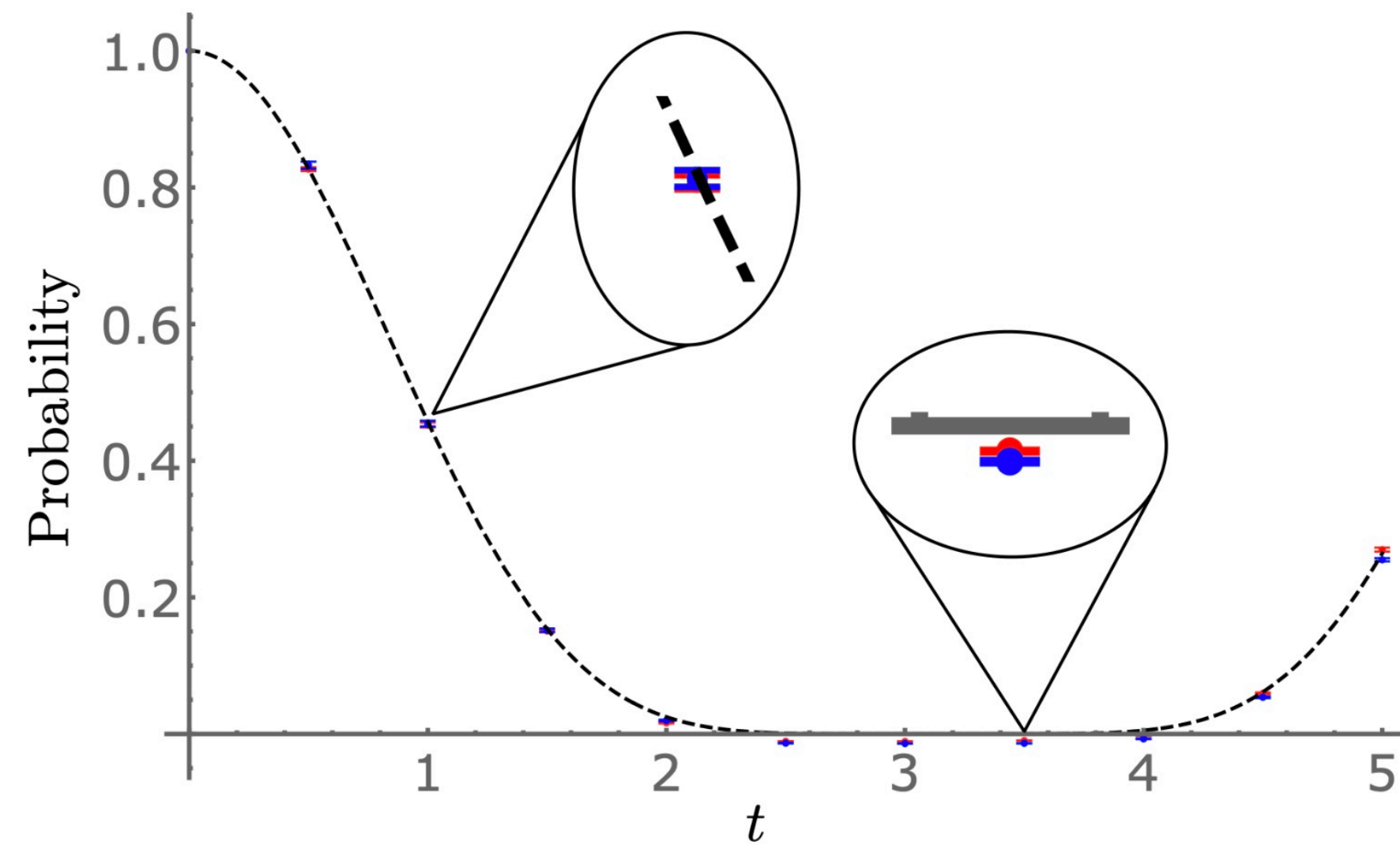




# Simulations using IBM's Quantum Computers

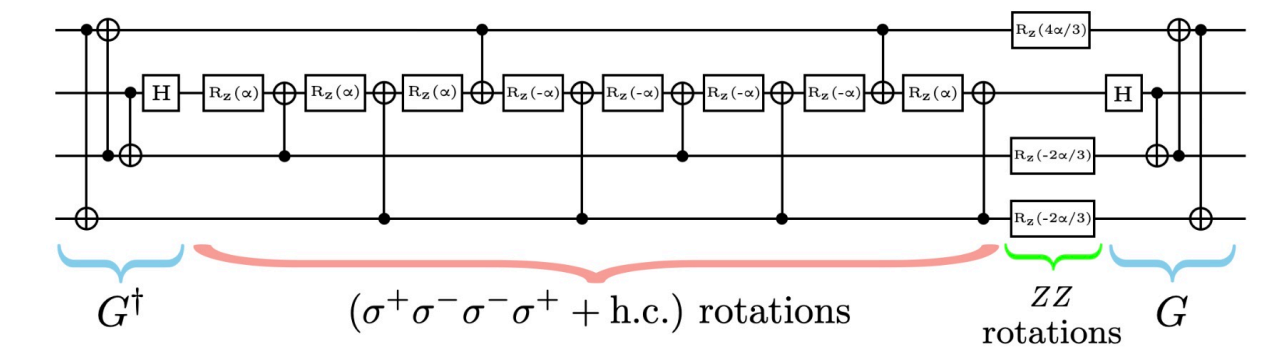
## 1-site, 3 colors, 1 flavor

Trivial Vacuum-to-Vacuum

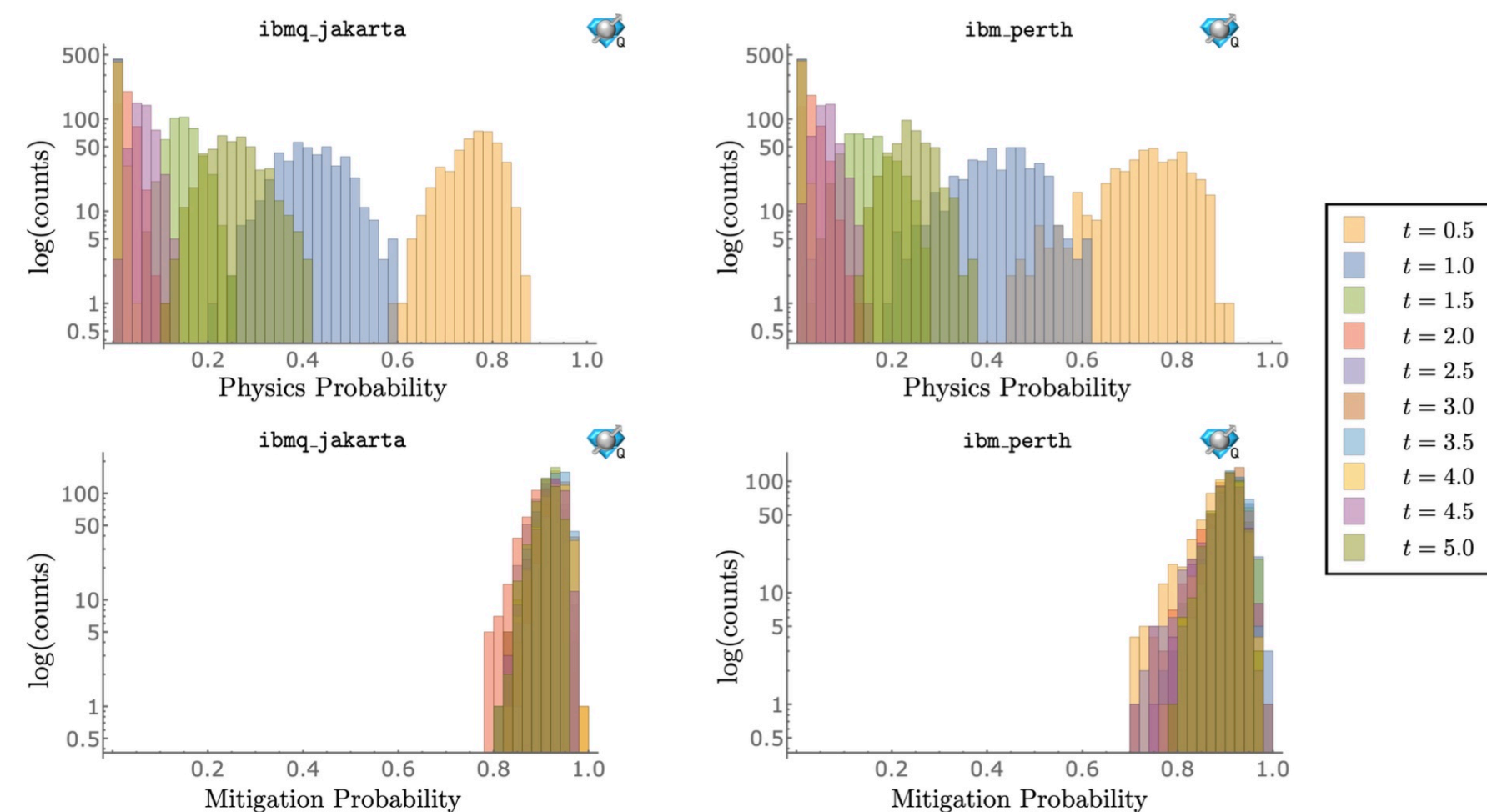
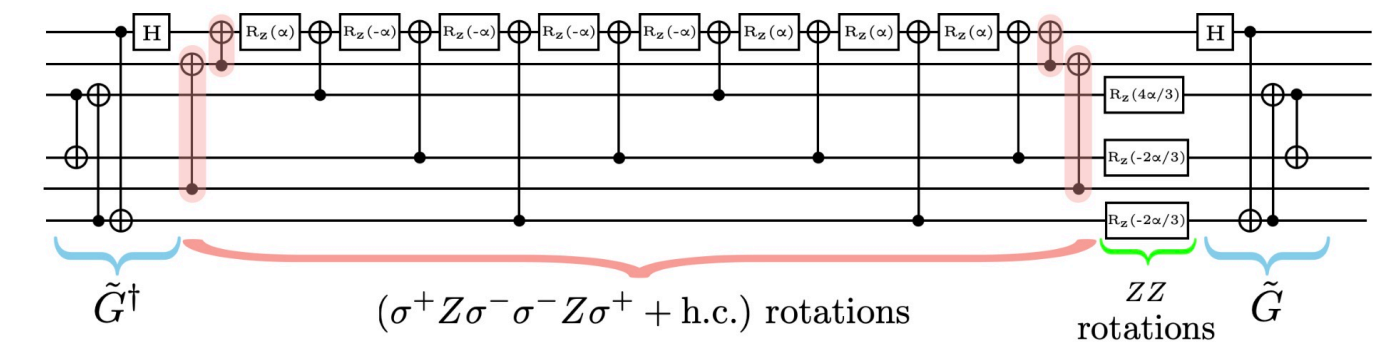


### IBM 7 qubit Perth and Jakarta

34 CNOTs per step  
447 Pauli-Twirled circuits  
1000 shots per circuits

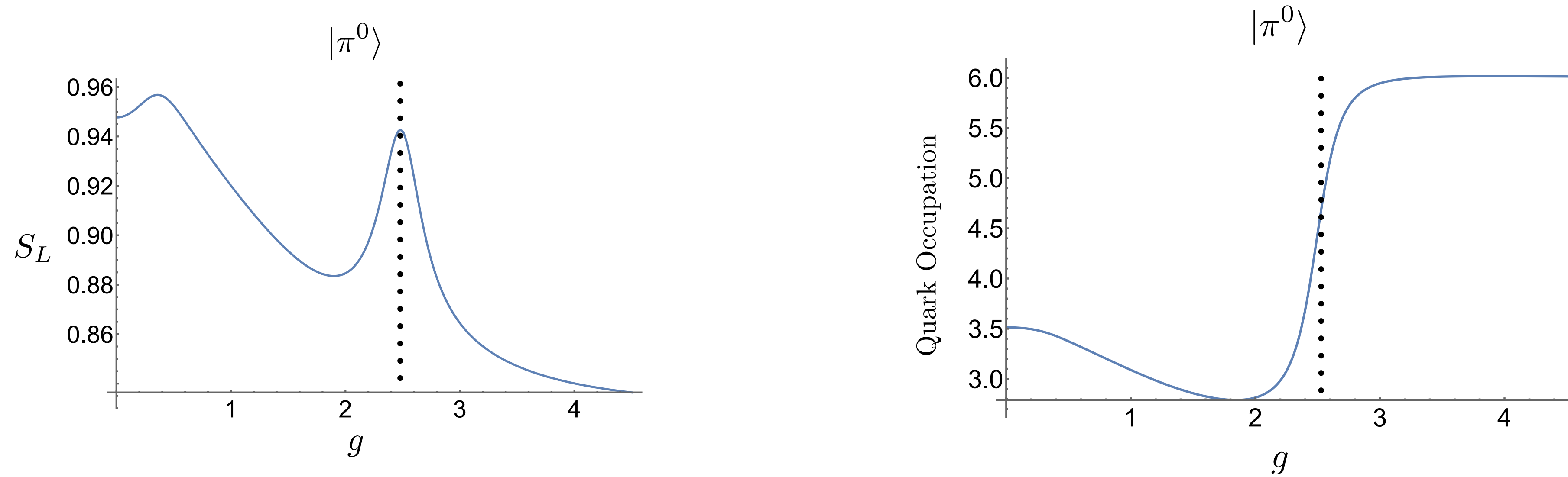


Dynamic Decoupling  
Pauli-Twirling  
Post selection  
De-coherence renormalization

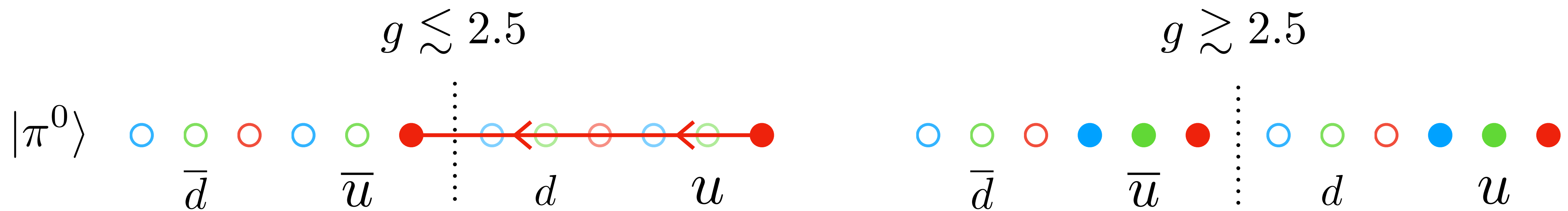


Number of CNOT gates for one Trotter step of $SU(3)$			
$L$	$N_f = 1$	$N_f = 2$	$N_f = 3$
1	30	114	242
2	228	878	1,940
5	1,926	7,586	16,970
10	8,436	33,486	75,140
100	912,216	3,646,086	8,201,600

# Entanglement structure in the mesons for $L = 2$

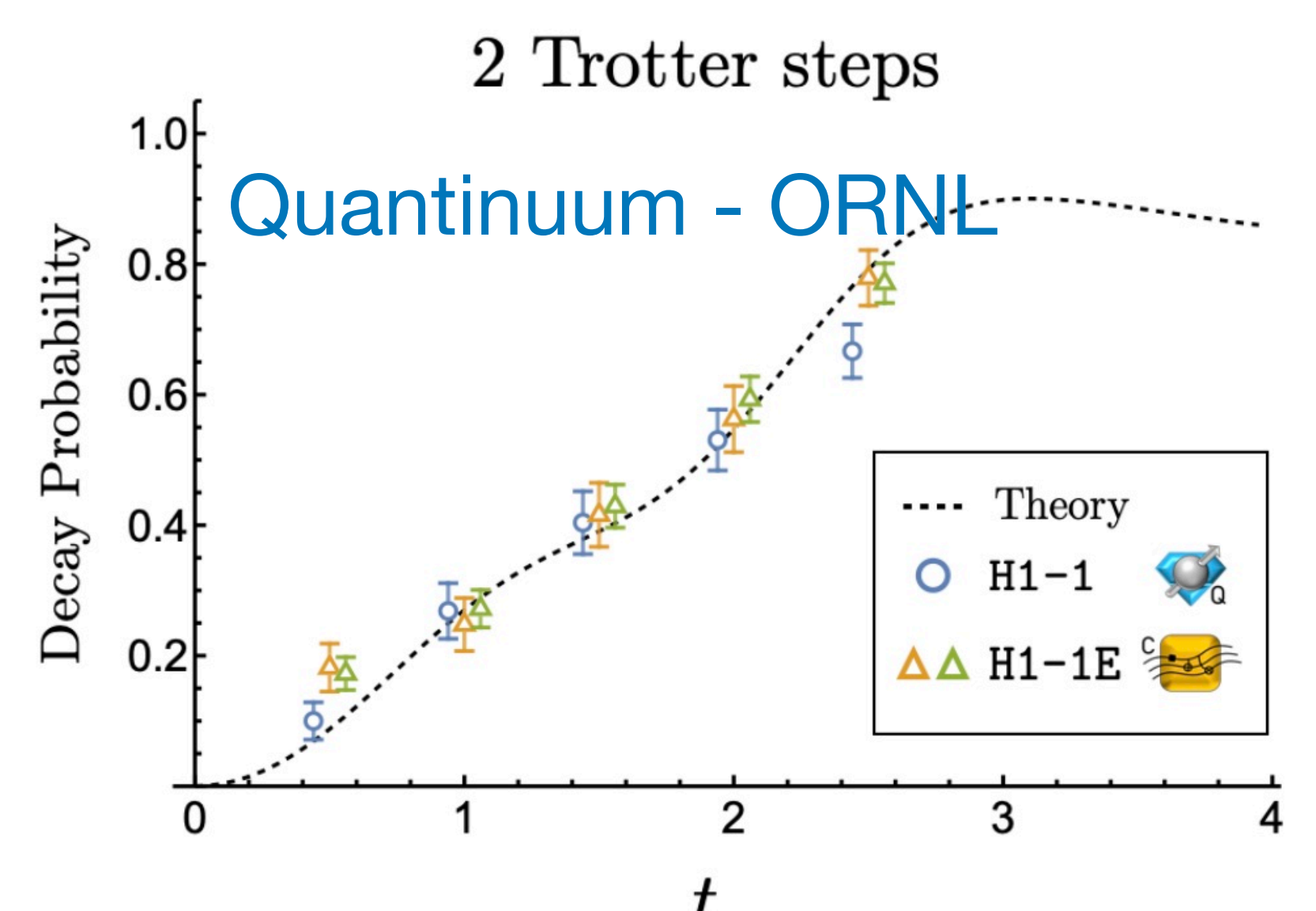
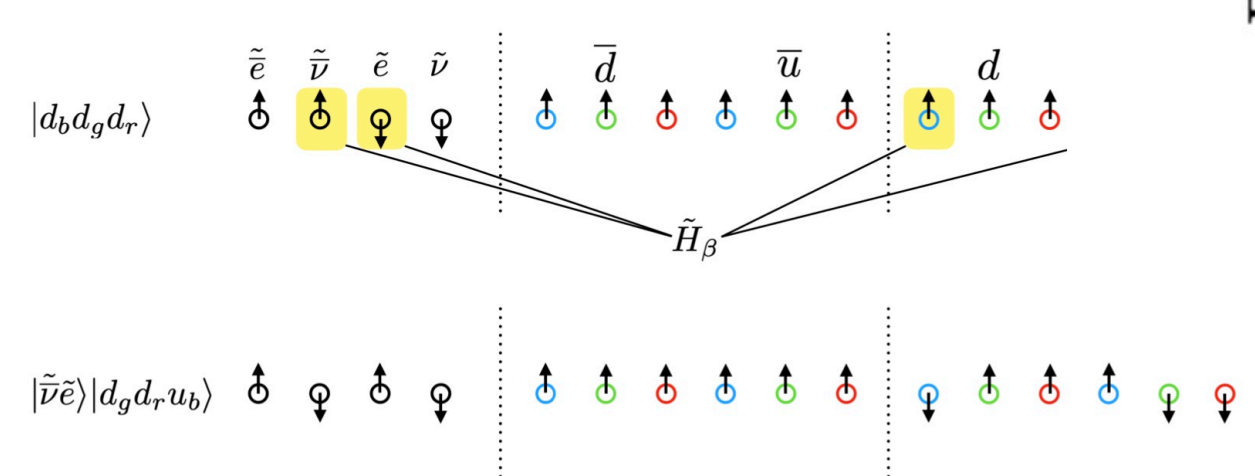
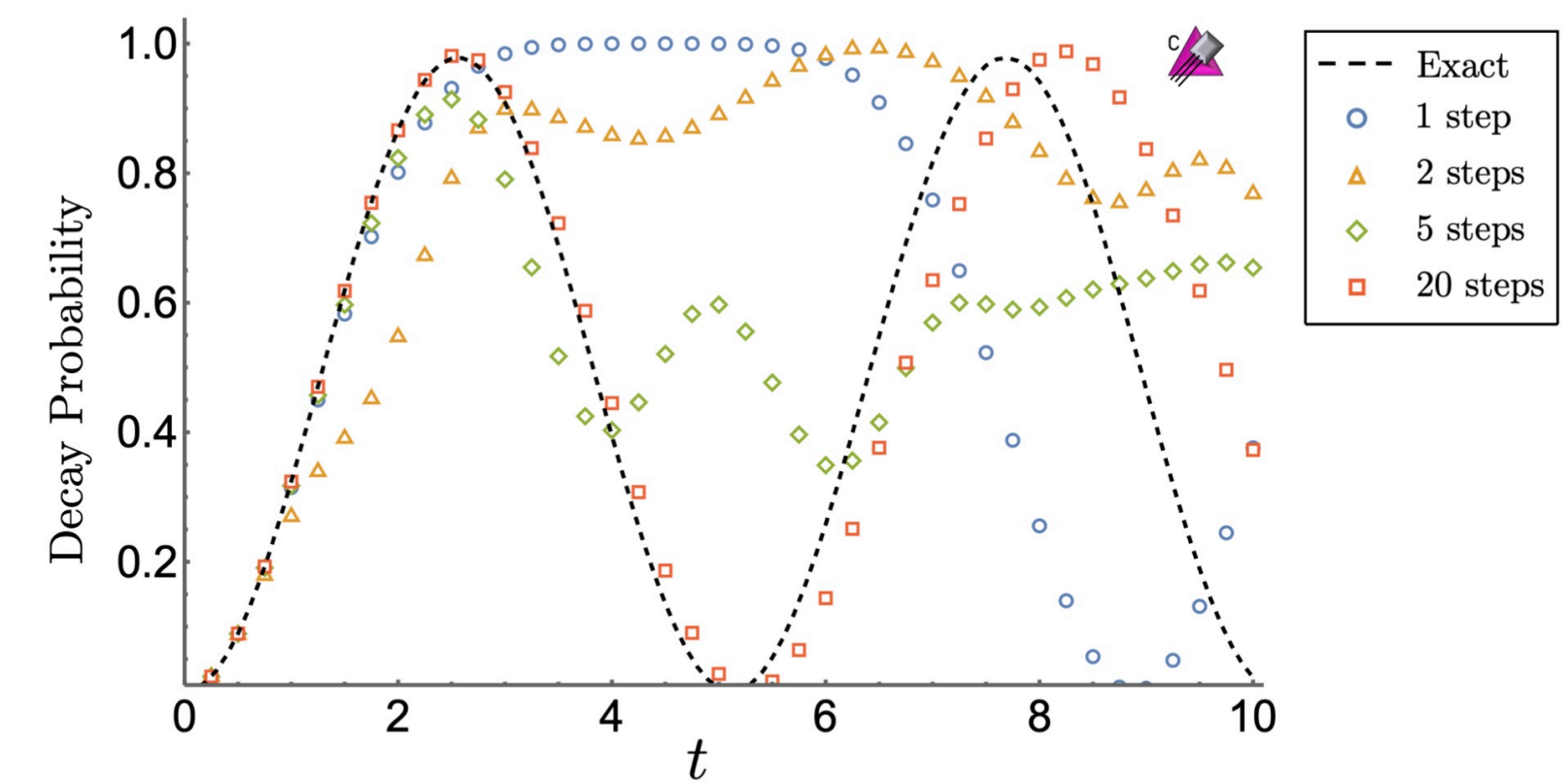
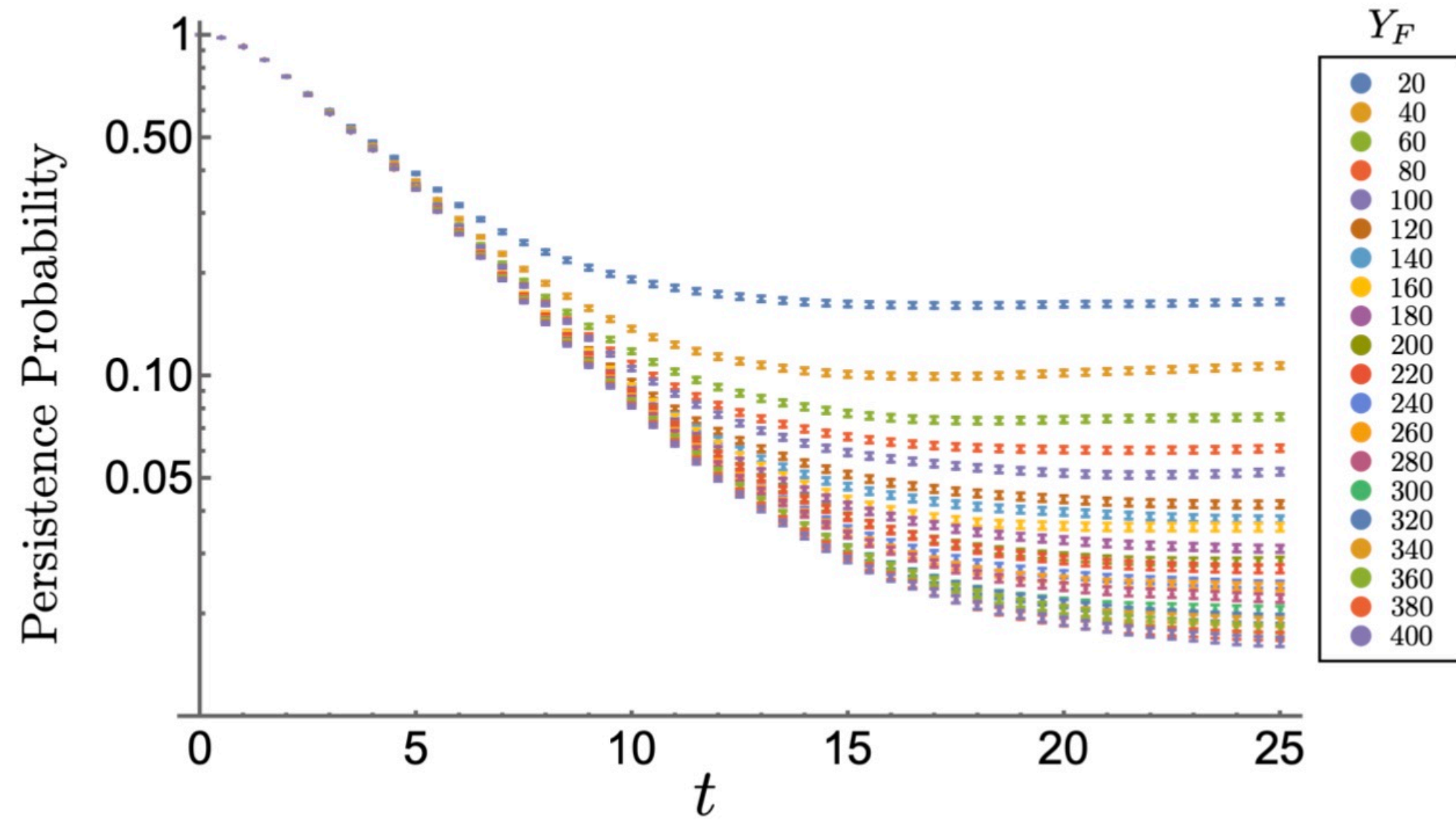
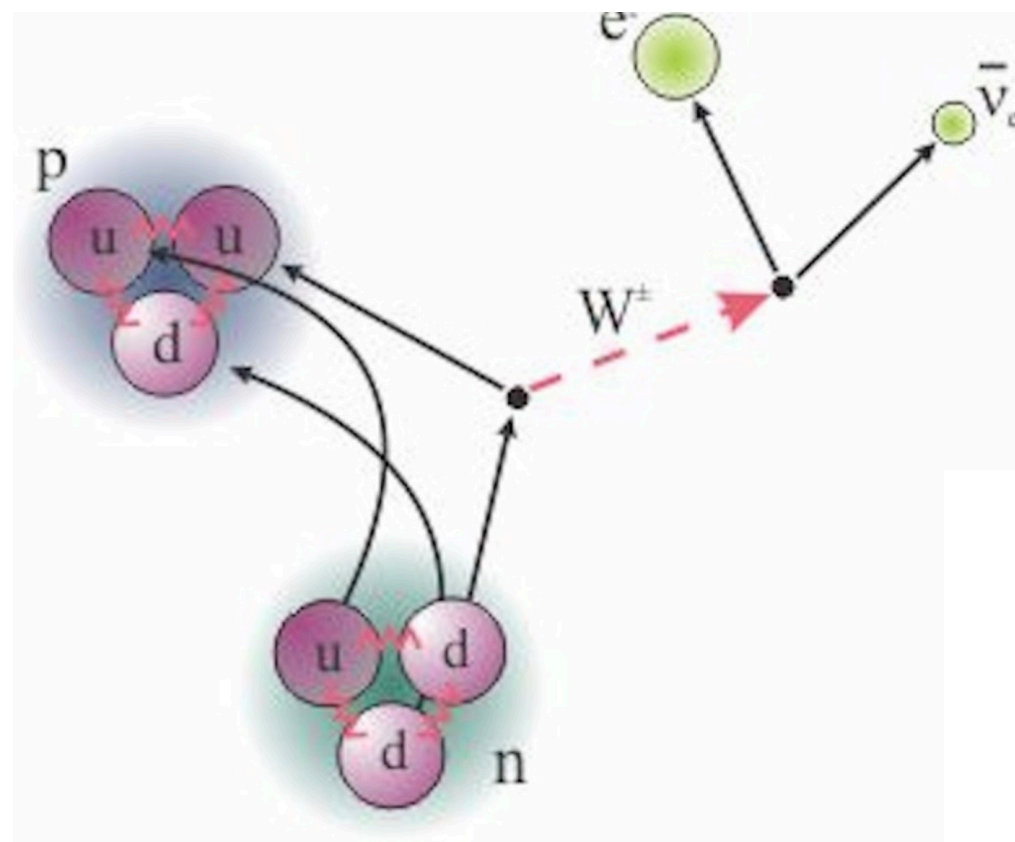


Peak in entanglement coincides with transition from quark-antiquark to baryon-anti-baryon structure

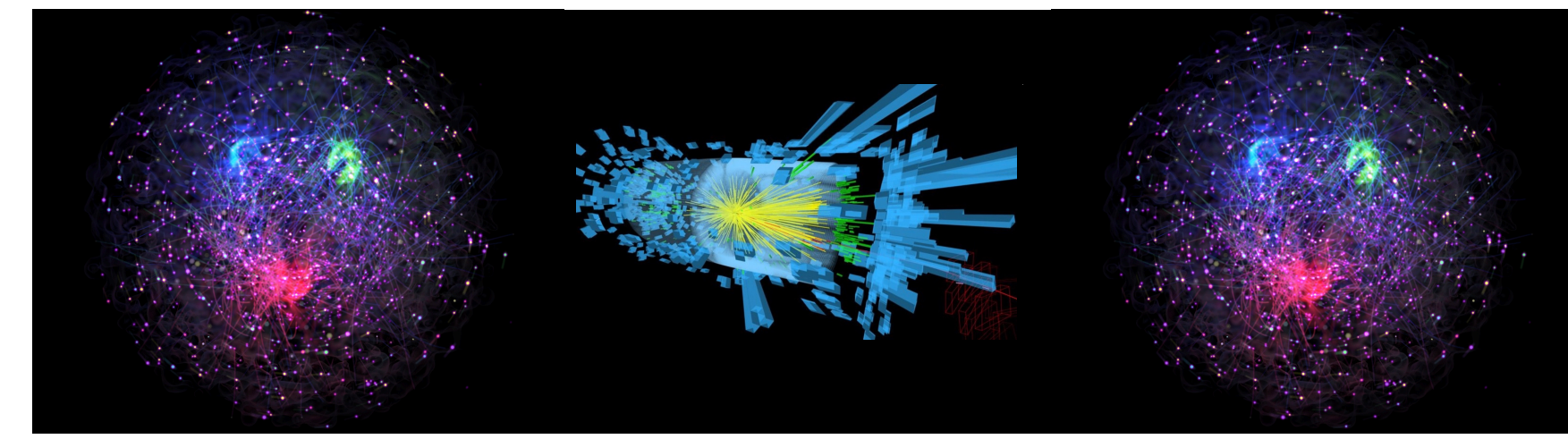


Balance between mass and gauge-field energies

# Real-time Exponential-Decay Weak Interactions



# (Classical) Steps Toward Hadronization and Fragmentation (in 1+1D)



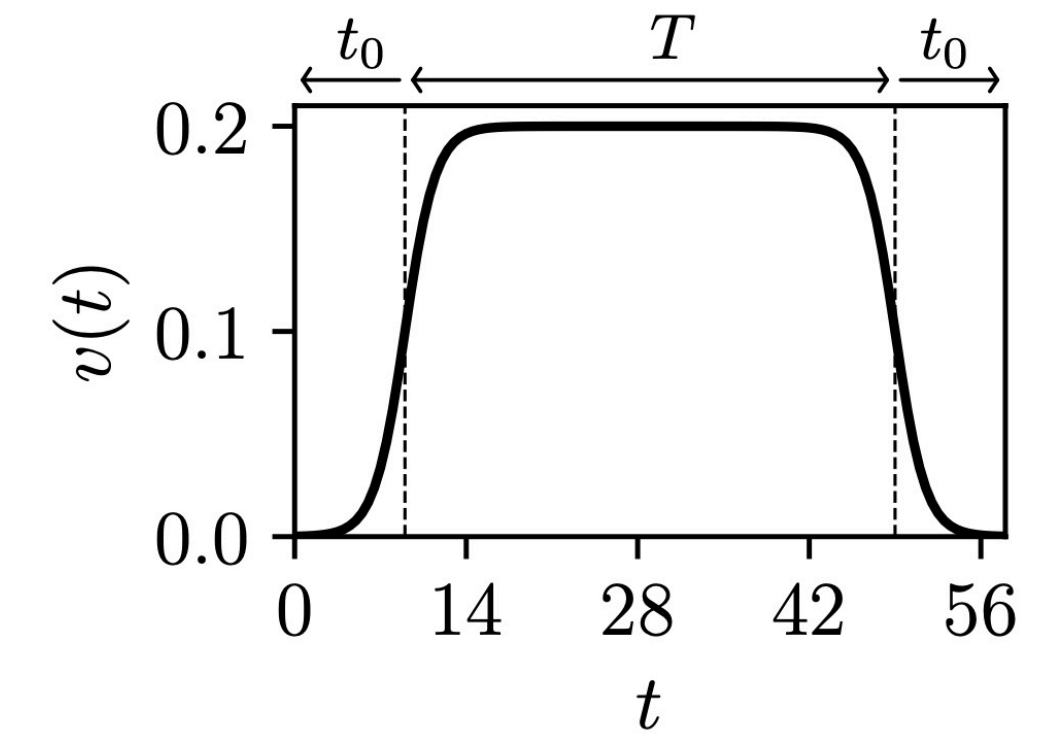
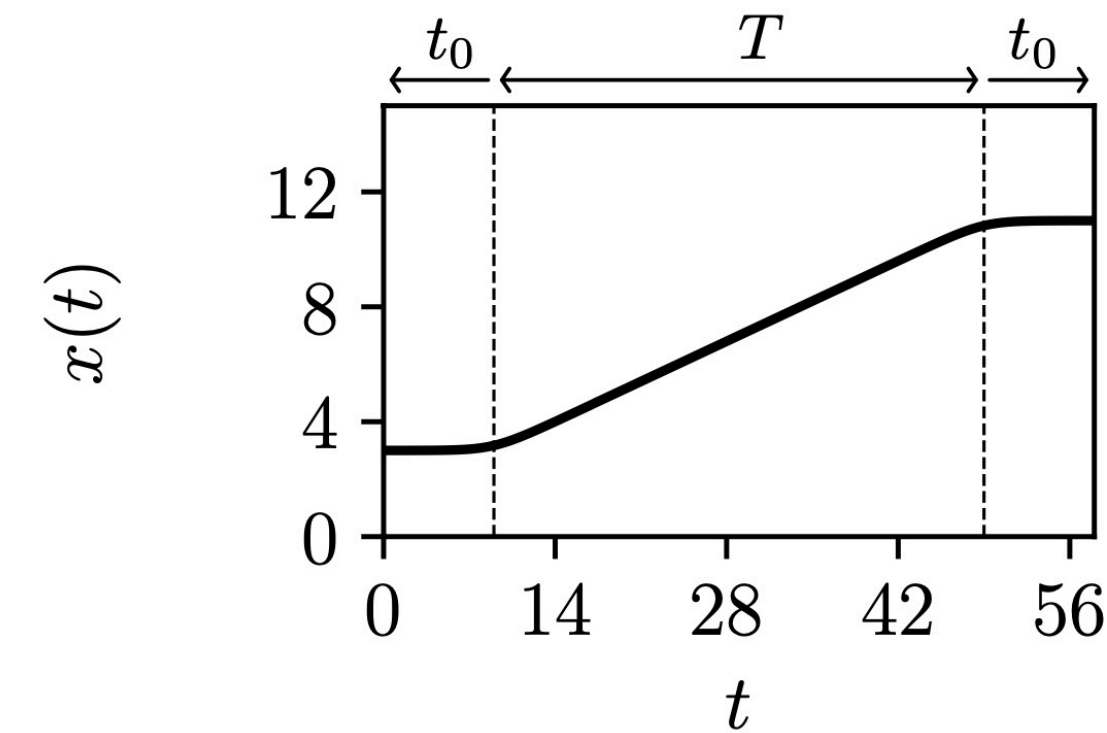
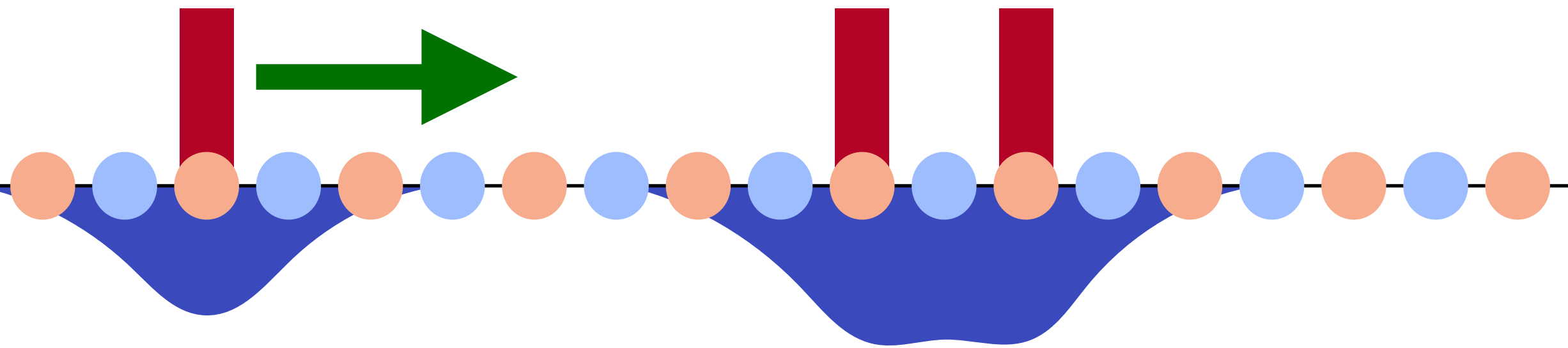
Steps Toward Quantum Simulations of Hadronization and Energy-Loss in Dense Matter

Roland C. Farrell (U. Washington, Seattle (main) and U. Bern, AEC), Marc Illa (U. Washington, Seattle (main)), Martin J. Savage (U. Washington, Seattle (main)) (May 10, 2024)

e-Print: [2405.06620](https://arxiv.org/abs/2405.06620) [quant-ph]



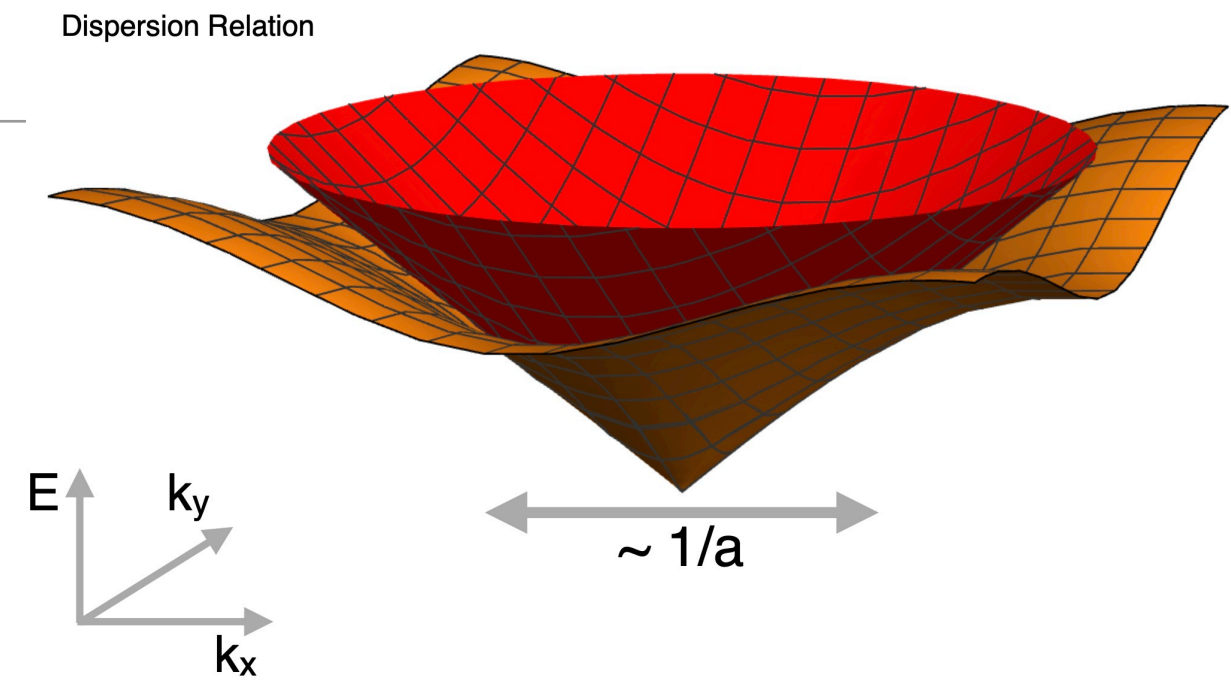
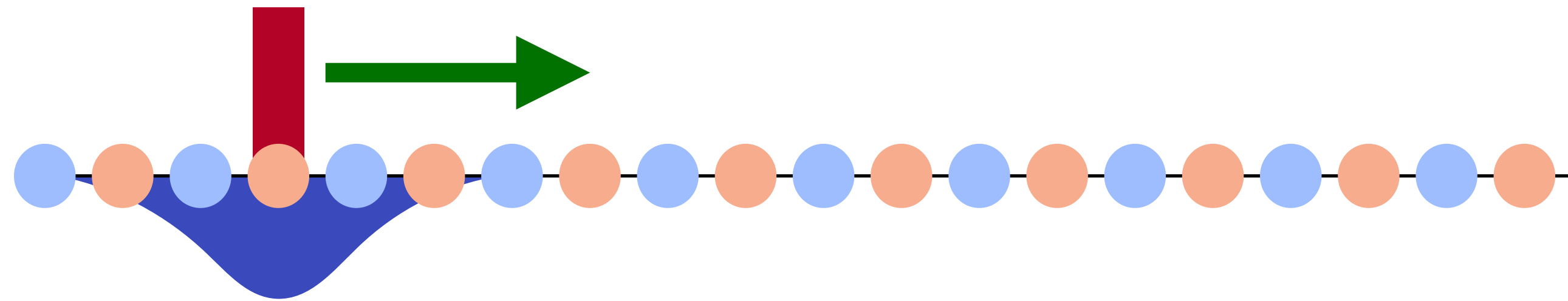
## Classical background charges



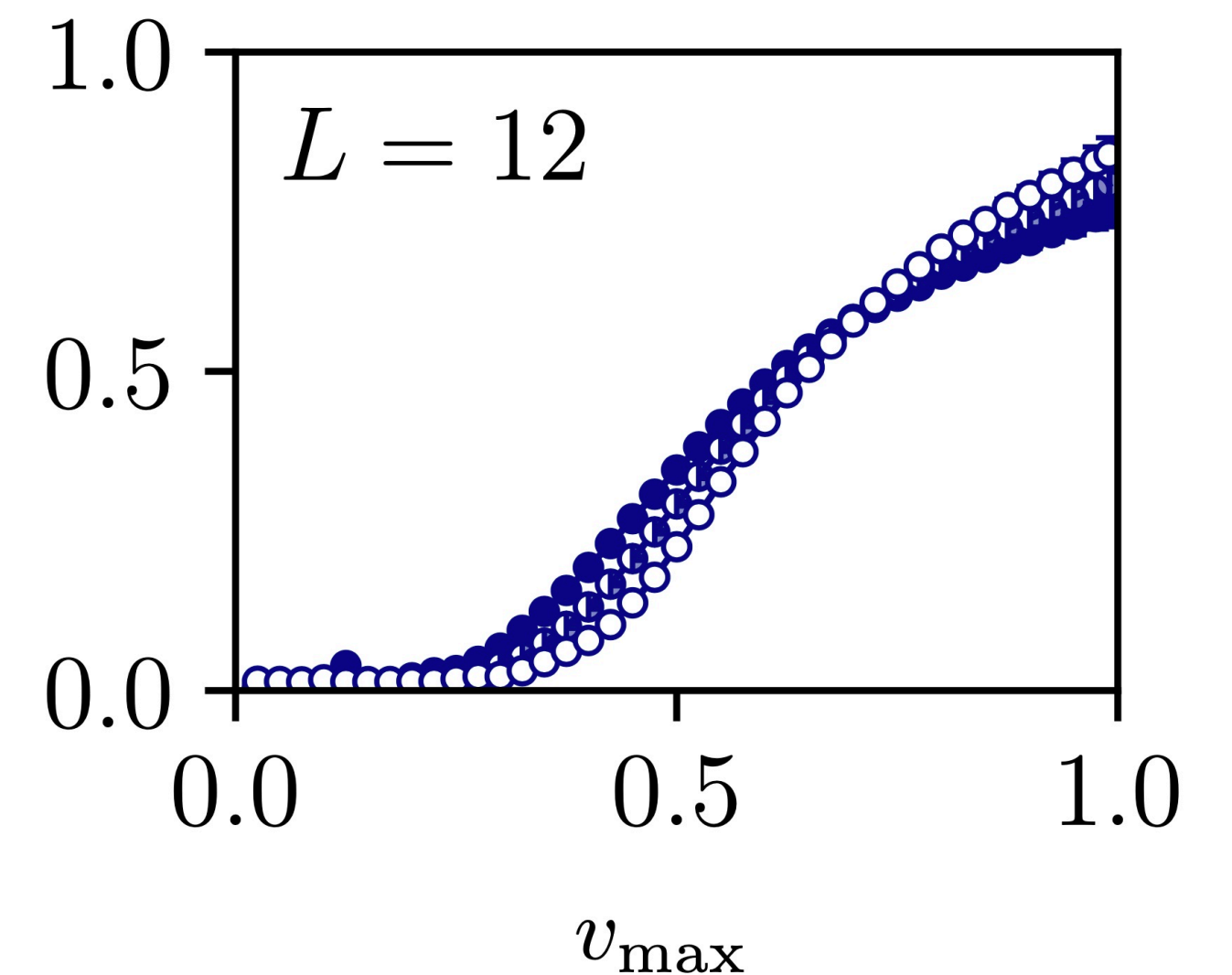
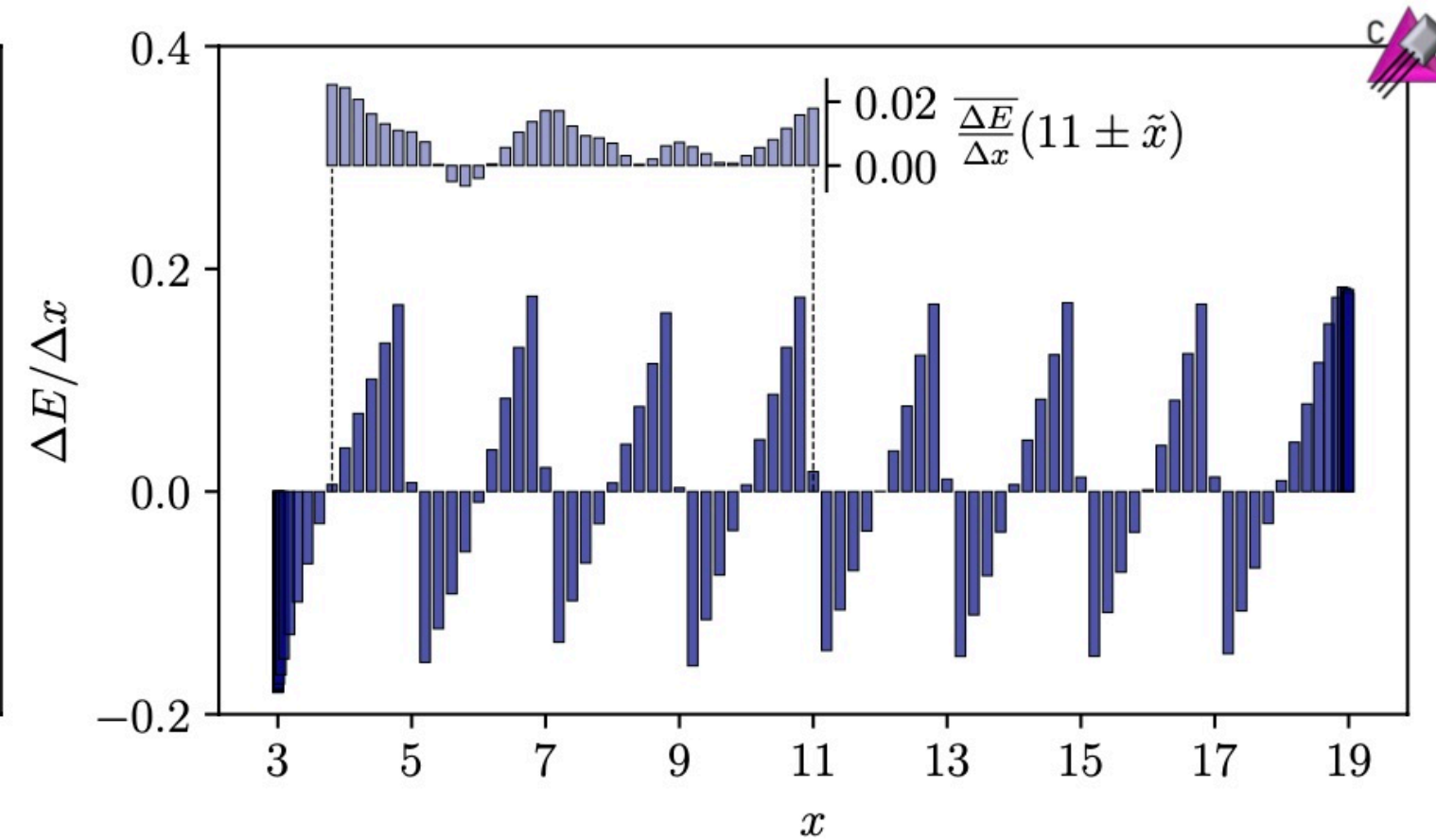
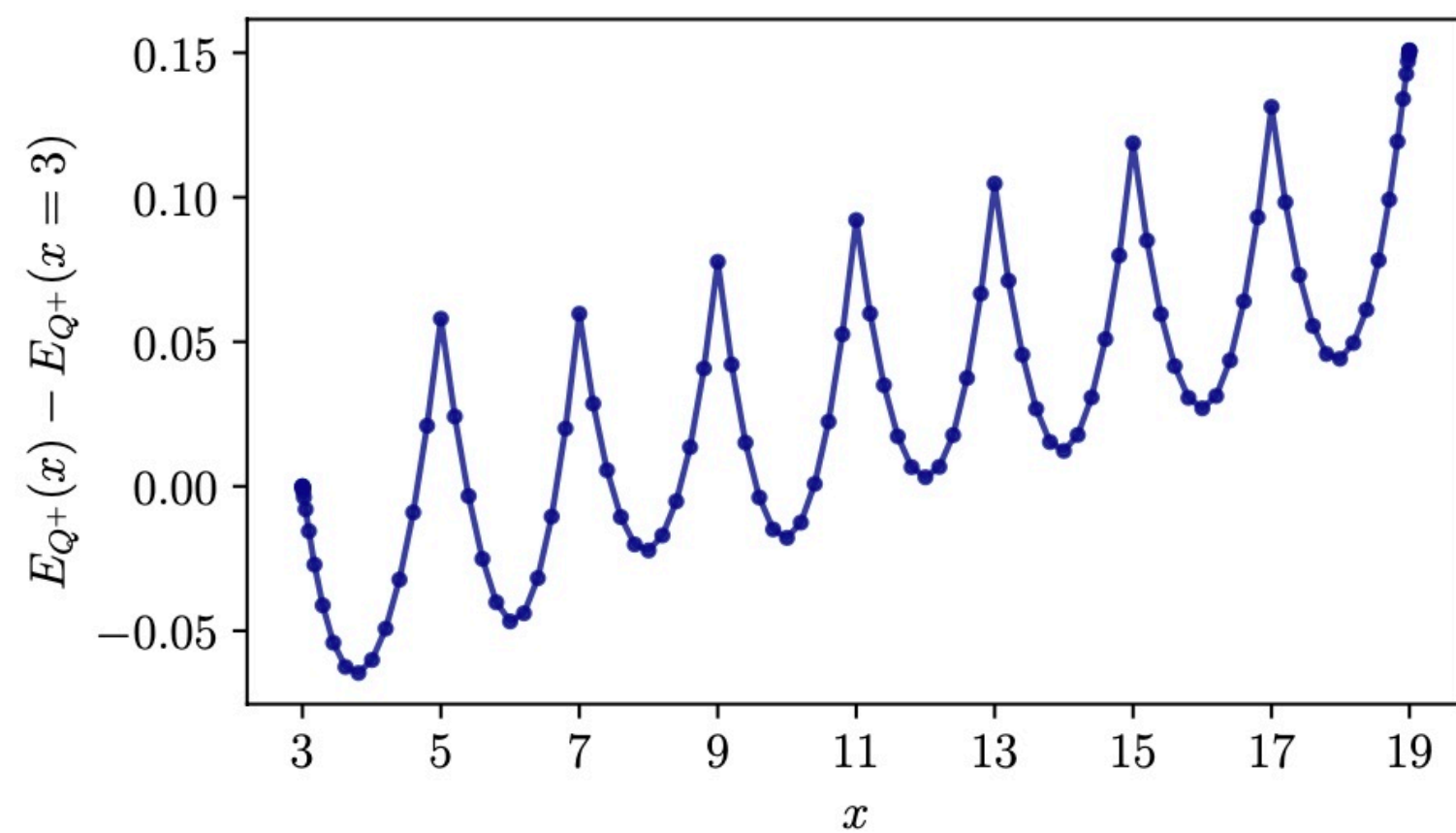
## Continuum and infinite volume limits

- Lattice spacing taken to zero
  - recover Lorentz symmetry, special relativity
- Length taken to Infinity
- Fixed physics with parametrically suppressed corrections
- Present quantum resources ~ limit lattice size and spacing (number of sites)
  - Classical HPC simulations only at present - quantum circuit depth
- Lattice spacing artifacts large

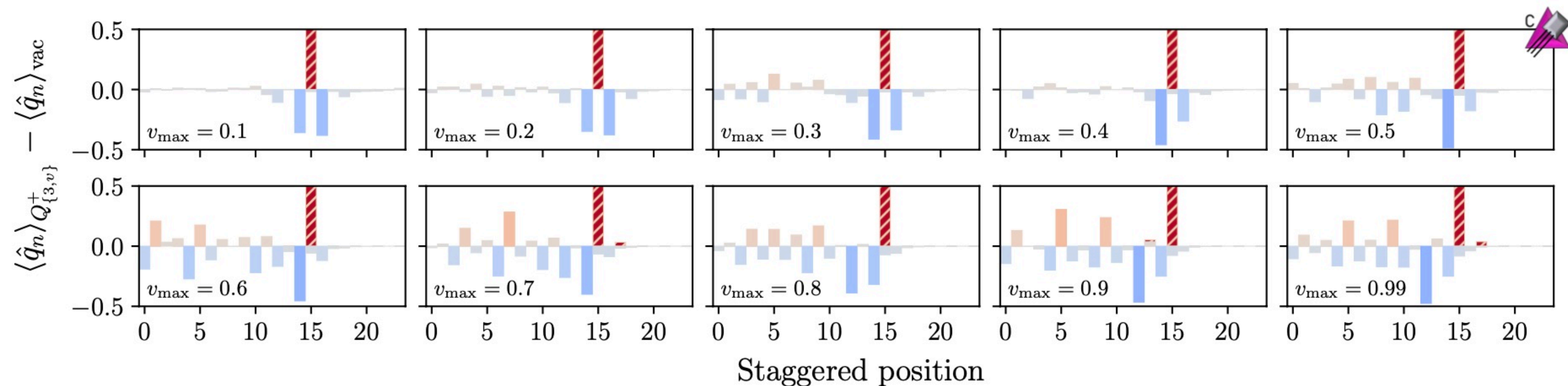
# Lorentz Violation by Lattice Spacing



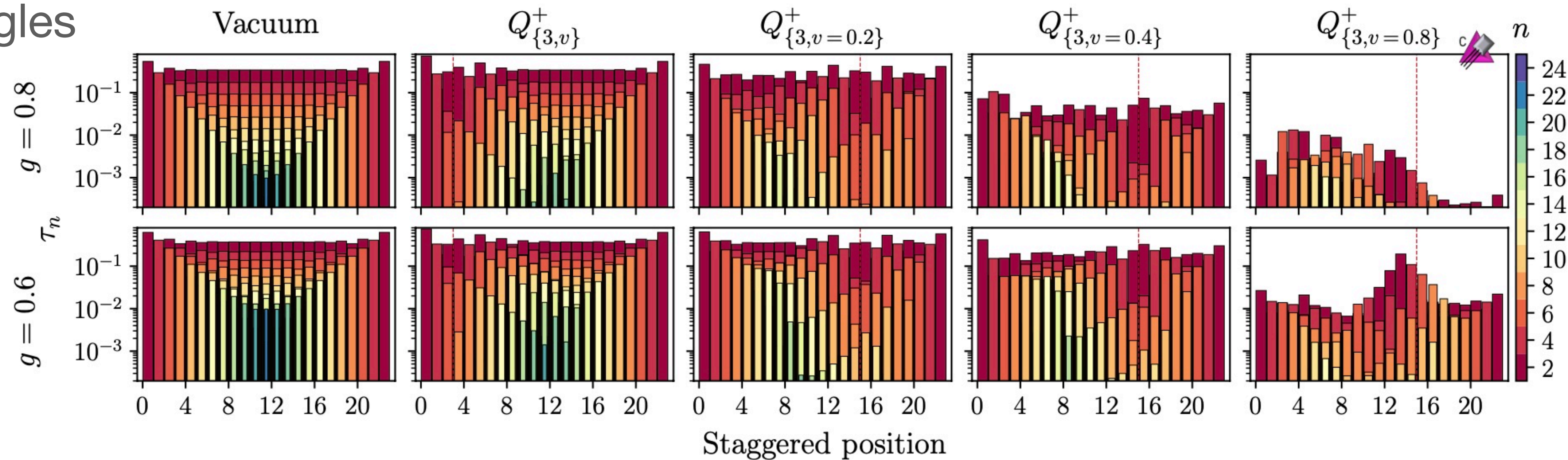
- Lorentz invariance dictates energy conservation at fixed velocity in vacuum
- Energy loss into the light degrees of freedom is
  - a lattice spacing artifact
  - creating hadrons with some probability on top of the vacuum - useful but not physics



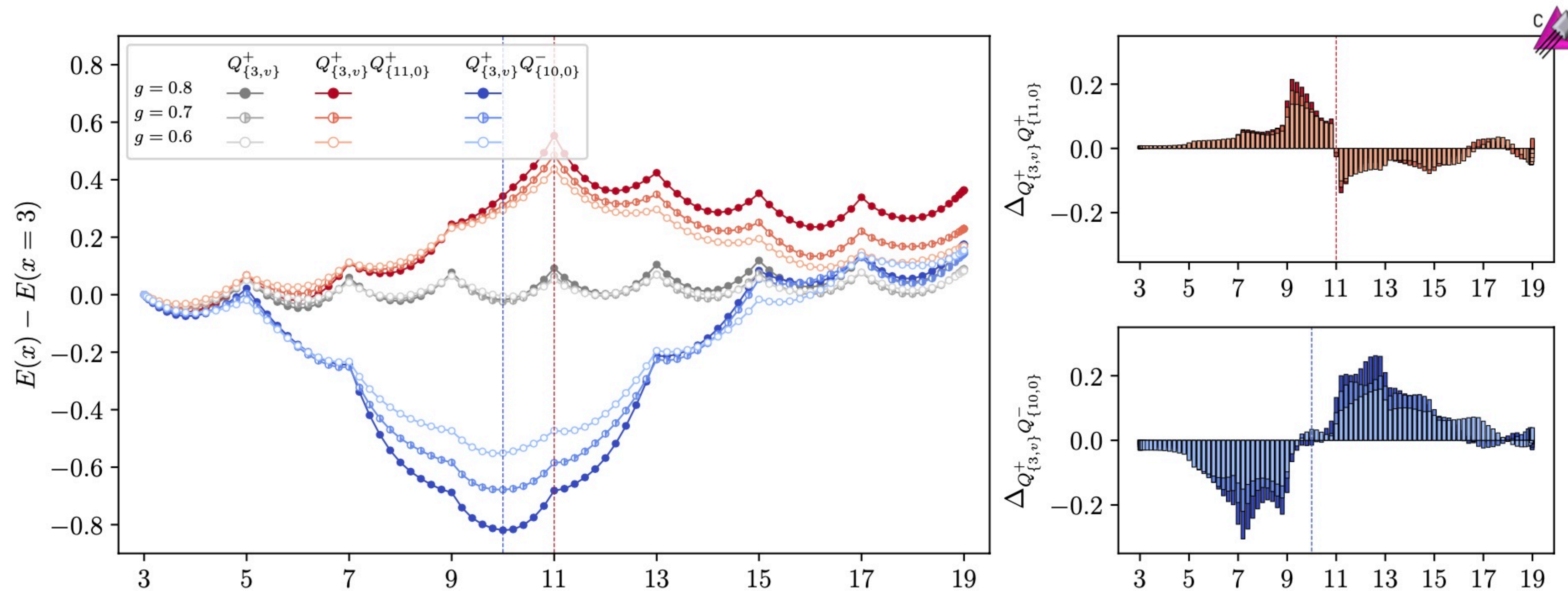
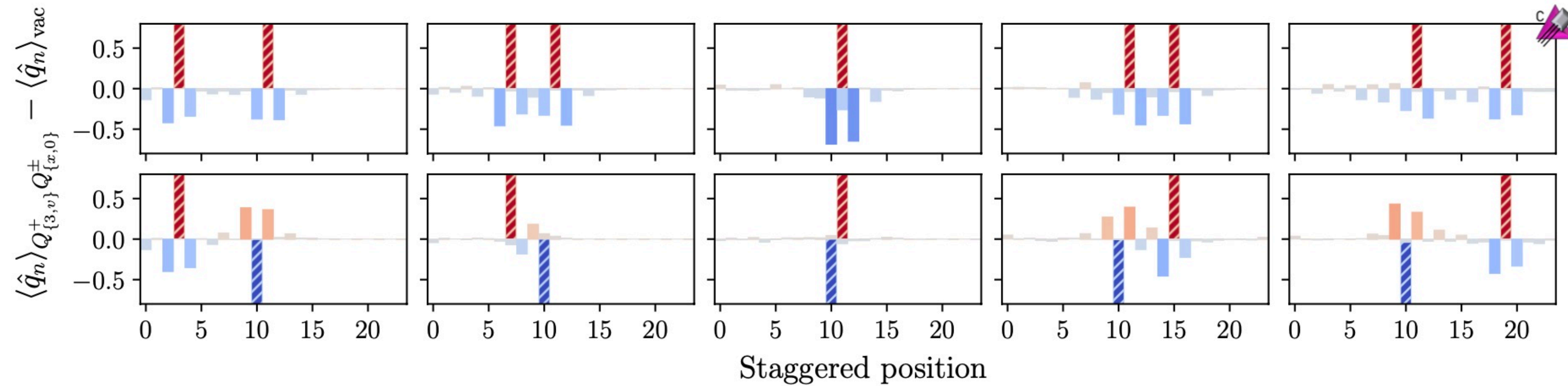
# Lorentz Violation by the Lattice Spacing



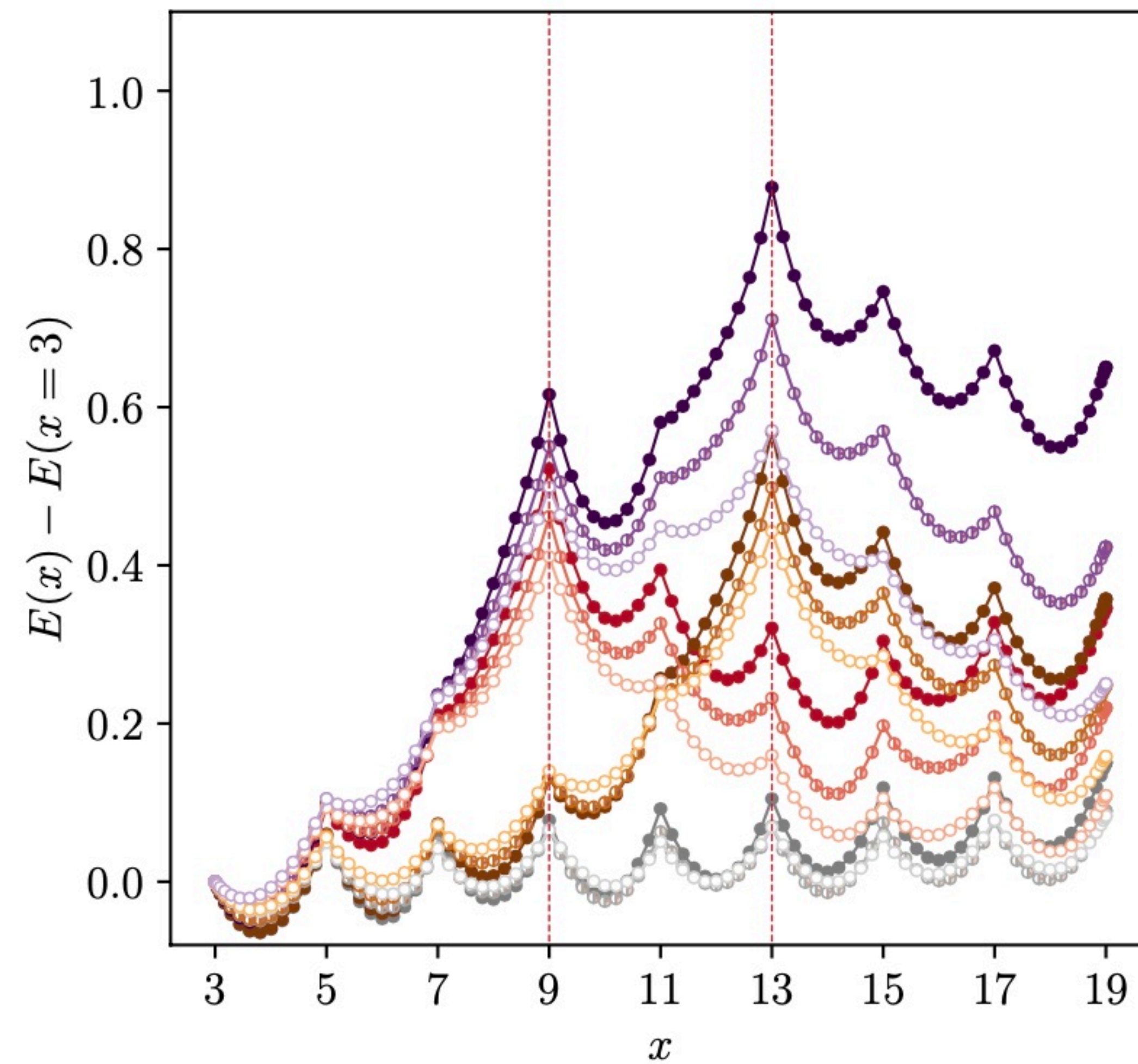
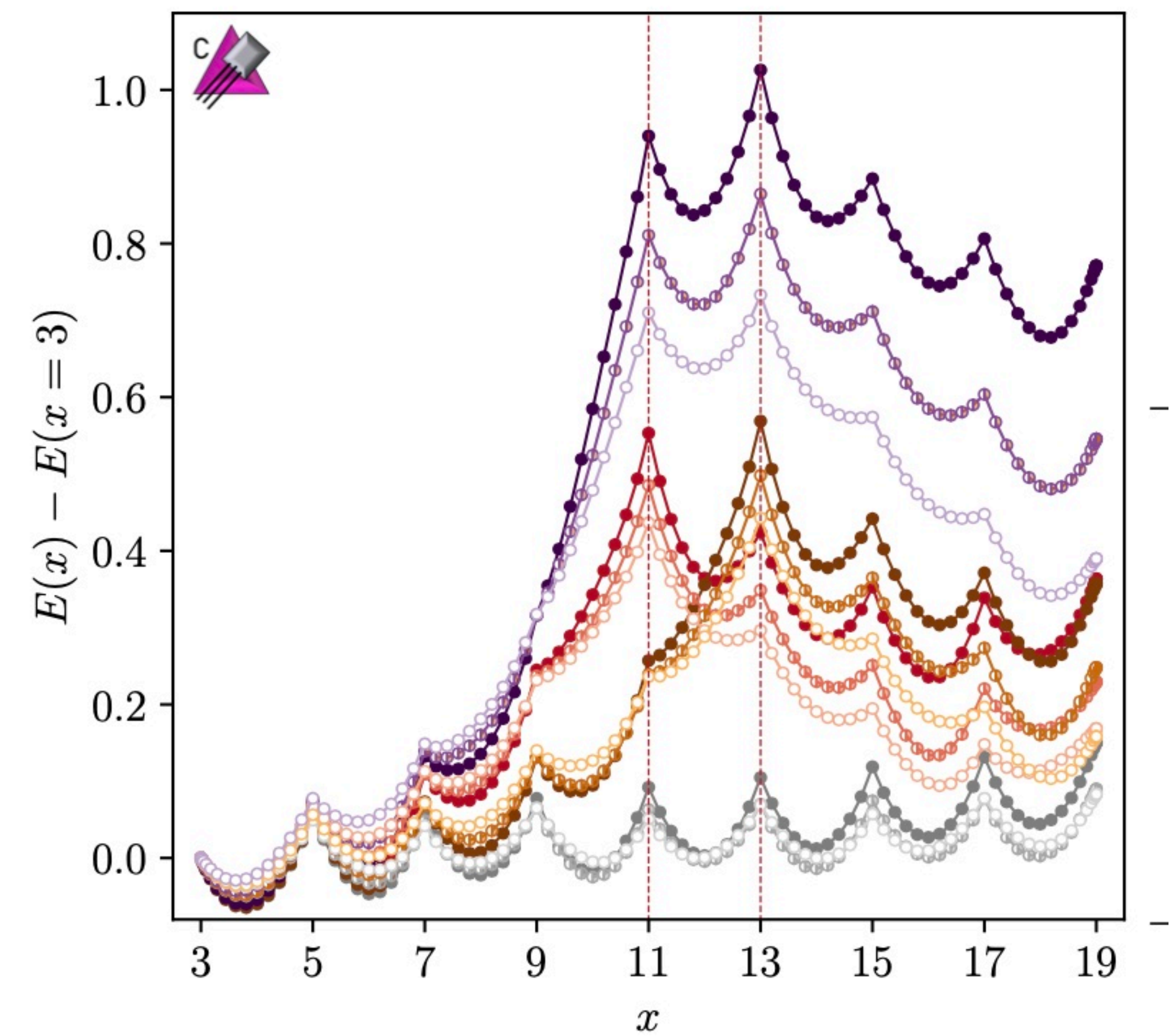
n-tangles



# Colliding Partons



# Matter and Coherence





# Dynamical Quantum Phase Transitions

## Dynamical topological transitions in the massive Schwinger model with a $\theta$ -term

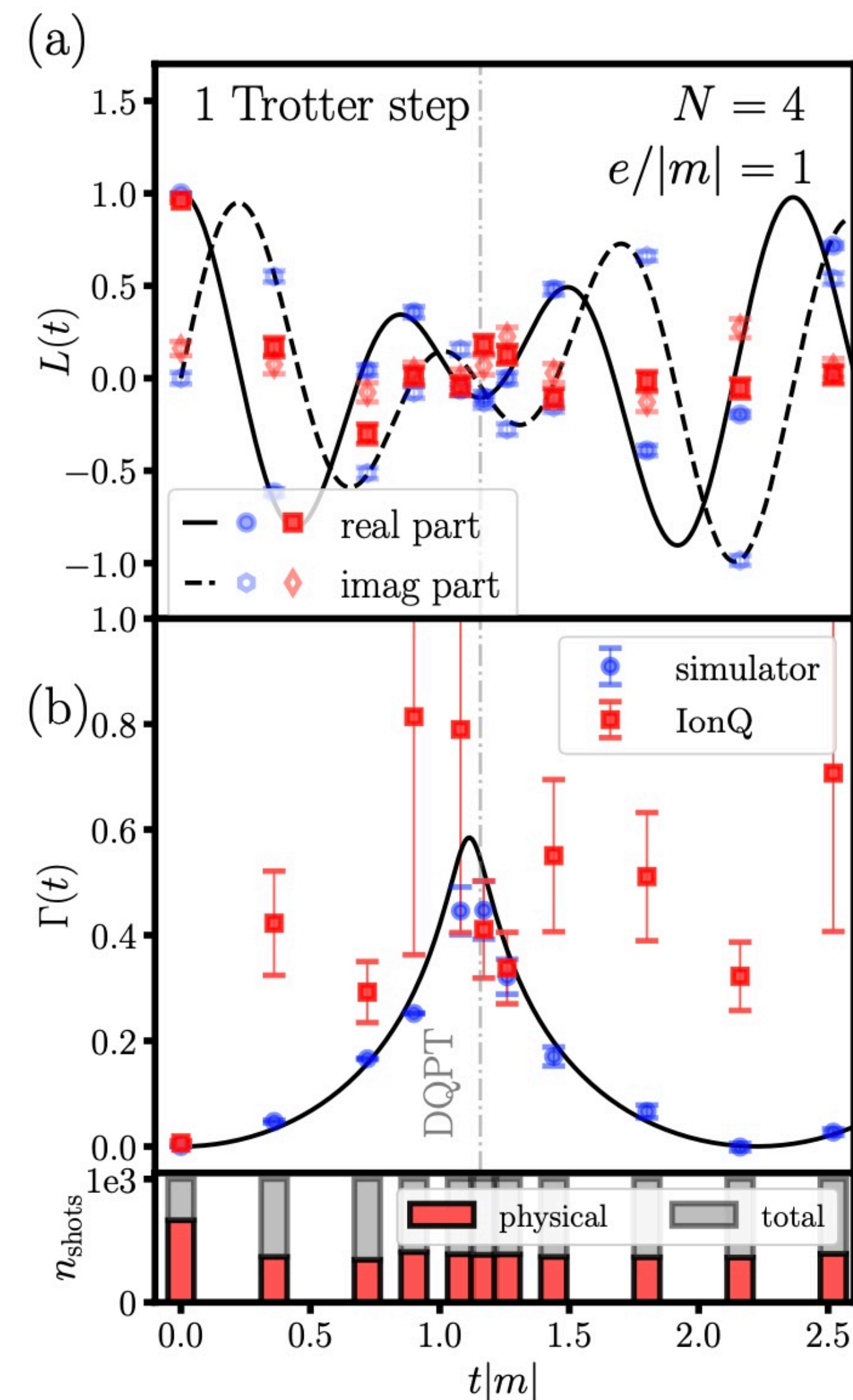
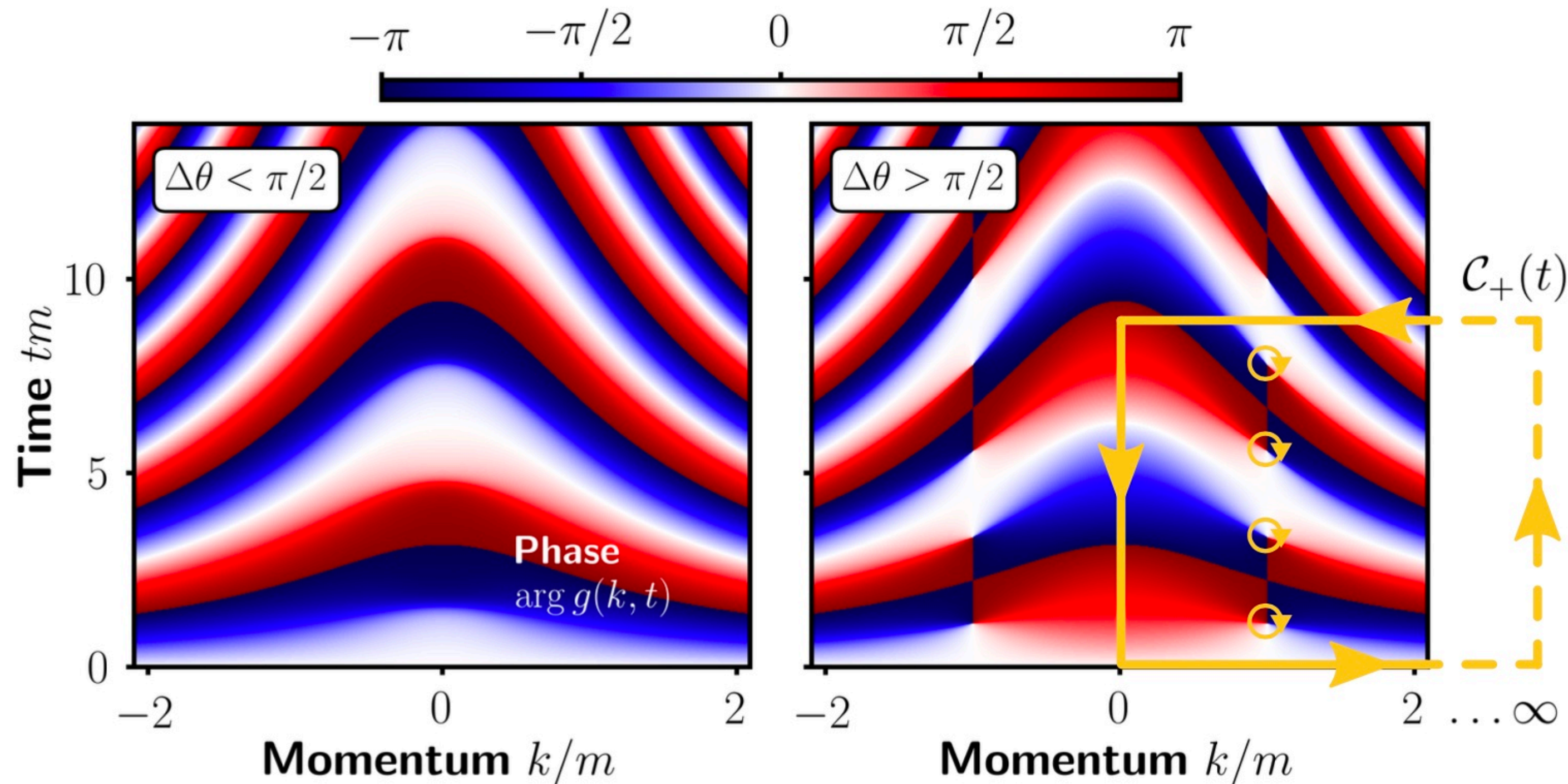
T. V. Zache,<sup>1,\*</sup> N. Mueller,<sup>2</sup> J. T. Schneider,<sup>1</sup> F. Jendrzejewski,<sup>3</sup> J. Berges,<sup>1</sup> and P. Hauke<sup>1,3</sup>

2018

## Quantum computation of dynamical quantum phase transitions and entanglement tomography in a lattice gauge theory

Niklas Mueller,<sup>1,2,3,\*</sup> Joseph A. Carolan,<sup>4</sup> Andrew Connelly,<sup>5</sup>  
Zohreh Davoudi,<sup>1,6,†</sup> Eugene F. Dumitrescu,<sup>7,‡</sup> and Kübra Yeter-Aydeniz<sup>8</sup>

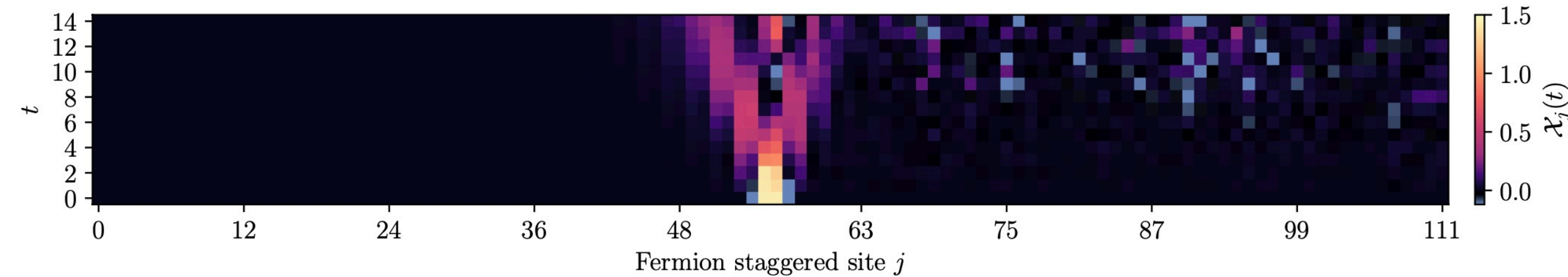
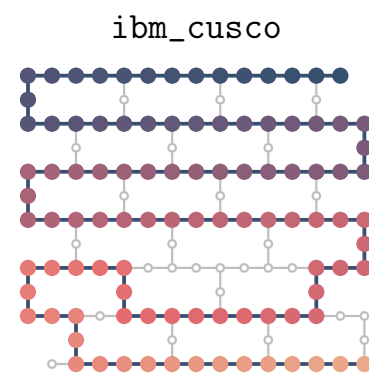
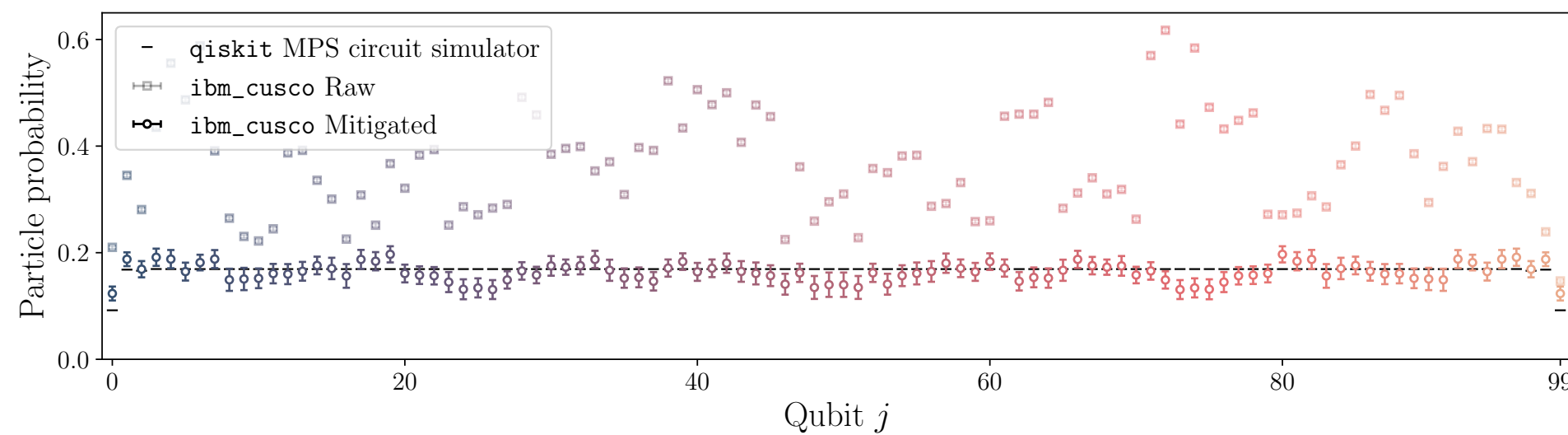
2023



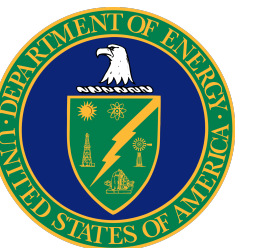


# Summary

**Roland Farrell**  
**Marc Ila**  
**Anthony Ciavarella**

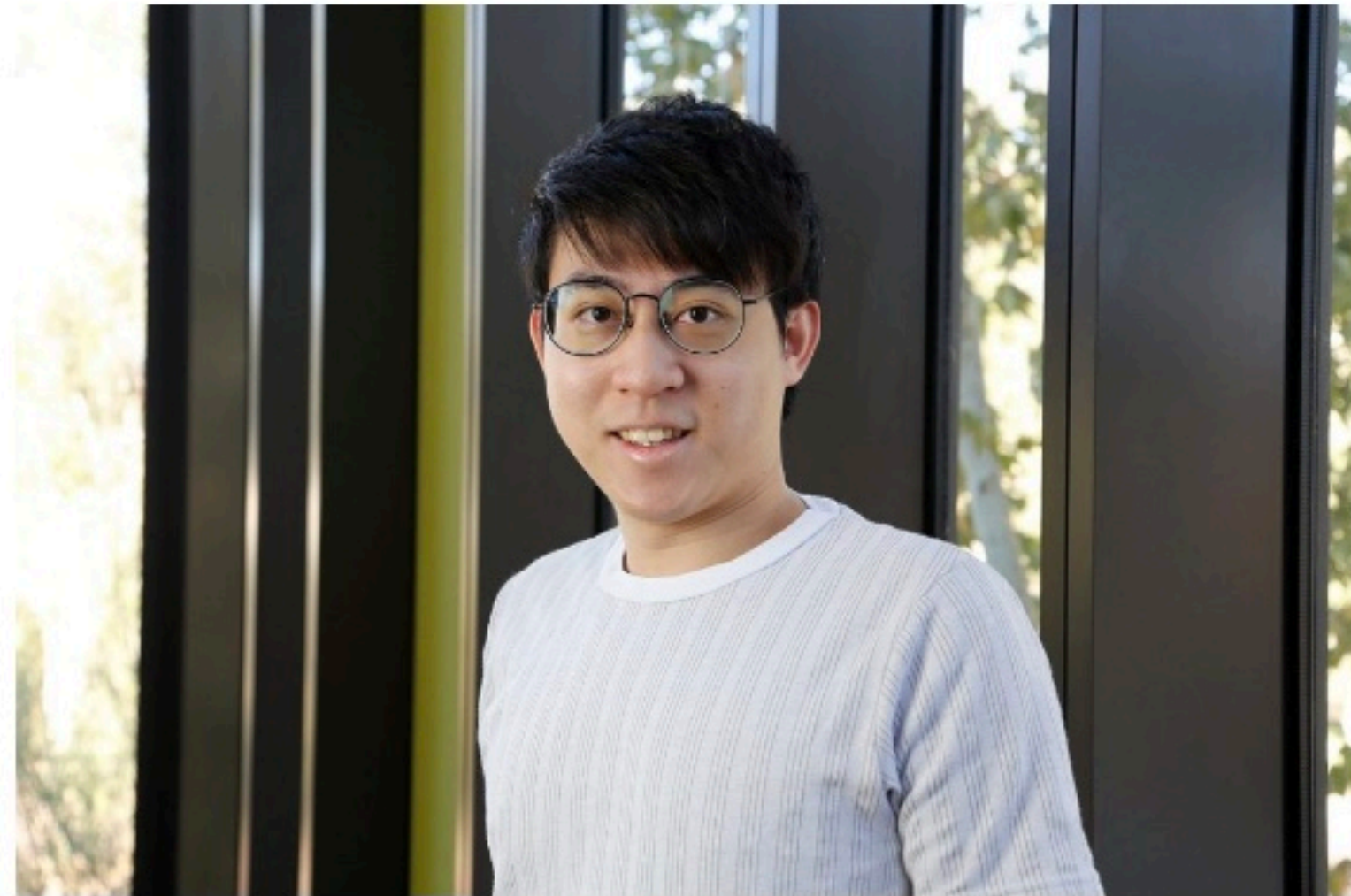


- Quantum Simulations are essential for advancing capabilities in describing dynamical quantum systems.... Standard Model physics and beyond.
- 1+1D systems are a key developmental arena for 3+1D simulations
  - conceptual, algorithmic, workflow, co-design
  - confinement, charge screening, fermion condensate, hadrons
- We introduced of scalable quantum circuits for lattice QFT simulations, and showed our results from  $>100$  qubits,  $>14k$  entangling gates
- Quantum Magic and Multi-partite Entanglement are “new” areas being pursued (see Caroline Robin’s talk tomorrow)





# Seminar

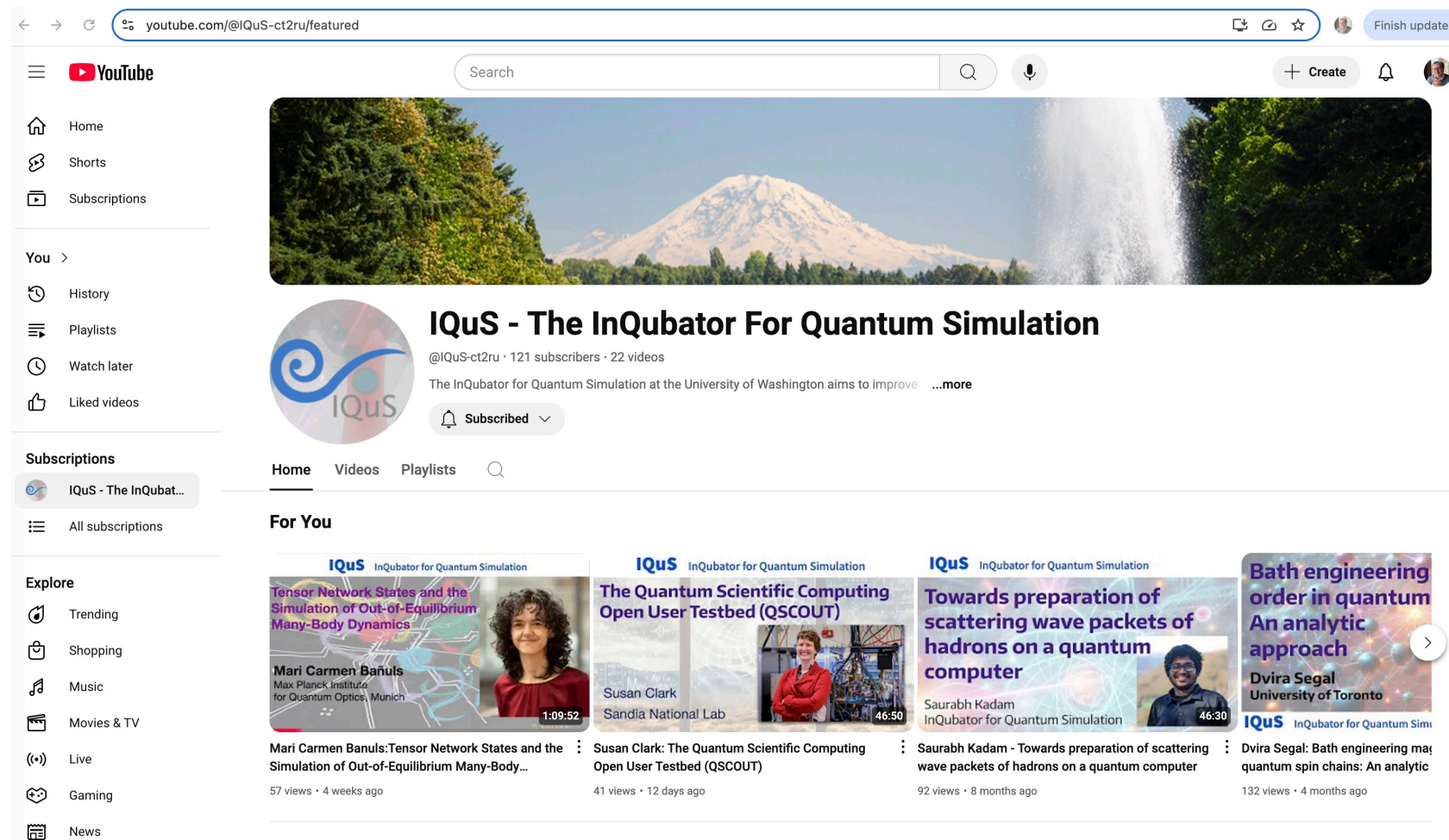


📅 Wednesday Oct 16 2024 ⌚ 1:30 pm - 2:30 pm

## What cannot be learned in the quantum universe?

Hsin-Yuan (Robert) Huang, Google Quantum AI and Caltech. Online participation available.

📍 C520 Physics and Astronomy Building



FIN